

CSE211: Compiler Design

Oct. 18, 2021

- **Topic:** Introduction to Module 2: analysis and optimizations!
- **Questions:**
 - *What sort of compiler optimizations do you know about?*
 - *What sort of intermediate representations do you know about?*

Announcements

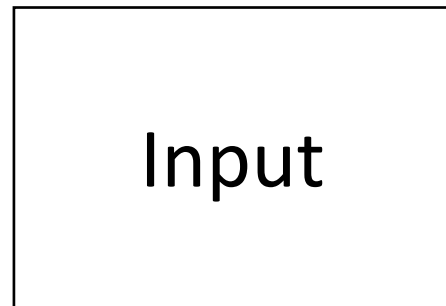
- Homework 1 is out
 - Due on the 25th
 - One week!
 - No extensions
- Get your paper reading approved by me by Monday
 - No extensions, 5% of your grade
- One more office hour:
 - Thursday 3 – 5 PM

Announcements

- I will be gone Monday and Wednesday next week to attend a khronos group meeting.
 - The schedule is still in flux:
 - either I will hold class synchronously on Zoom
 - Or provide asynchronous lectures
 - Maybe a combination, stay tuned

On to Module 2!

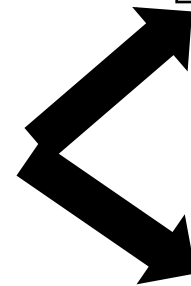
Optimizations and analysis



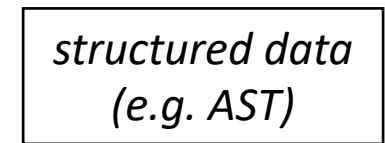
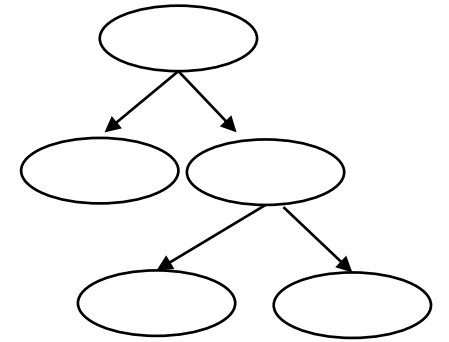
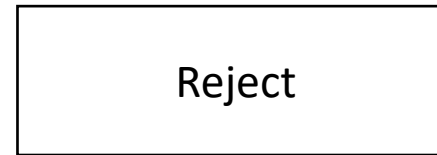
A string



*Language
Recognizer for
language L*

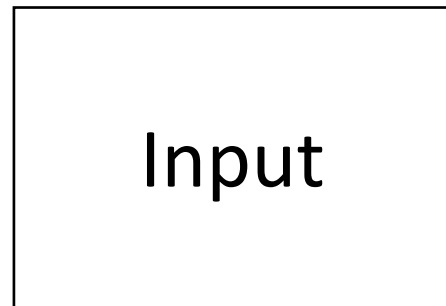


*continue to the rest
of compilation*

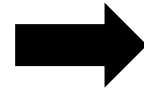


On to Module 2!

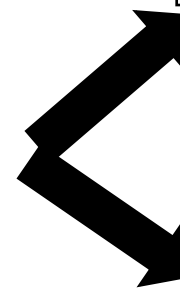
Optimizations and analysis



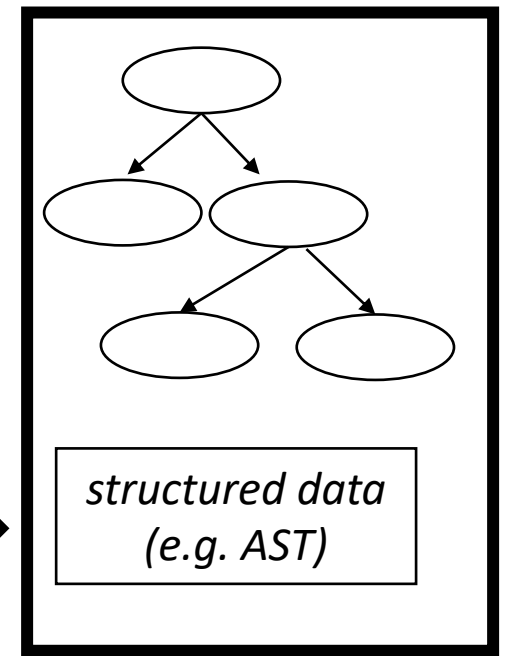
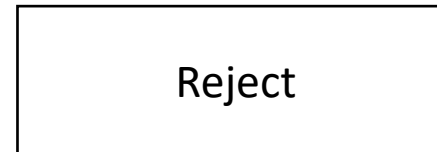
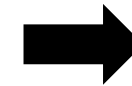
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*Language
Recognizer for
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*continue to the rest
of compilation*



**Where most
optimizations
and flow analysis
happens!**

Intermediate representations (IRs)

- Intermediate step between human-accessible programming languages and horrible machine ISAs
- Ideal for analysis because:
 - More regularity than high-level languages (simple instructions)
 - Less constraints than ISA languages (virtual registers)
 - ***Machine-agnostic optimizations***
 - See Godbolt example

$x = y + z;$
 $w = y + z;$  $x = y + z;$
 $w = x;$

Different IRs

Many different IRs, each have different purposes

- Trees
 - Abstract syntax trees
 - Data-dependency trees
 - **Good for instruction scheduling**
- Textual
 - 3 address code
 - **Good for removing redundant expressions**
- Graphs
 - Control flow graphs
 - **Good for data flow analysis (finding uninitialized variables)**

Different IRs

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 - Control flow graphs
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What are some examples of a modern compiler pipeline?

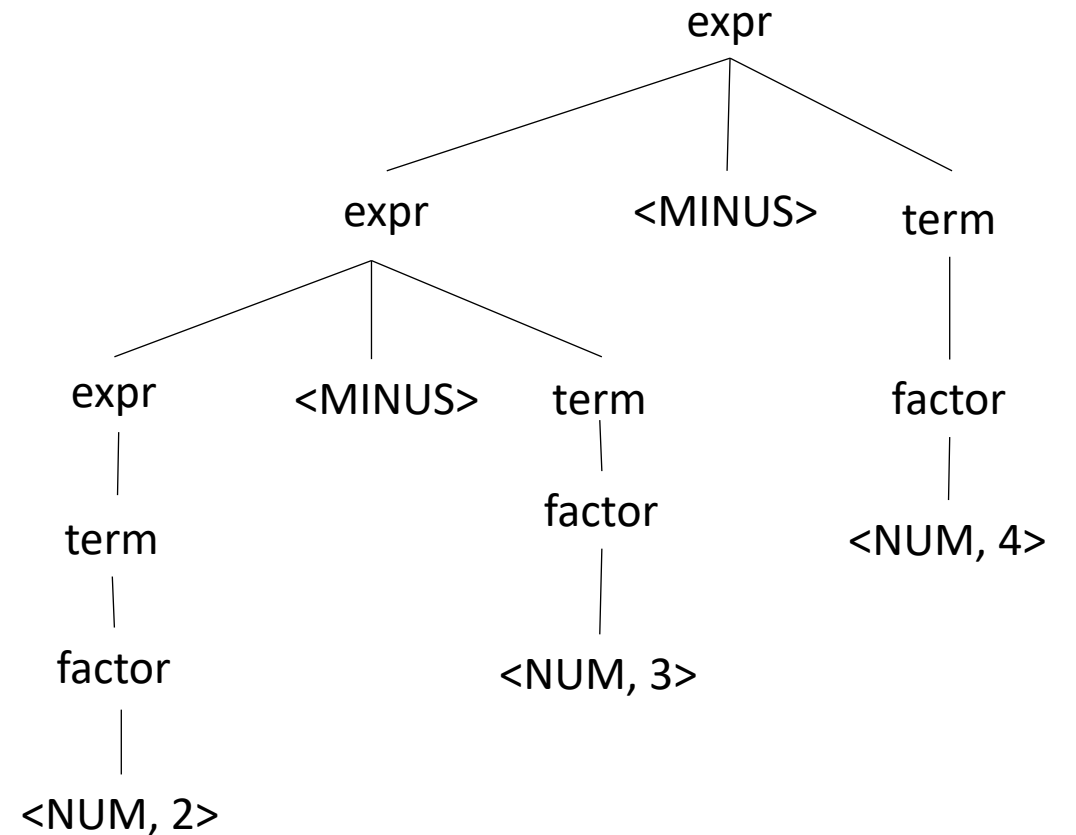
GPUs often have many IRs... why?

Abstract Syntax Trees

- Remember the expression parse tree

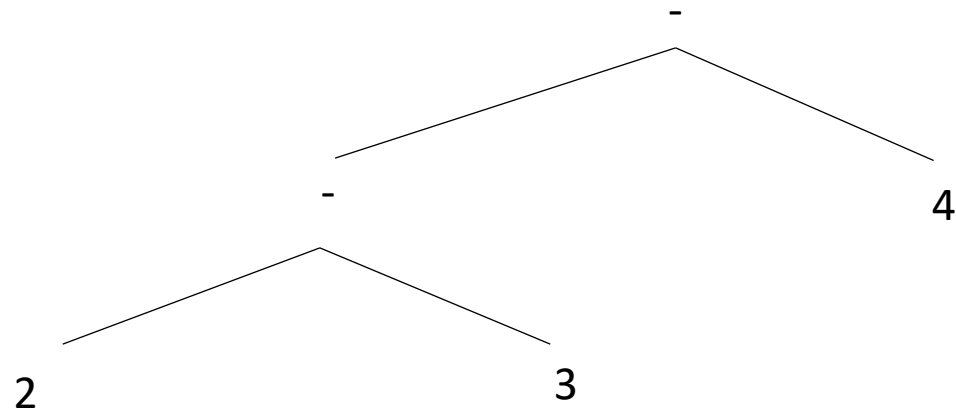
input: 2-3-4

| Operator | Name | Productions |
|----------|--------|---|
| +,- | expr | : expr PLUS term expr MINUS term term |
| *,/ | term | : term TIMES pow term DIV pow Pow |
| ^ | pow | : factor CARROT pow factor |
| () | factor | : LPAR expr RPAR NUM |



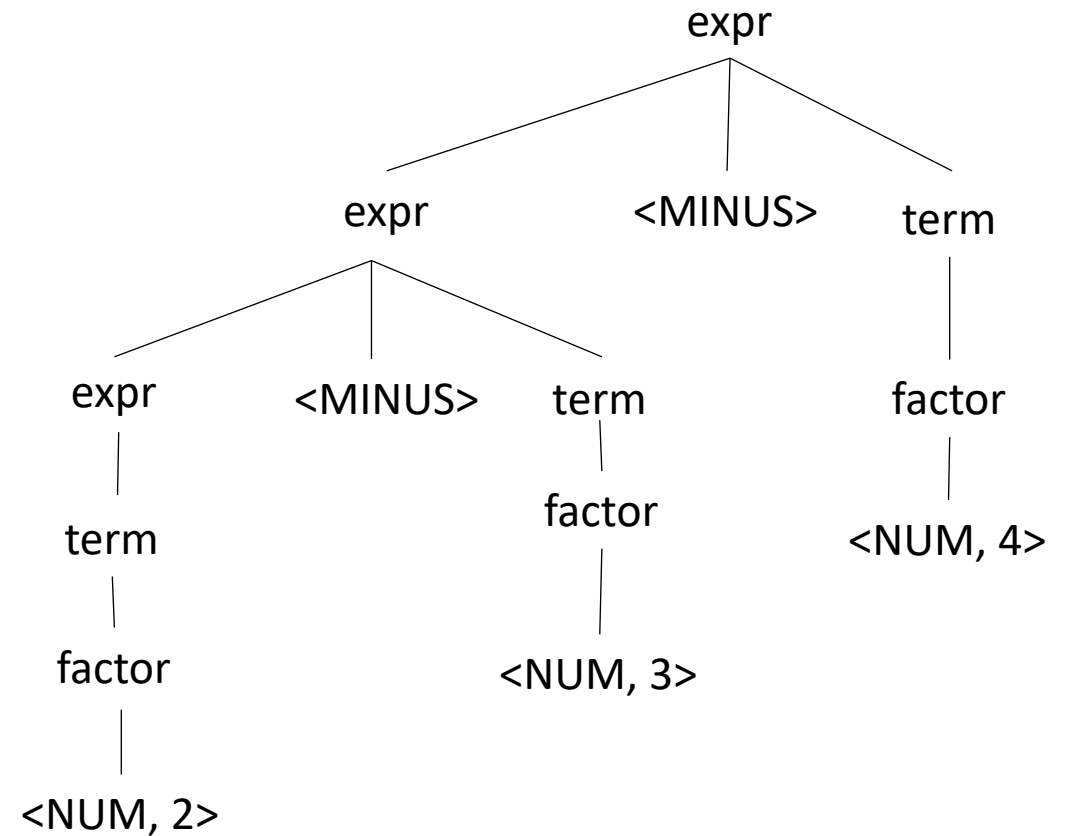
Abstract Syntax Trees

- Convert into an AST



Much more compact!

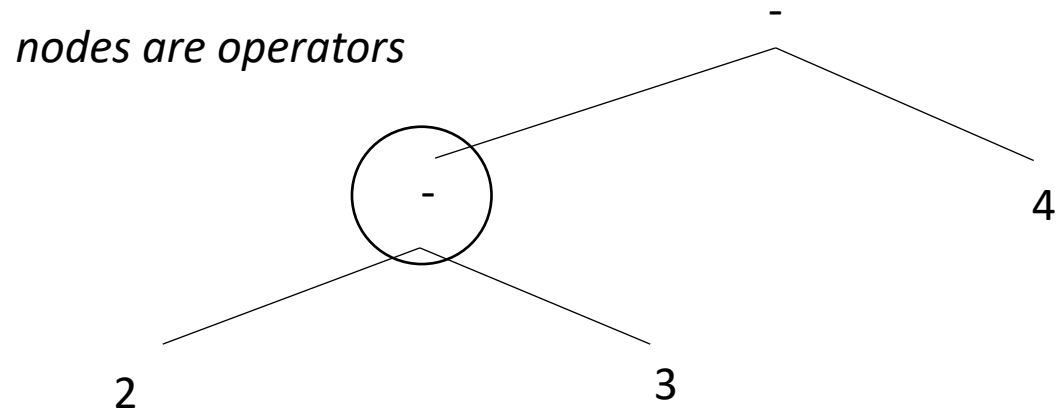
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Abstract Syntax Trees

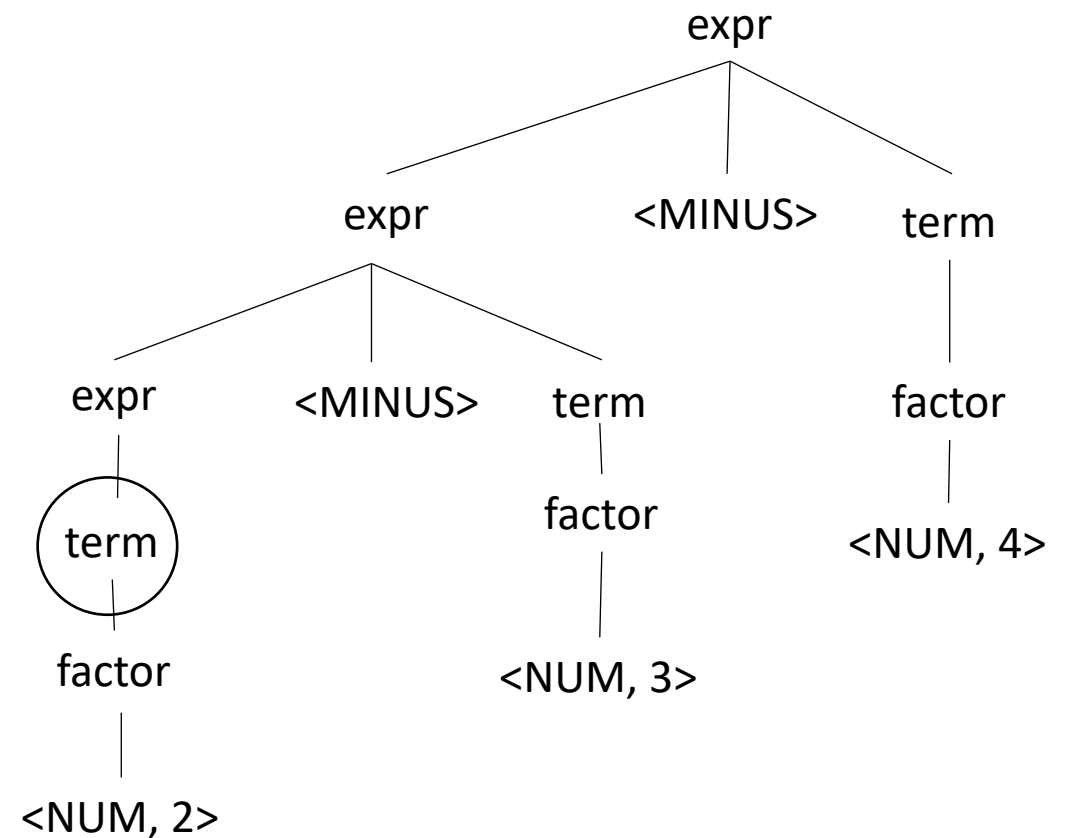
- Convert into an AST

input: 2-3-4



Much more compact!

nodes are production rules



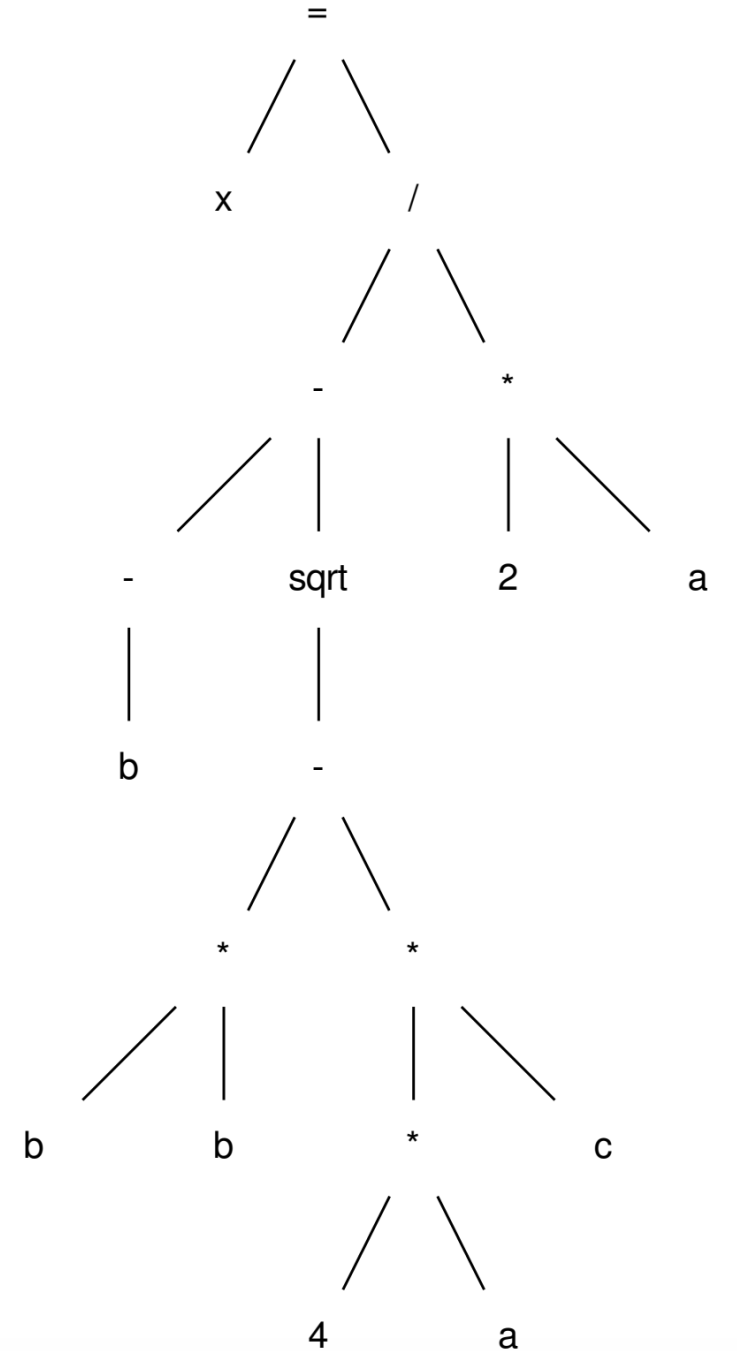
Abstract Syntax Trees

- Easier to see bigger trees, e.g. quadratic formula:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = (-b - \text{sqrt}(b*b - 4 * a * c)) / (2*a)$$

$$x = (-b - \text{sqrt}(b*b - 4 * a * c)) / (2*a)$$



3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
 - unlimited virtual registers
- represented many ways:

`rx = ry op rz;`

`r5 = r3 + r6;`

`r6 = r0 * r7;`

3 address code IR

- Each instruction consists of 3 “addresses”
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- represented many ways:

$r_x \leftarrow r_y \text{ op } r_z;$

$r_5 \leftarrow r_3 + r_6;$

$r_6 \leftarrow r_0 * r_7;$

3 address code IR

- Each instruction consists of 3 “addresses”
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- represented many ways:

```
rx = op ry, rz;
```

```
r5 = add r3, r6;
```

```
r6 = mult r0, r7;
```


3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
 - unlimited virtual registers
- some instructions don't fit the pattern:

```
store ry, rz;
```

```
r5 = copy r3;
```

```
r6 = call (r0, r1, r2, r3...);
```

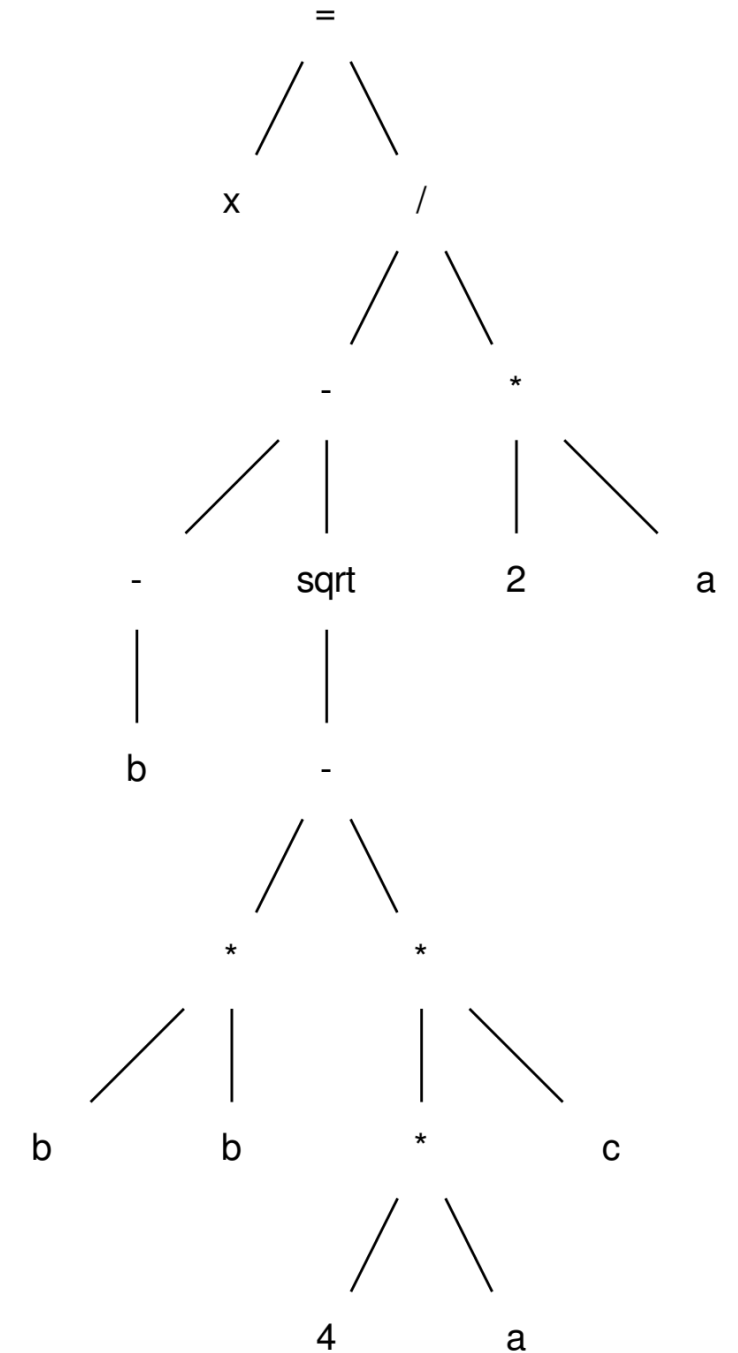
3 address code IR

- Each instruction consists of 3 “addresses”
 - Address here means a virtual register or value
 - unlimited virtual registers
- Other information:
 - Annotated
 - Typed
 - Alignment

```
r5 = r3 + r6; !dbg !22  
r6 = r0 *(int32) 67;  
store(r1, r2), aligned 8
```

Convert this code to 3 address code

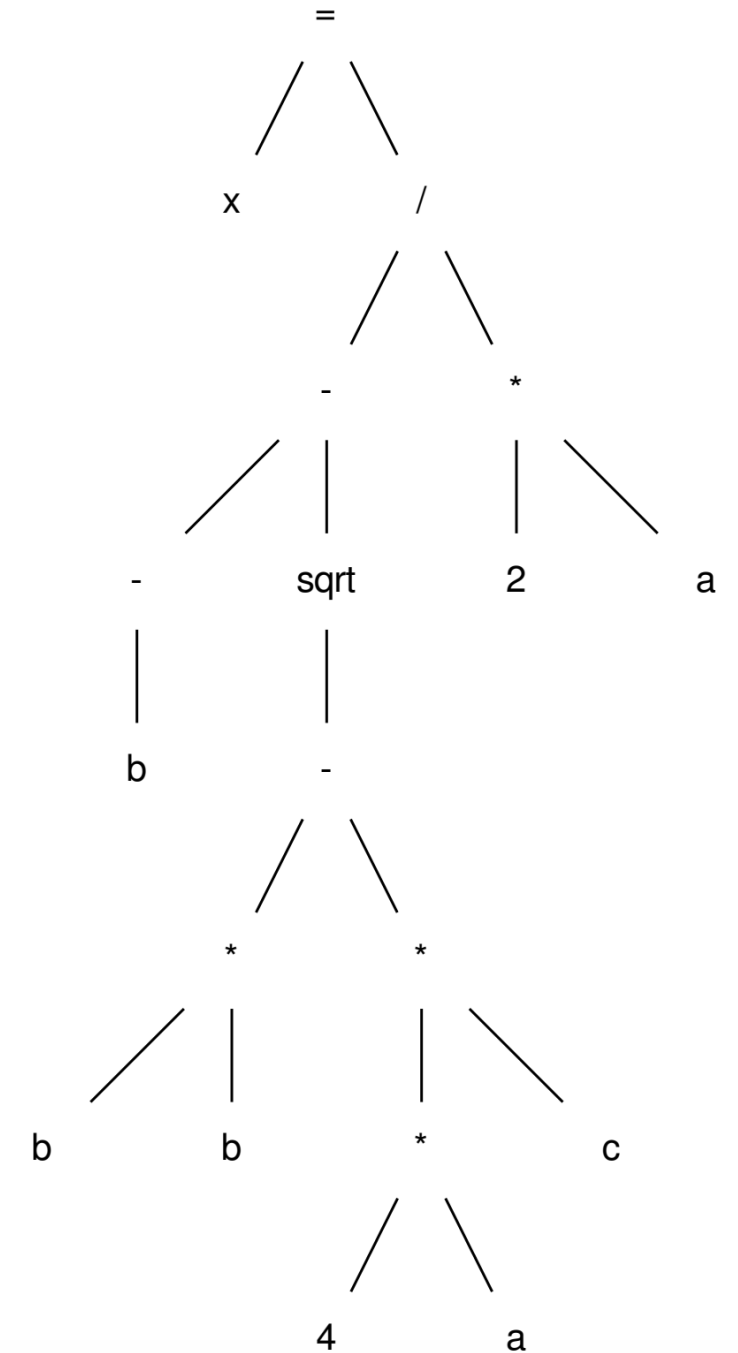
post-order traversal, creating virtual registers for each node



Convert this code to 3 address code

post-order traversal, creating virtual registers for each node

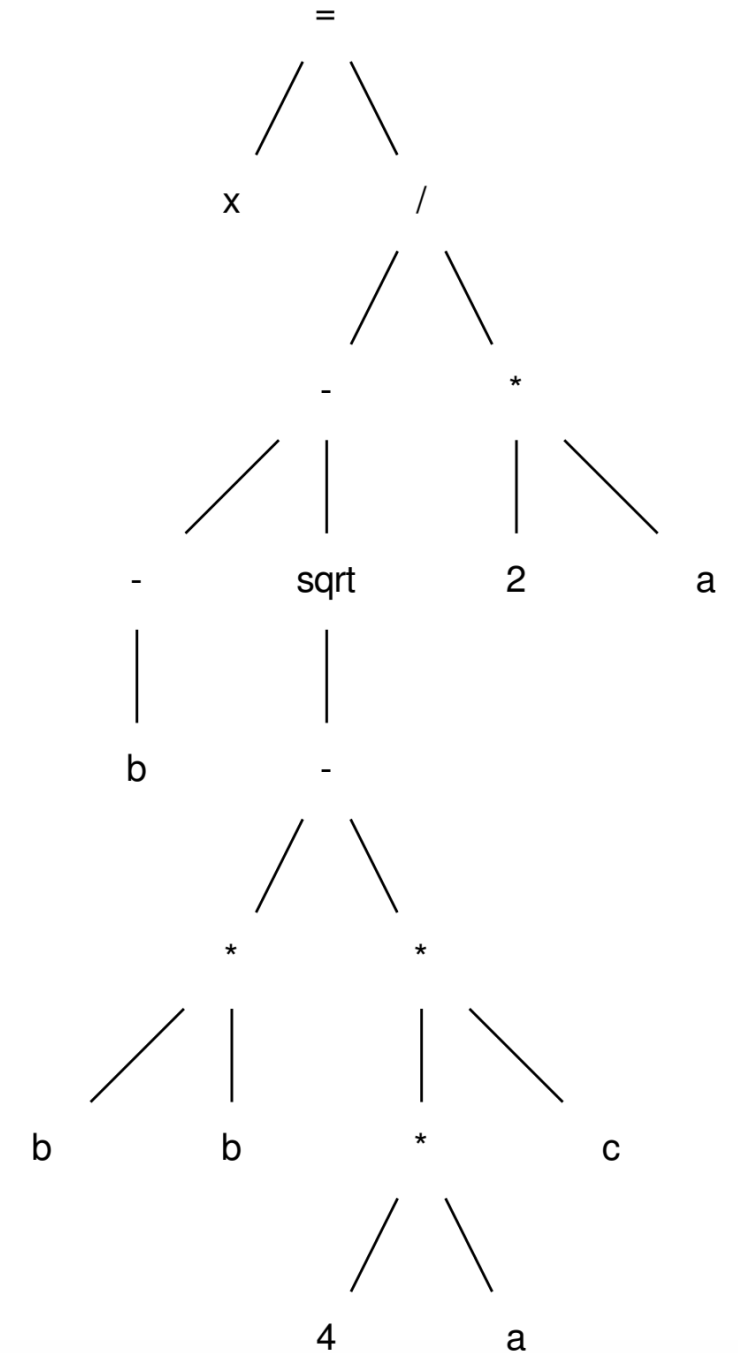
```
r0 = neg(b) ;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers for each node

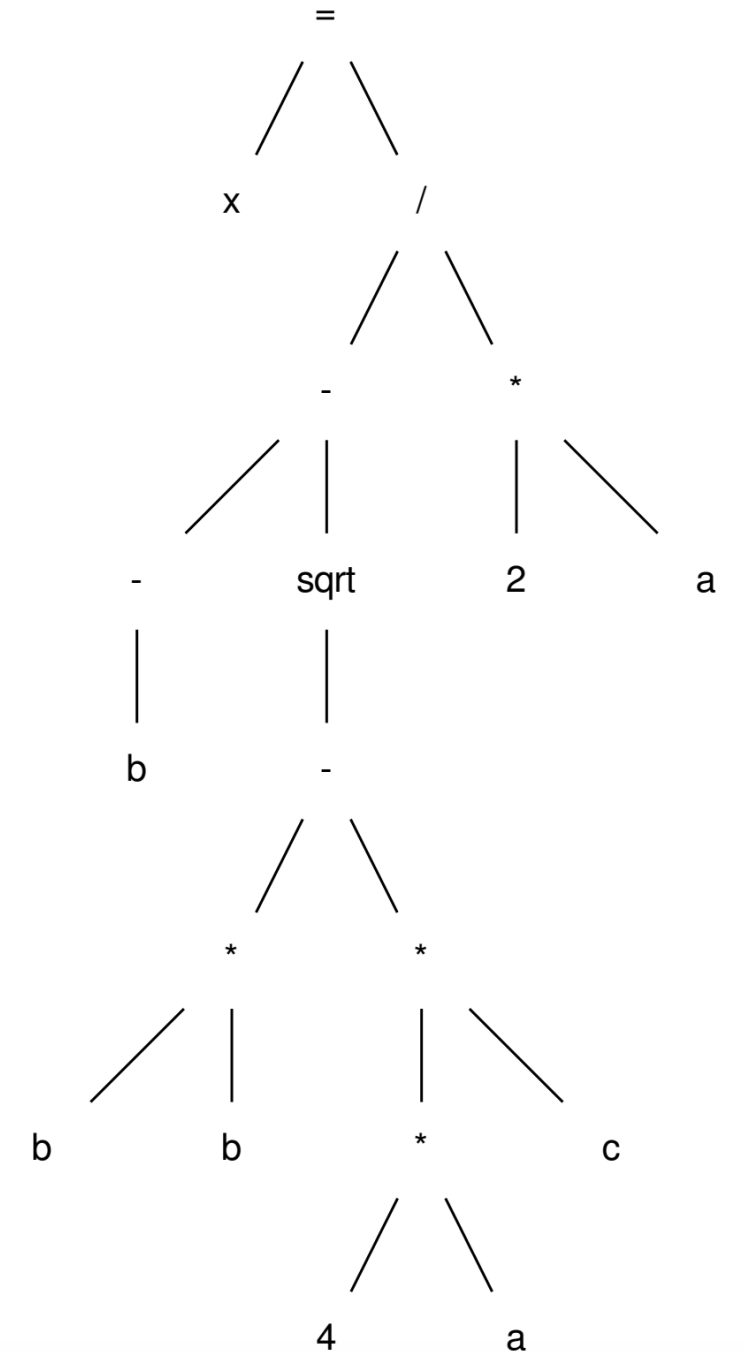
```
r0 = neg(b);  
r1 = b * b;
```



Convert this code to 3 address code

post-order traversal, creating virtual registers for each node

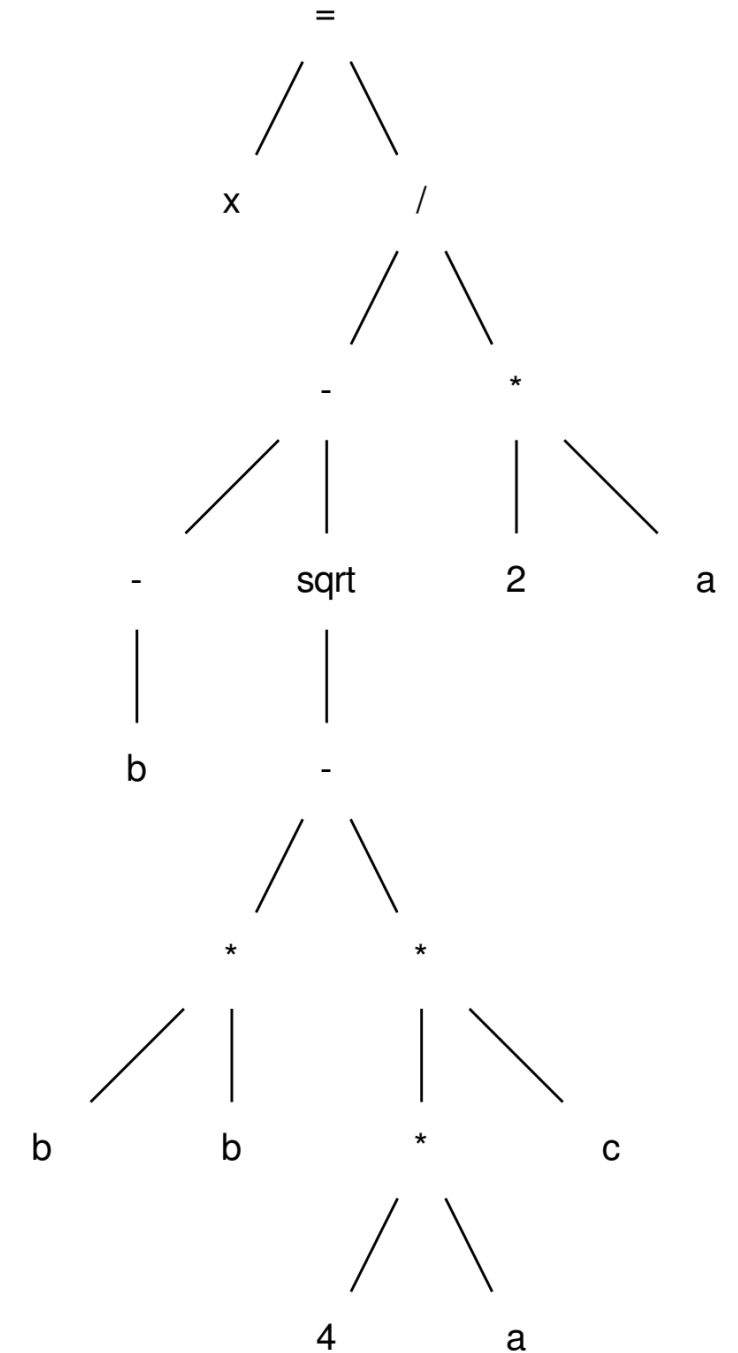
```
r0 = neg(b) ;  
r1 = b * b ;  
r2 = 4 * a ;
```



Convert this code to 3 address code

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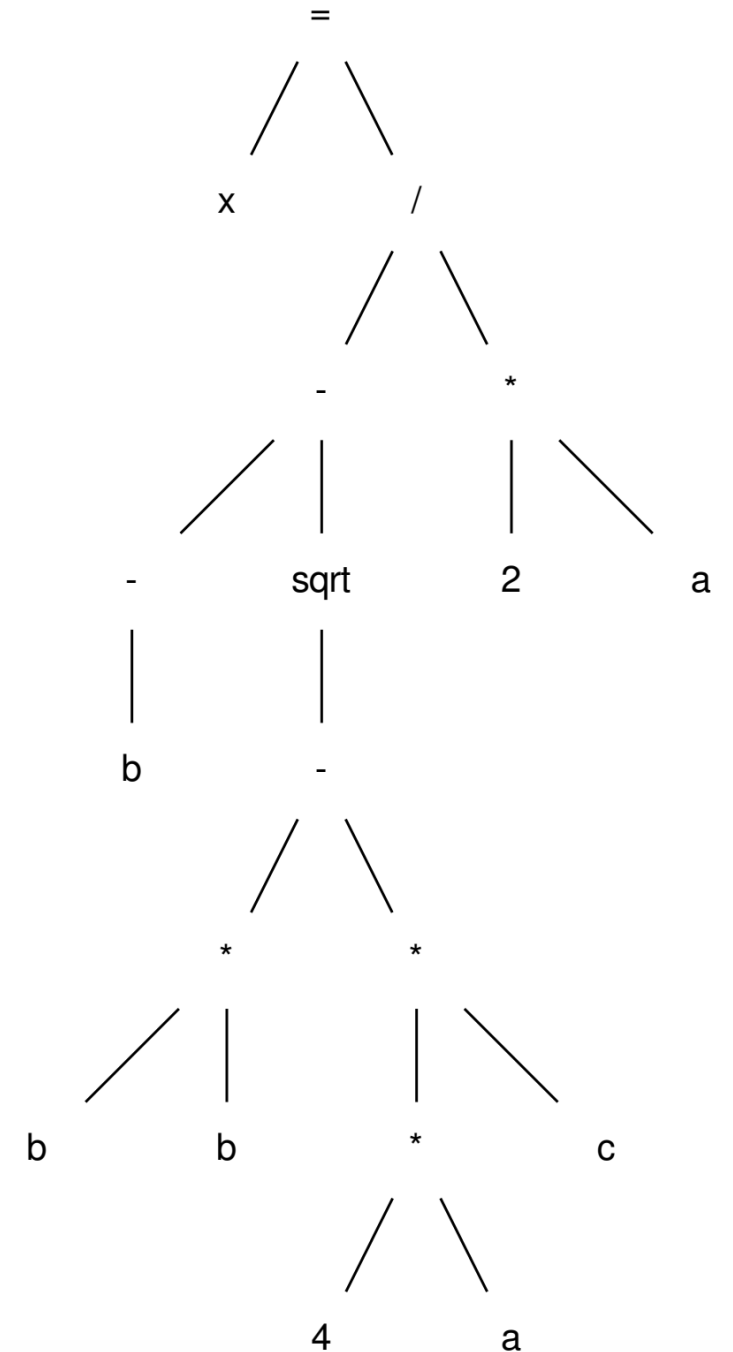
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r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;
```



Convert this code to 3 address code

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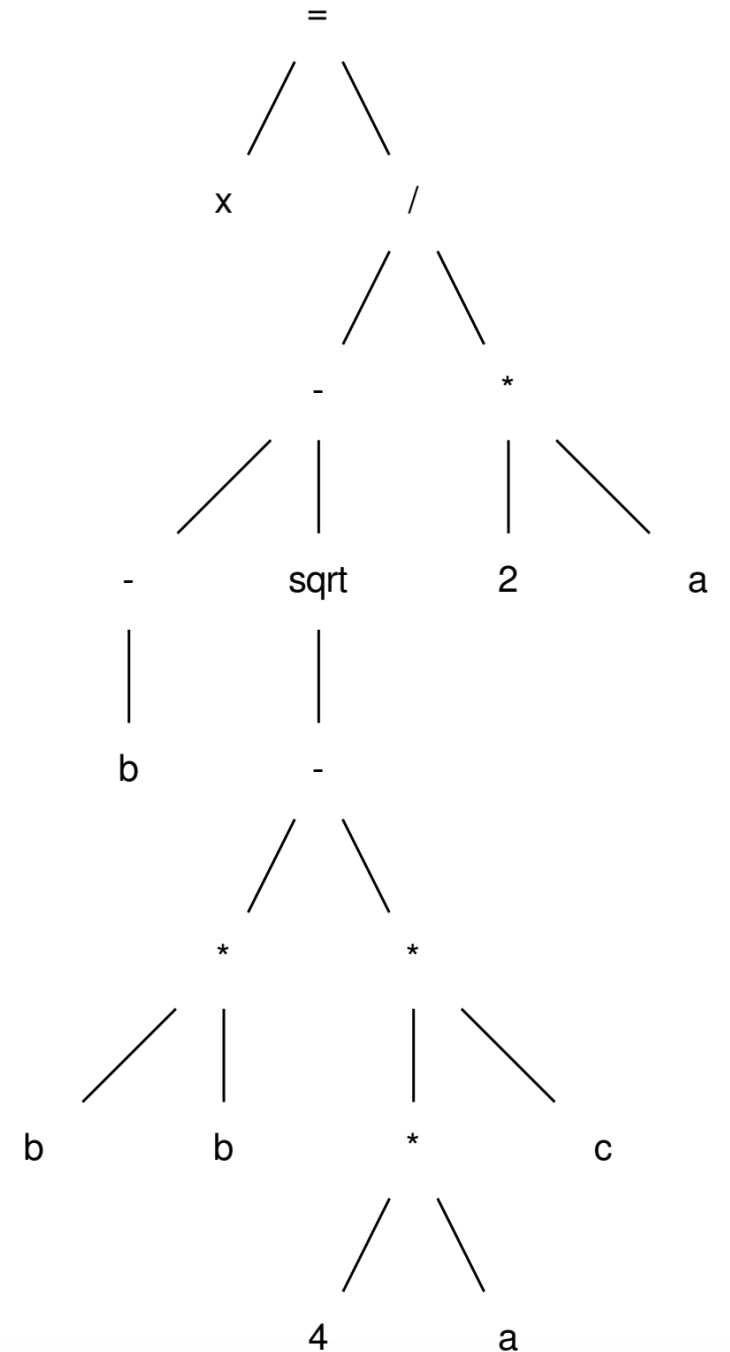
```
r0 = neg(b);  
r1 = b * b;  
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r4 = r1 - r3;
```



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post-order traversal, creating virtual registers for each node

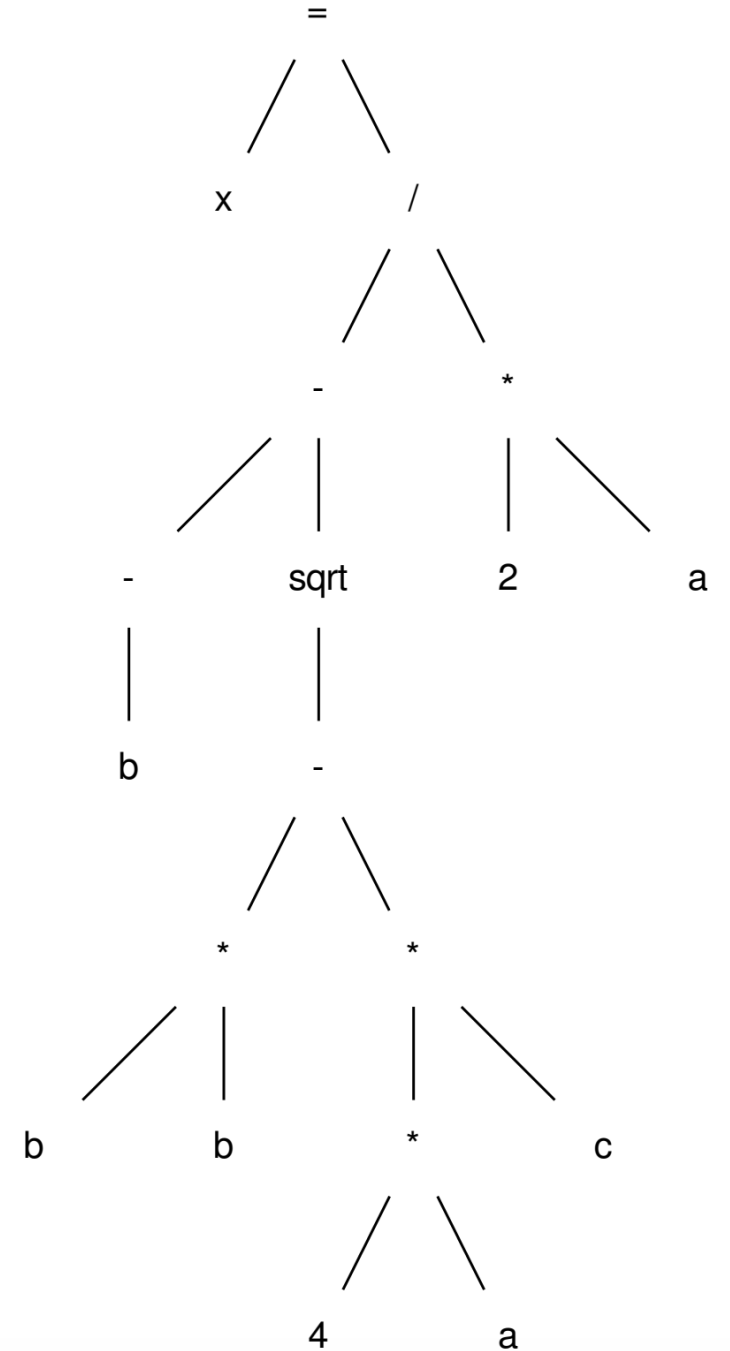
```
r0 = neg(b);  
r1 = b * b;  
r2 = 4 * a;  
r3 = r2 * c;  
r4 = r1 - r3;  
r5 = sqrt(r4);
```



Convert this code to 3 address code

post-order traversal, creating virtual registers for each node

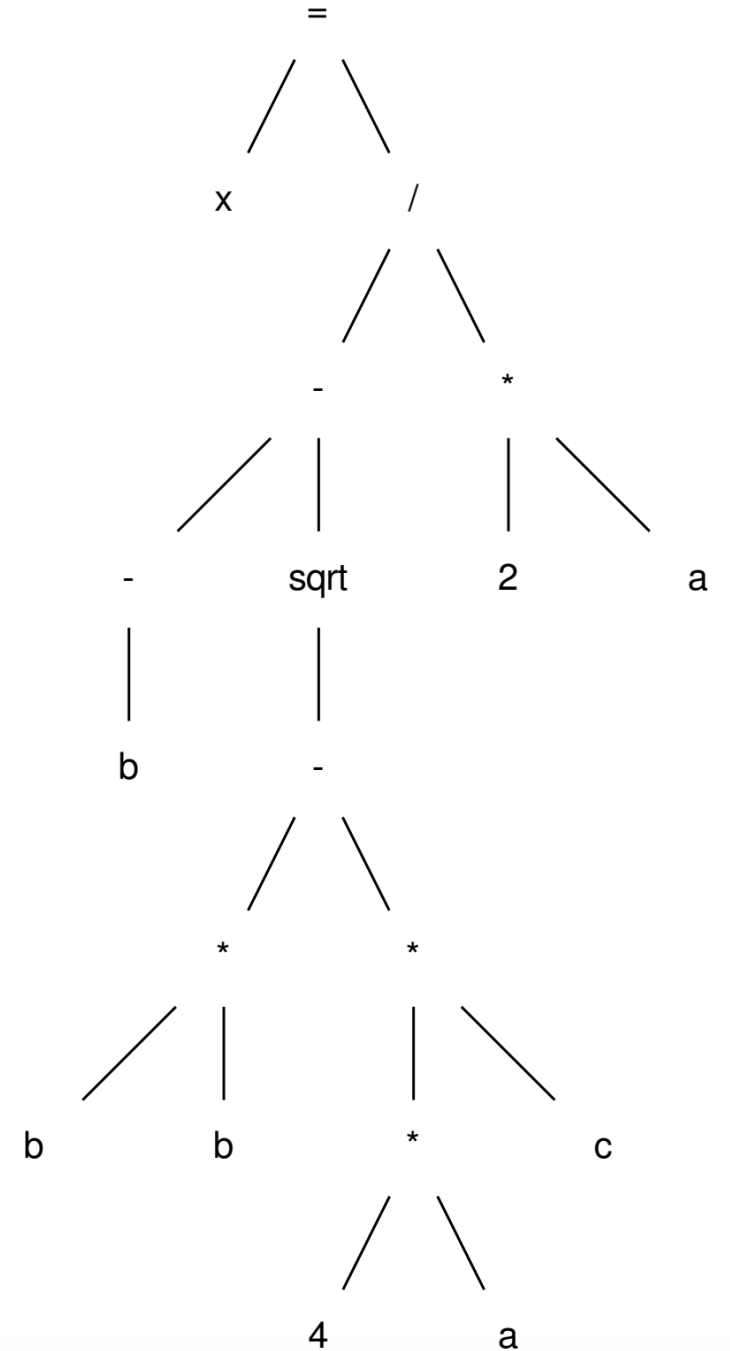
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Convert this code to 3 address code

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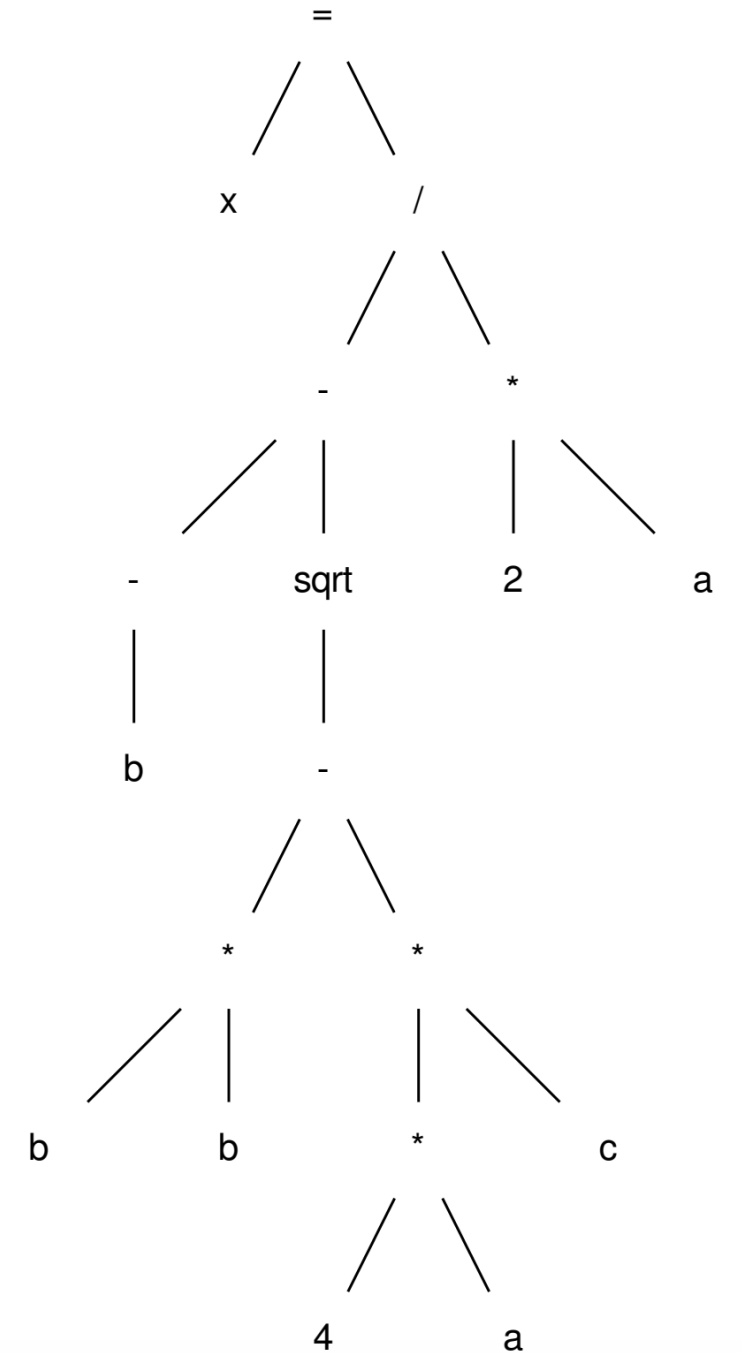
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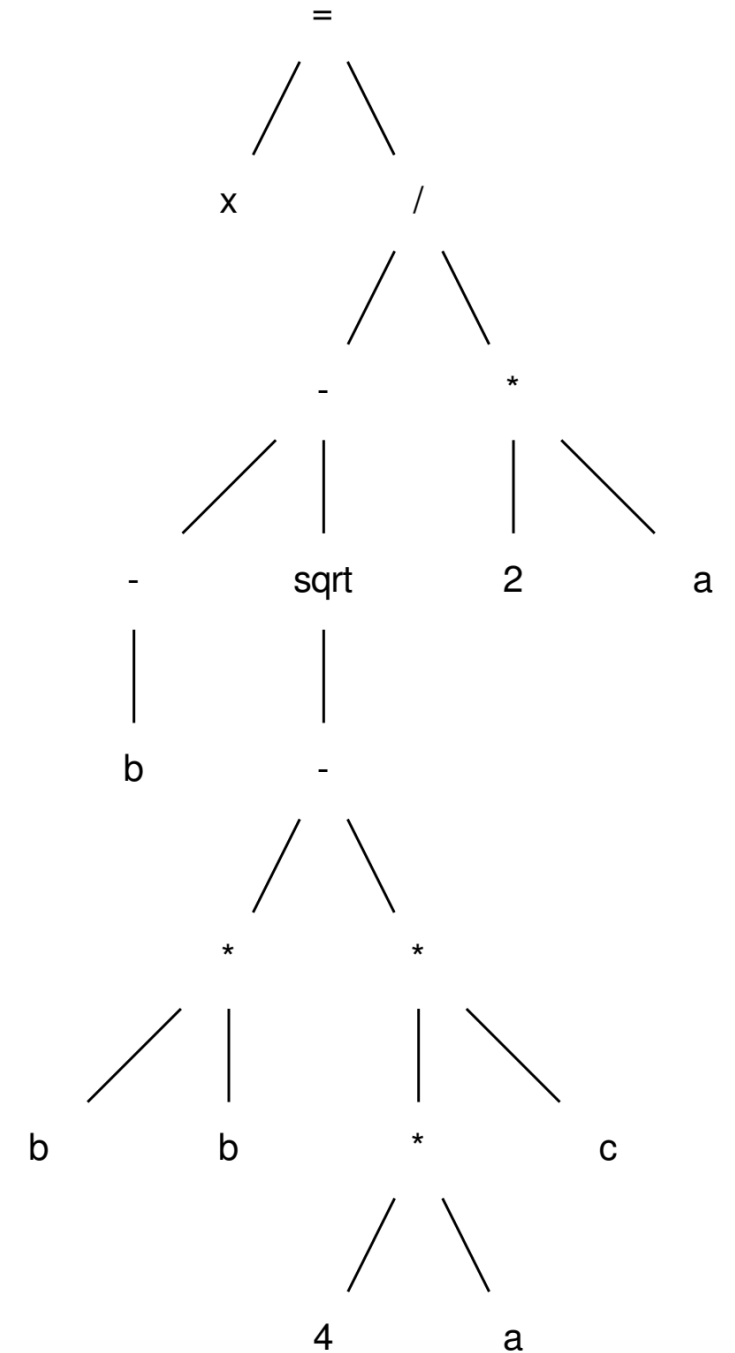
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r8 = r6 / r7 ;  
x = r8 ;
```



What now?

We can more easily compile to machine code
OR

```
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r1 = b * b ;  
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r3 = r2 * c ;  
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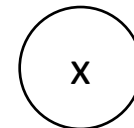
What now?

We can perform more optimizations, example:
by making a data-dependency graph (DDG)

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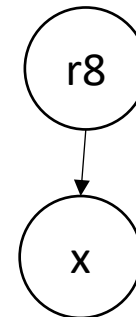

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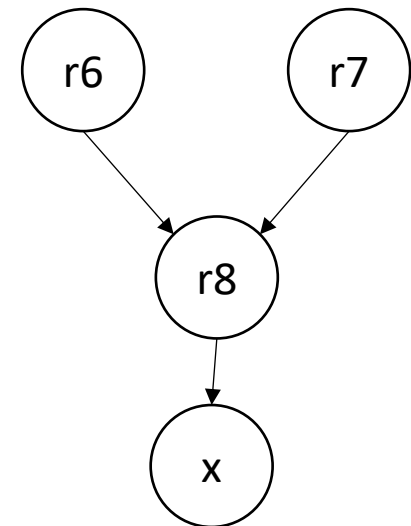
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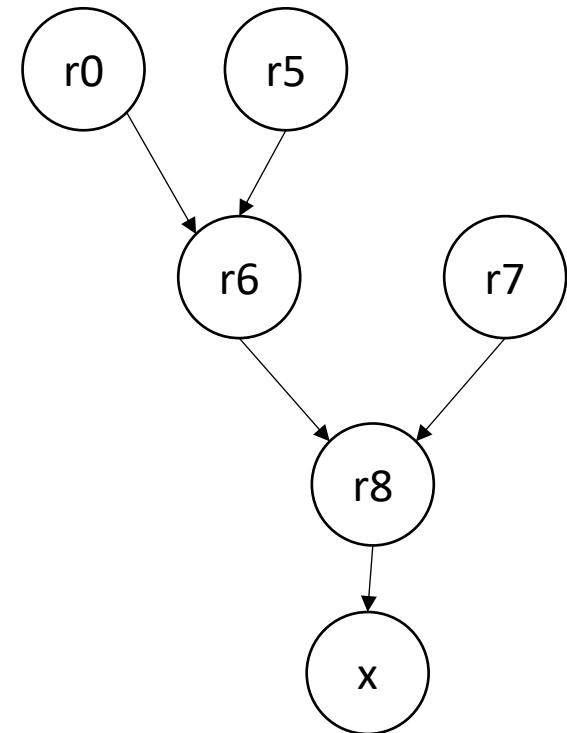
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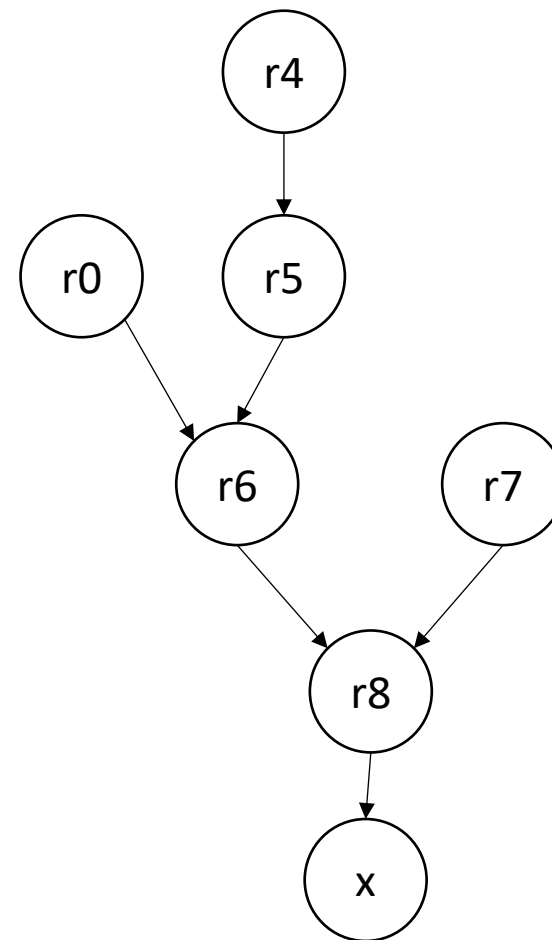
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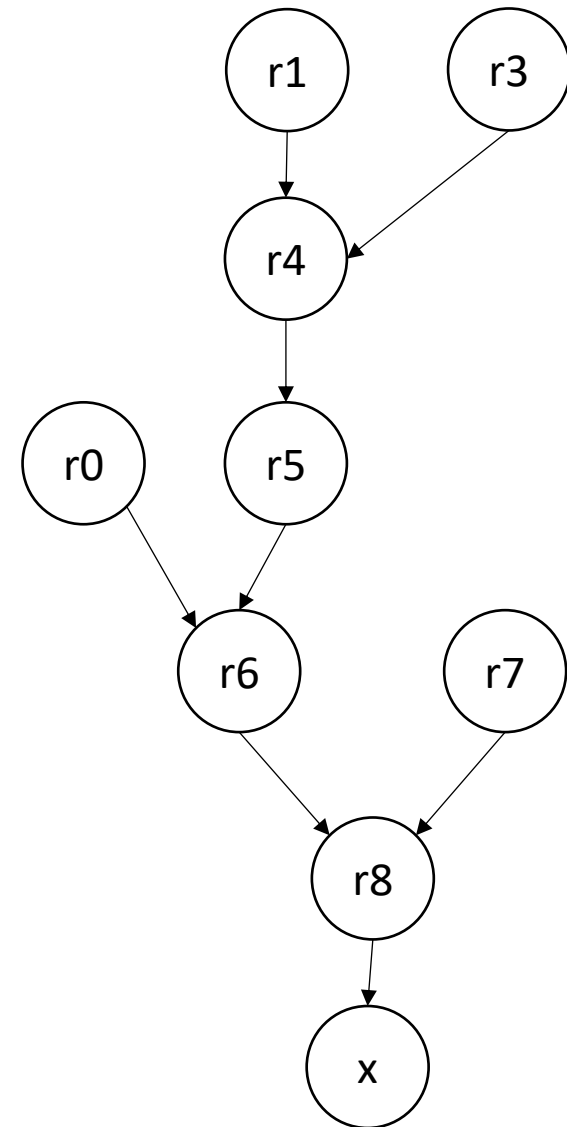
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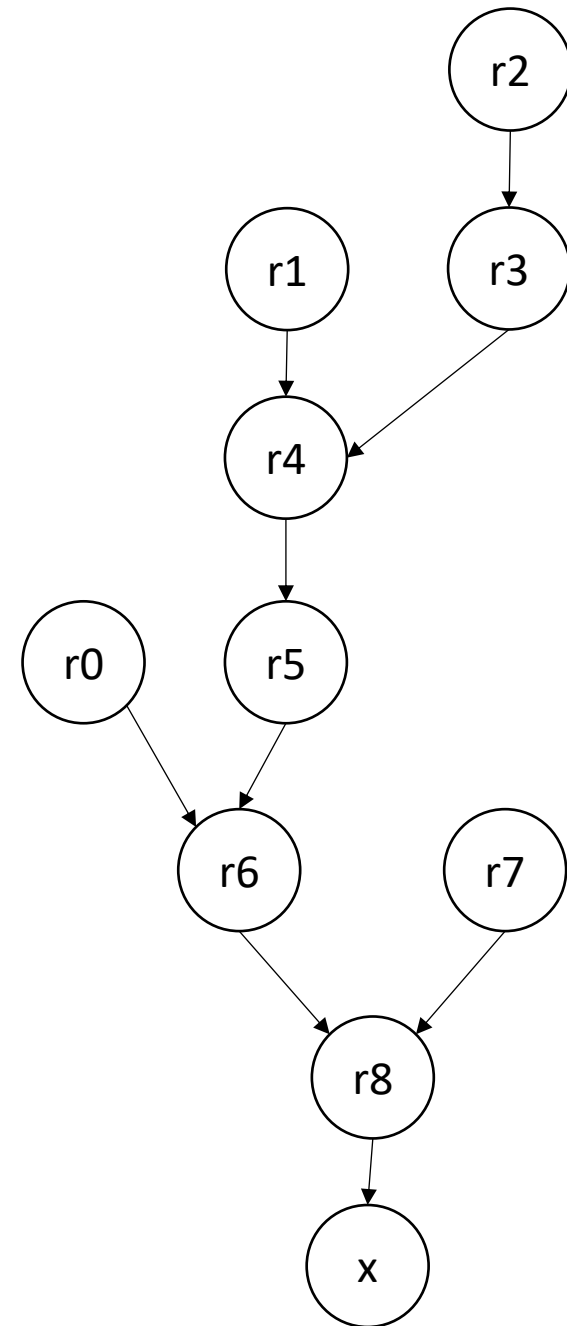
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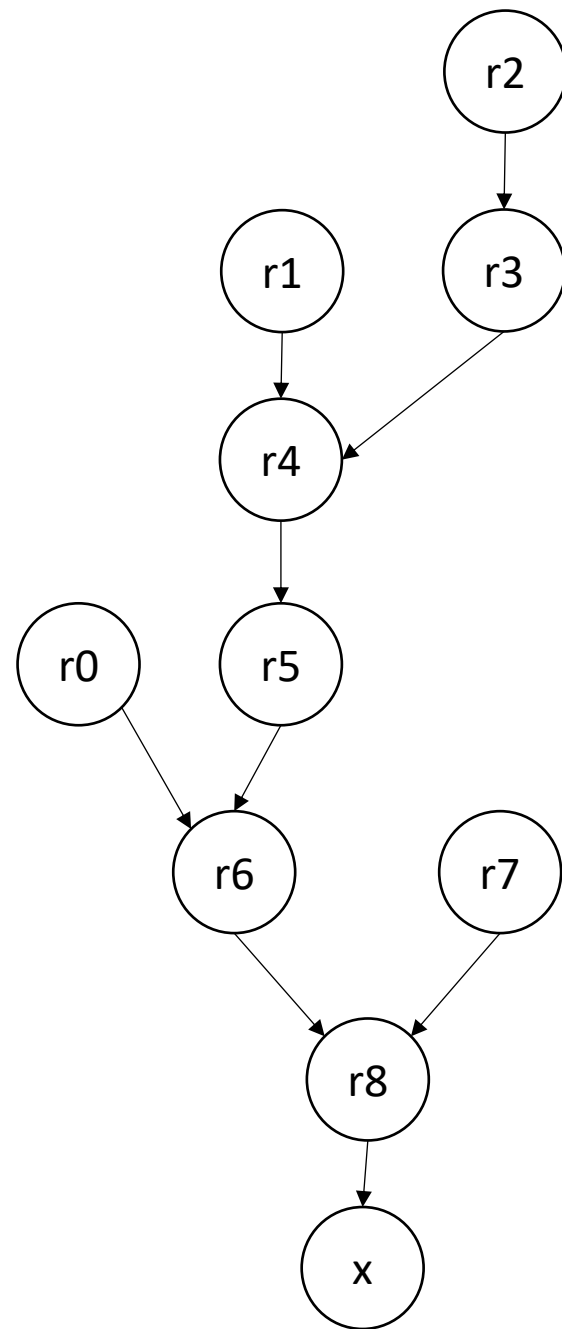
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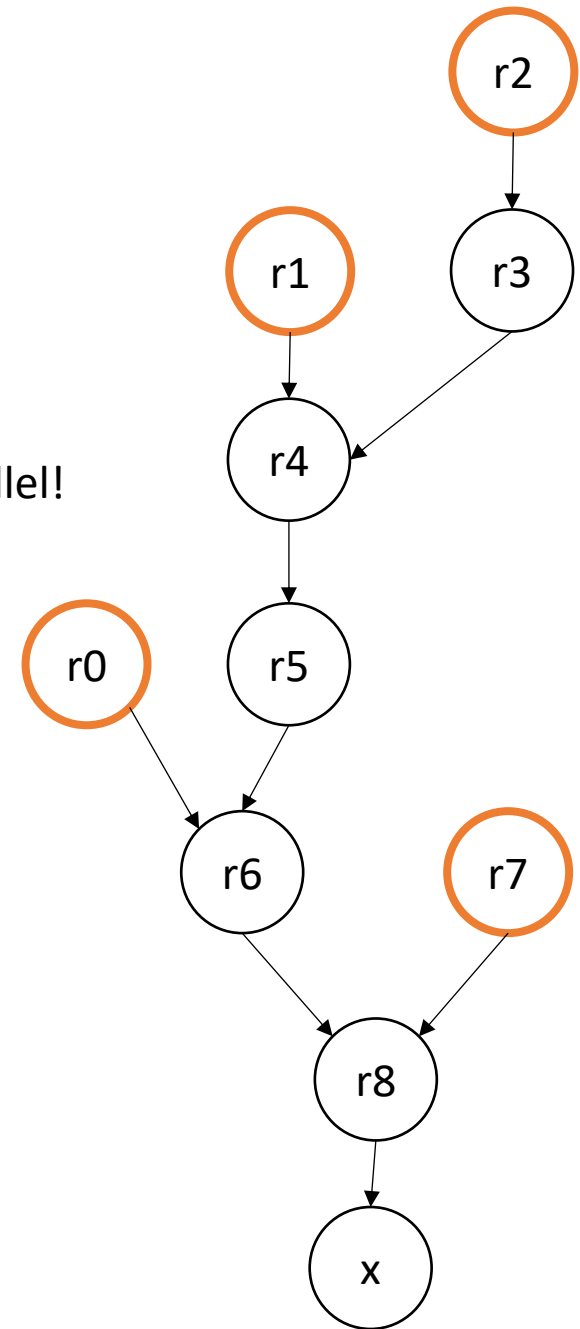
What can this tell us?



We can perform more optimizations, example:
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```

can be done in parallel!

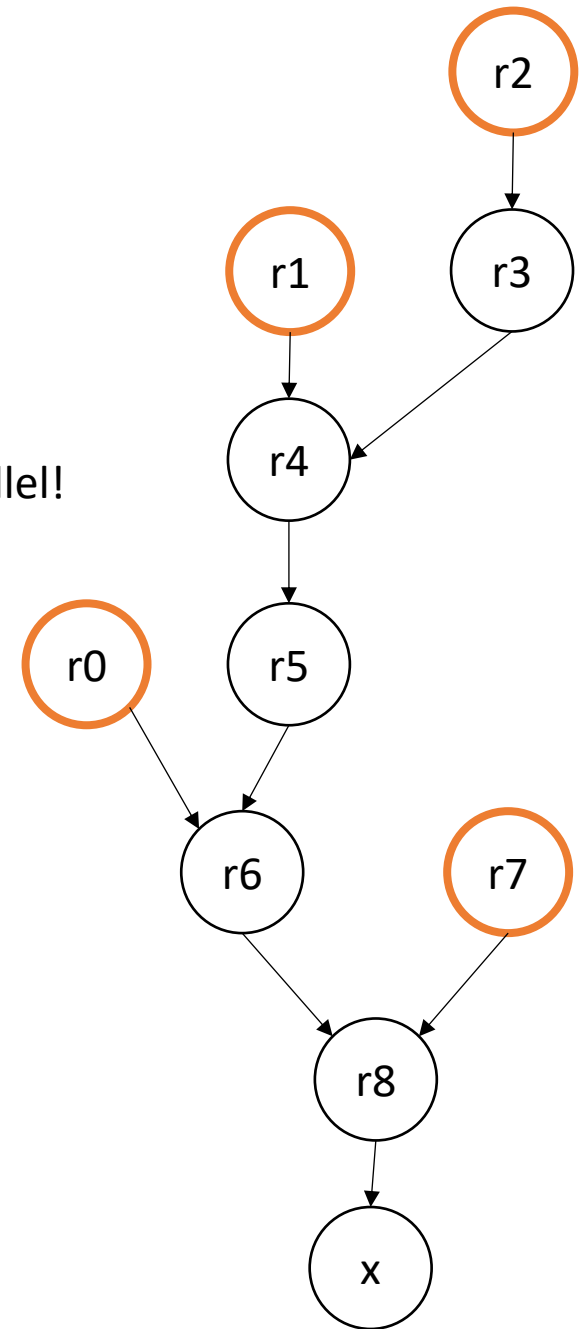


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```

Can be hoisted!

can be done in parallel!



We can perform more optimizations, example:
by making a data-dependency graph (DDG)

```
r0 = neg (b) ;
```

```
r1 = b * b ;
```

```
r2 = 4 * a ;
```

```
r3 = r2 * c ;
```

```
r4 = r1 - r3 ;
```

```
r5 = sqrt (r4) ;
```

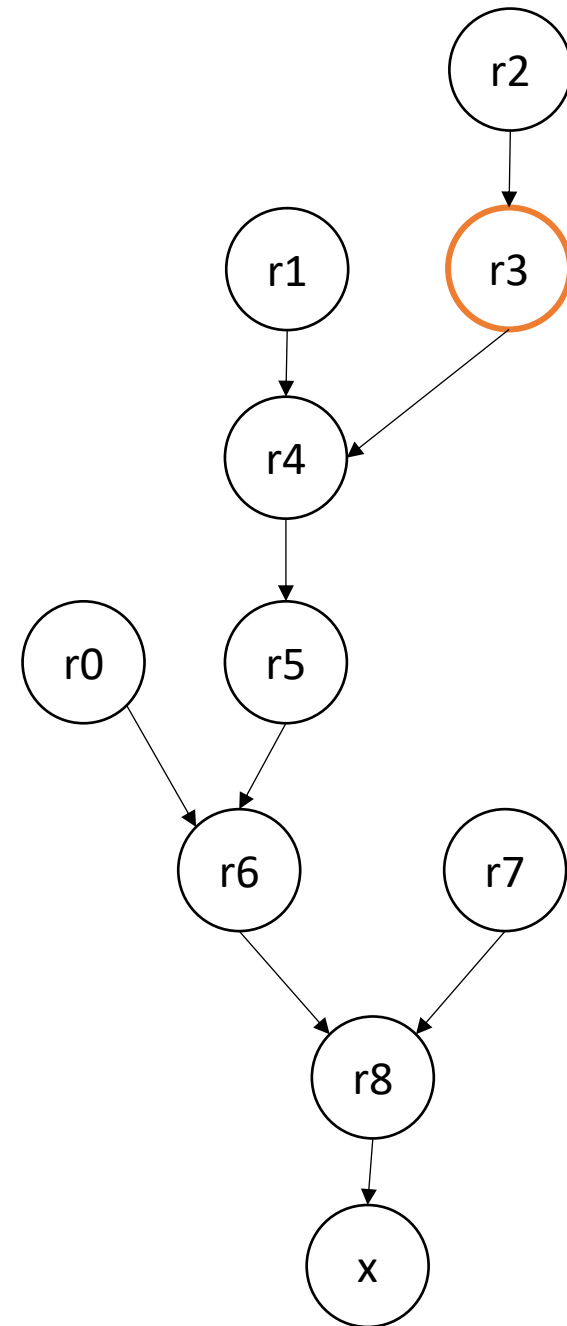
```
r6 = r0 - r5 ;
```

```
r7 = 2 * a ;
```

```
r8 = r6 / r7 ;
```

```
x = r8 ;
```

should we hoist this one?



Lots of considerations in optimizing

- More on instruction scheduling later
 - Processor agnostic?
- Back to 3-address code
- We looked at expressions, but how about conditionals?

What about control flow?

- 3 address code typically contains a conditional branch:

```
br <reg>, <label0>, <label1>
```

if the value in <reg> is true, branch to <label0>, else branch to <label1>

```
br <label0>
```

unconditional branch

What about control flow?

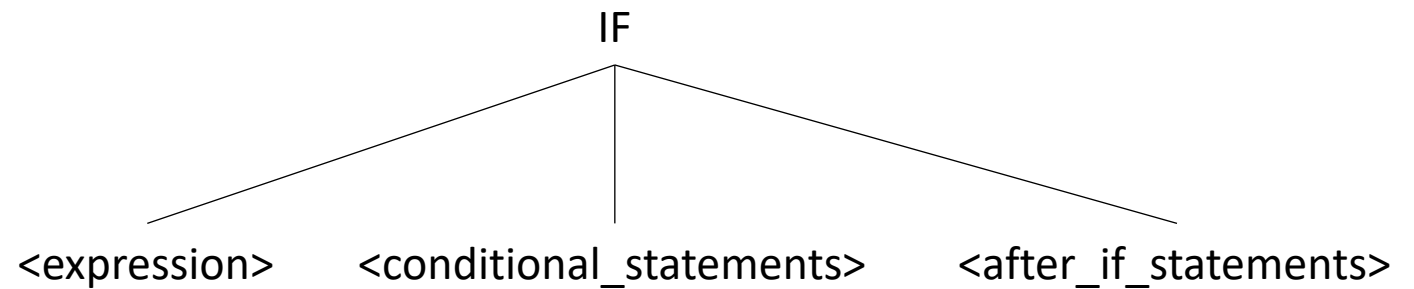
```
if (expr) {  
  // conditional statements  
}  
// after if statements
```

First, produce an AST

What about control flow?

```
if (expr) {  
  // conditional statements  
}  
// after if statements
```

Next lower to 3 address code



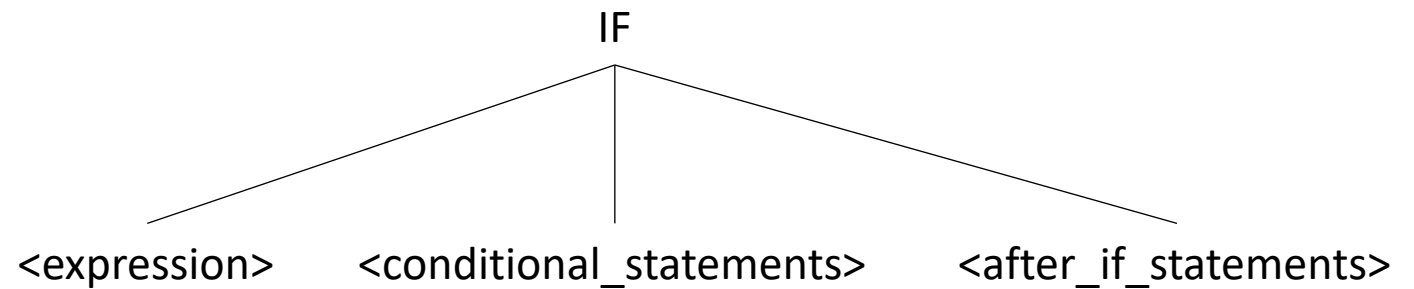
What about control flow?

```
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    // conditional statements  
}  
// after if statements
```

```
r0 = <expression>;  
br r0, conditional_stmts, after_if;
```

```
conditional_stmts:  
<conditional_statements>;
```

```
after_if:  
<after_if_statements>;
```



What about control flow?

```
while (expr) {  
    // inside_loop_statements  
}  
// after_loop_statements
```

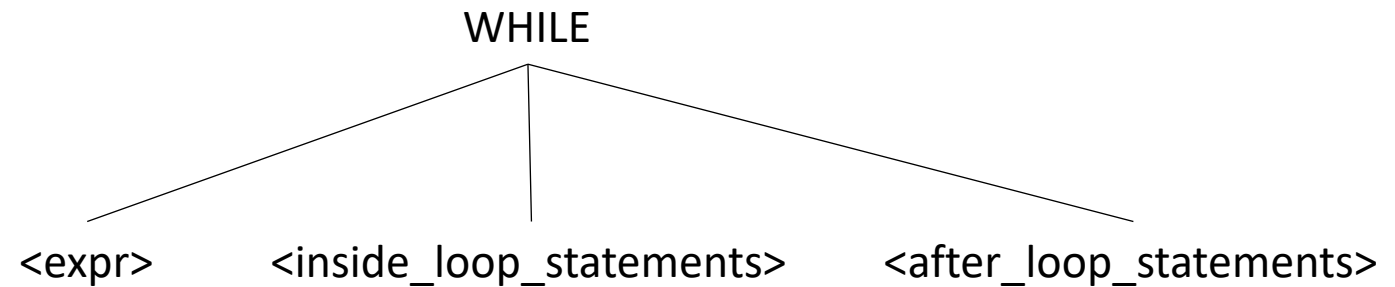
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// after_loop_statements
```



What about control flow?

```
while (expr) {  
    // inside_loop_statements  
}  
// after_loop_statements
```

```
beginning_label:
```

```
r0 = <expr>
```

```
br r0, inside_loop, after_loop;
```

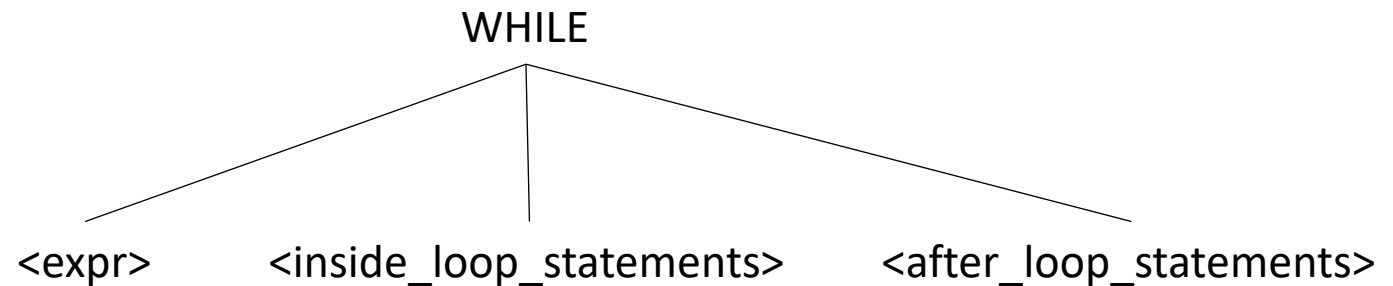
```
inside_loop:
```

```
<inside_loop_statements>
```

```
br beginning_label;
```

```
after_loop:
```

```
<after_loop_statements>
```

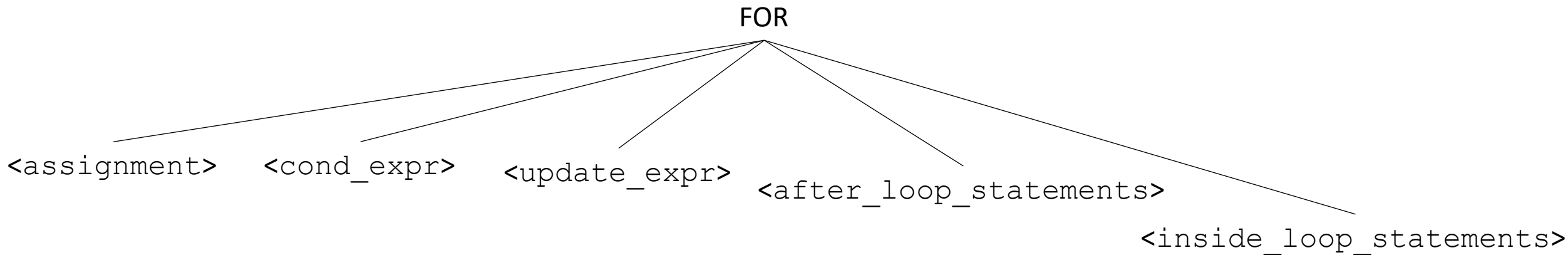


For loop

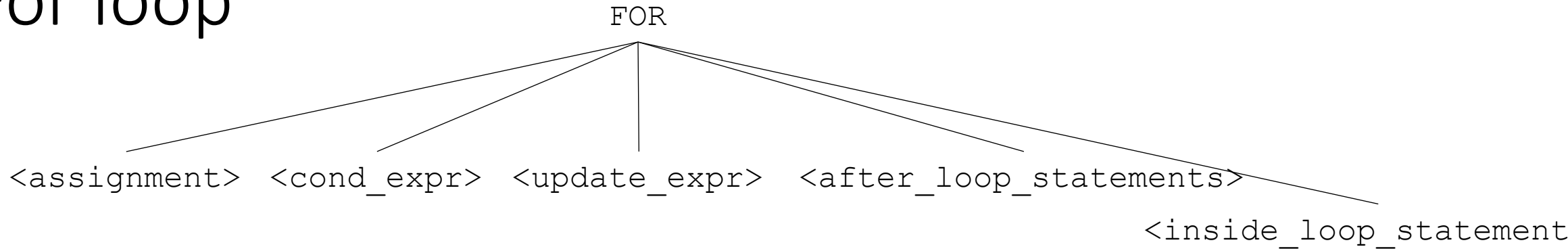
```
for (assignment; cond_expr; update_expr) {  
    // inside_loop_statements  
}  
// after_loop_statements
```

For loop

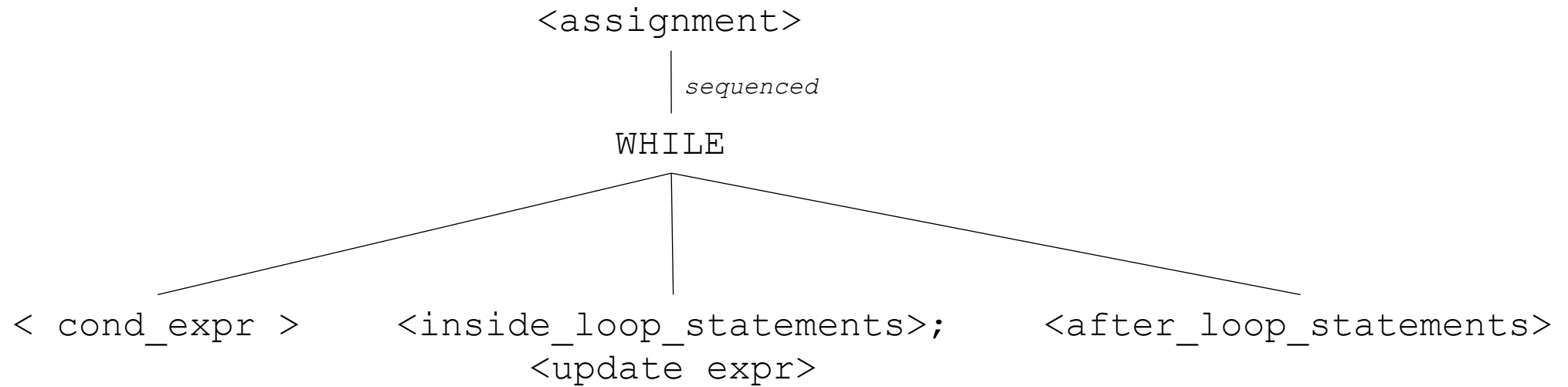
```
for (assignment; cond_expr; update_expr) {  
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}  
// after_loop_statements
```



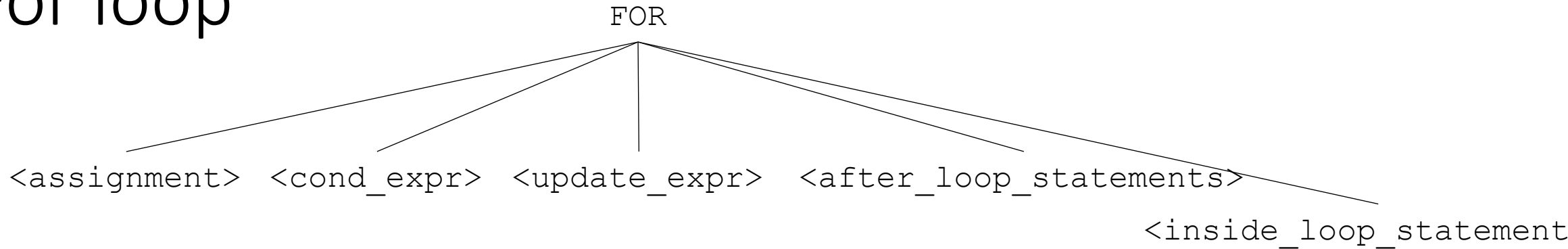
For loop



Can be de-sugared into a while loop:

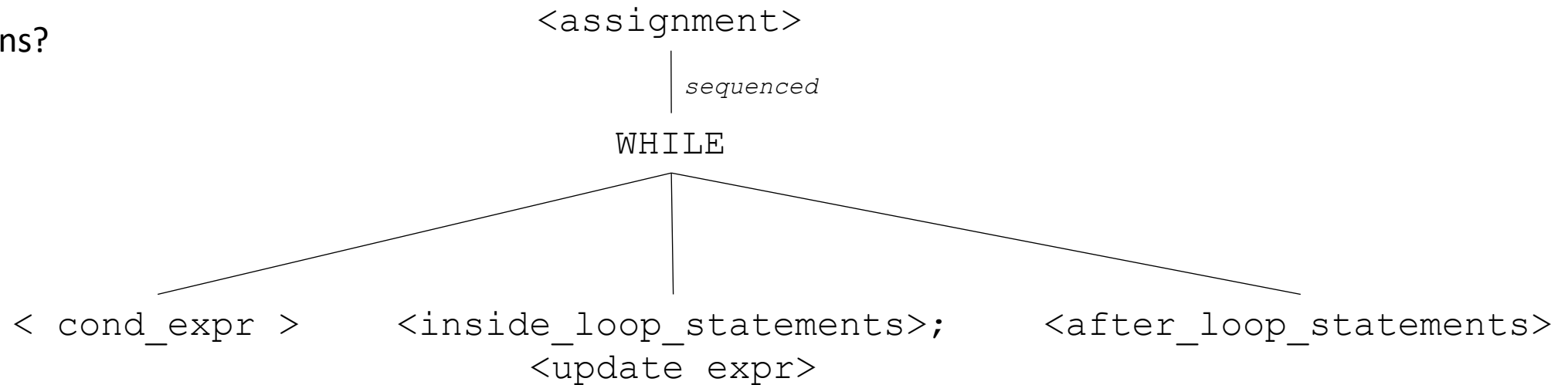


For loop



Can be de-sugared into a while loop:

Pros? Cons?



IR Program structure

- A sequence of 3 address instructions
- Programs can be split into **Basic Blocks**:
 - A sequence of 3 address instructions such that:
 - There is a single entry, single exit
- *Important property*: an instruction in a basic block can assume that all preceding instructions will execute

Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

IR Program structure

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Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

Two Basic Blocks

```
Label_x:  
op1;  
op2;  
op3;  
  
Label_y:  
op4;  
op5;
```

How might they appear in a high-level language? What are some examples?

IR Program structure

- A sequence of 3 address instructions
- Programs can be split into **Basic Blocks**:
 - A sequence of 3 address instructions such that:
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IR Program structure

- A sequence of 3 address instructions
- Programs can be split into **Basic Blocks**:
 - A sequence of 3 address instructions such that:
 - There is a single entry, single exit
- *Important property*: an instruction in a basic block can assume that all preceding instructions will execute

How might they appear in a high-level language?

Four Basic Blocks

```
...  
if (x) {  
    ...  
}  
else {  
    ...  
}  
...
```

Two Basic Blocks

Single Basic Block

```
Label_x:  
op1;  
op2;  
op3;  
br label_z;
```

```
Label_x:  
op1;  
op2;  
op3;  
  
Label_y:  
op4;  
op5;
```

Optimization levels

- **Local optimizations:**
 - Optimizes an individual basic block
- **Regional optimizations:**
 - Combines several basic blocks
- **Global optimizations:**
 - operates across an entire procedure
 - what about across procedures?

Optimization levels

```
Label_0:  
x = a + b;  
y = a + b;
```

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Optimization levels

- **Local optimizations:**

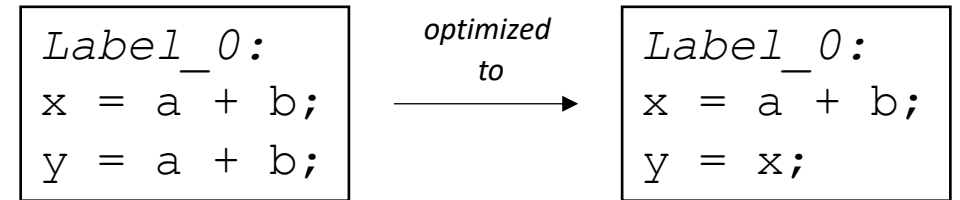
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Optimization levels

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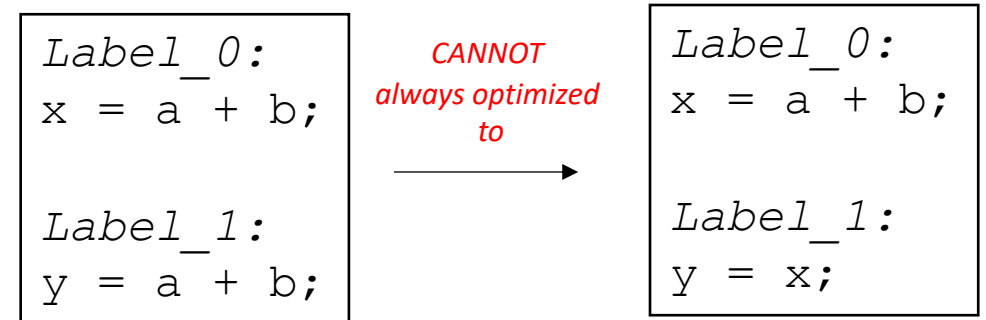
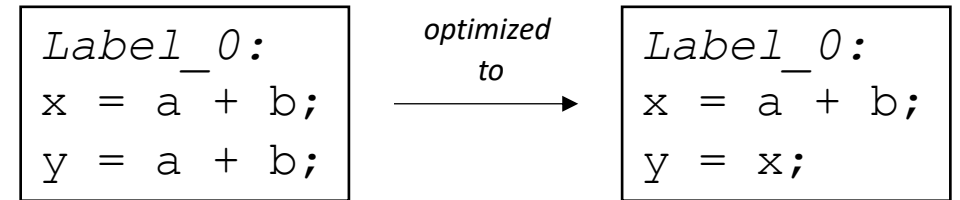
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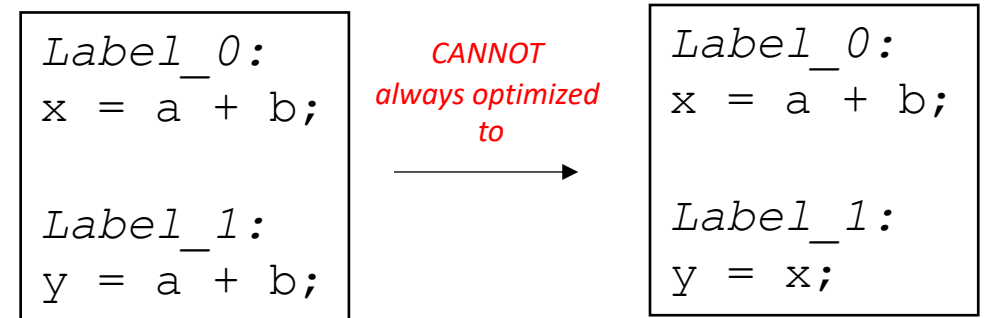
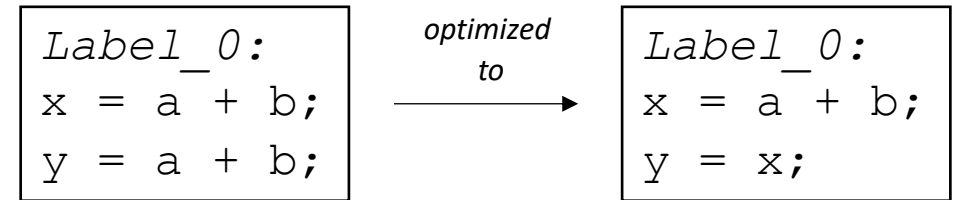
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- Combines several basic blocks

- **Global optimizations:**

- operates across an entire procedure
- what about across procedures?



*code could skip Label_0,
leaving x undefined!*

```
br Label_1;
```

```
Label_0:  
x = a + b;
```

```
Label_1:  
y = a + b;
```

Regional Optimization

```
...  
if (x) {  
    ...  
}  
else {  
    x = a + b;  
}  
y = a + b;  
...
```

*at a higher-level,
we cannot replace:
y = a + b.
with
y = x;*

Regional Optimization

```
...  
if (x) {  
    ...  
}  
else {  
    x = a + b;  
}  
y = a + b;  
...
```

*at a higher-level,
we cannot replace:
y = a + b.
with
y = x;*

```
x = a + b;  
if (x) {  
    ...  
}  
else {  
    ...  
}  
y = a + b;  
...
```

*But if a and b are
not redefined, then
y = a + b;
can be replaced with
y = x;*

Next Class

- A basic-block local optimization
 - local value numbering
- Friday: Control flow graphs and intra-block analysis