# High-performance Graph Processing on GPUs

Original slides by: Sreepathi Pai University of Rochester, October 12, 2018

Adapted by Tyler Sorensen for CSE211 at UCSC Nov. 15, 2022

Sreepathi Pai acks: Keshav Pingali, Alastair Donaldson, Muhammad Amber Hassaan, Tal Ben-Nun, Michael Sutton, Chad Voegele, Yi-Shan Lu, Ahmet Celik, Milos Gligoric, Sarfraz Khurshid

Remote due to strike

- Let's plan to stay remote during the strike

Keep me updated of any issues that you might be facing due to strike disruption

Grades have been posted for Midterm and attendance. Let us know if there are any issues.

We're still aiming to get HW 2 graded this week. I will keep you updated

Homework 3 is due in less than 1 week (Nov. 21). Please get started if you haven't.

Moving office hours to Friday this week (3-5pm)

Propose paper for paper reading review through Canvas (due today)

Determine if you are taking the Final or doing a Final Project. Please submit in Canvas. (due today)

Final project report can be a "blog post" (it will be submitted as a PR to the class website). This is an option if you want to make the report public. Otherwise, it is a written report.

Final project presentations:

Likely won't have time for all of them. Instead, please prepare a 12 minute presentation (we will be strict on time!)

I will randomly select 6 groups to present on the last day of class.

The rest will record a screen recording of the presentation.

Guest lecture: Felix Klock from amazon will be talking about the Rust compiler. (Nov. 29)

One more homework for the class (might be due after the last day of class to give you 2 weeks).

Get started early!

## **Review:**

Halide (other presentation)

## **Remainder of class**

Halide (other presentation)

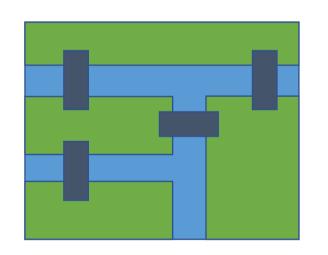
#### **Graph Processing**

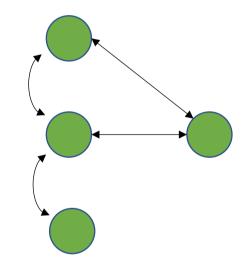
# Graphs (1736 Edition)

### Euler's Königsberg Bridges



Modern day



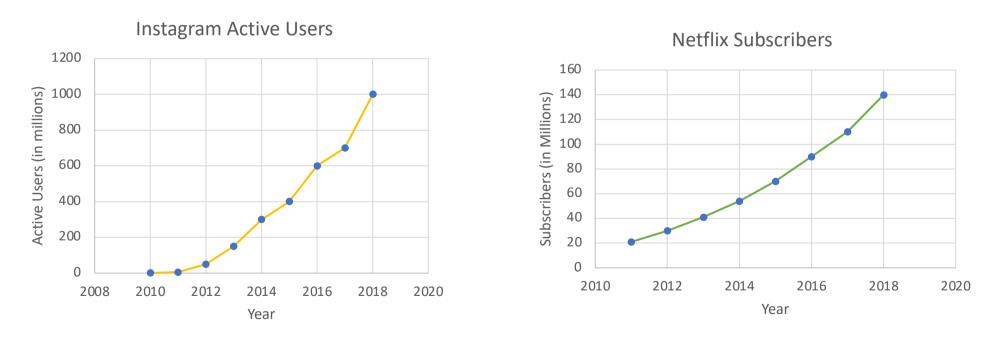


Abstract View

As a Graph

## Graphs in 2019

### Size/Growth of modern graphs

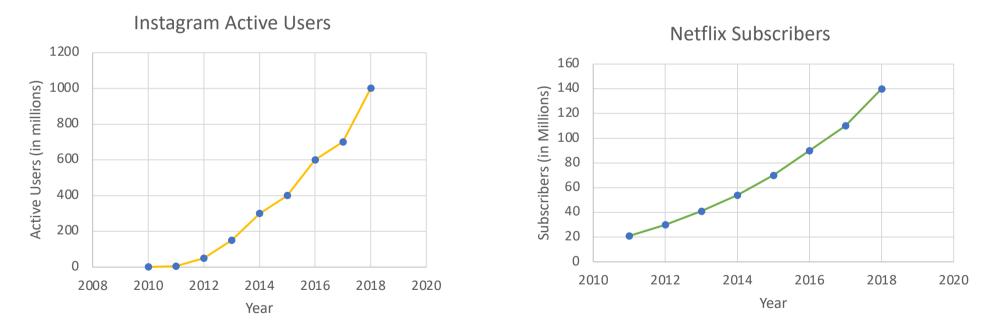


https://techcrunch.com/2018/06/20/instagram-1-billion-users/ https://www.statista.com/statistics/250934/quarterly-number-of-netflix-streaming-subscribers-worldwide/

# Graphs in 2019

- Applications:
  - recommendation systems

### Size/Growth of modern graphs

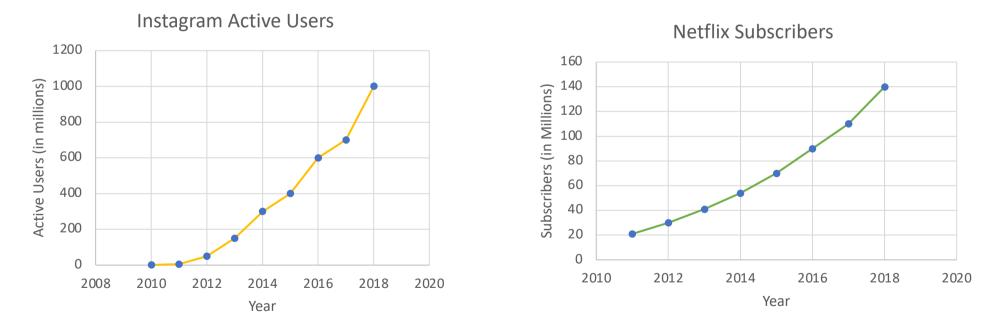


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# Graphs in 2019

### Size/Growth of modern graphs

- Applications:
  - recommendation systems
  - (mis)information spread

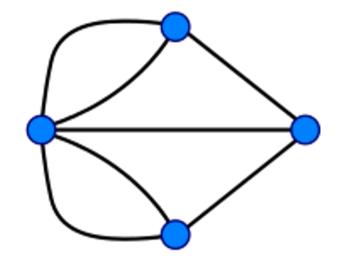


https://techcrunch.com/2018/06/20/instagram-1-billion-users/ https://www.statista.com/statistics/250934/quarterly-number-of-netflix-streaming-subscribers-worldwide/

# What is graph processing?

### Graphs are ubiquitous

- Social Networks
- Road Networks



### Graphs of interest are large:

– Millions of nodes, Billions of edges

Parallel Graph processing is necessary!

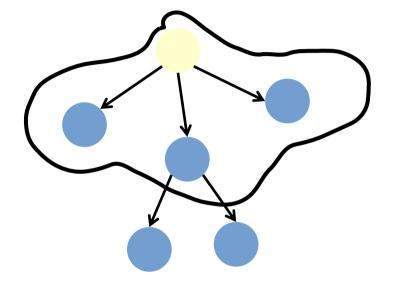
# **Graph Processing Platforms**

### **Cluster Processing Systems**

- Apache Giraph (Facebook)
- GraphLab (CMU)
- GraphX (UC Berkeley)

### Vertex-centric Programming Model

- Highly parallelizable
- Limited expressivity
- Optimized for scale-free graphs
- Scalable, but not performant



# Scalability, but at what COST? [McSherry et al. 2015]

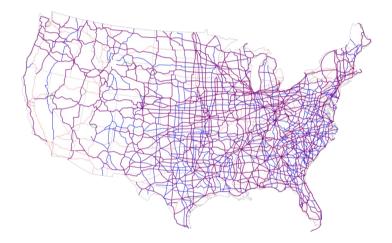
**Connected Components** 

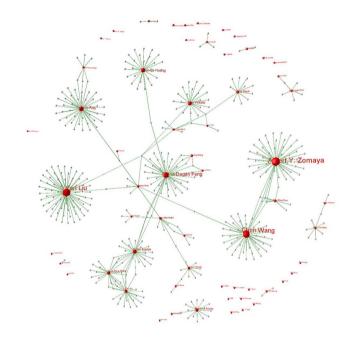
System/Algorithm	Cores	Twitter	UK-2007-05
GraphLab	128	242s	714s
GraphX	128	251s	800s
Label Propagation	1	153s	417s

Twitter: 41M vertices, 1.4B edges UK-2007-05: 105M vertices, 3.7B edges

McSherry F., Isard M., and Murray D. G., Scalability, but at what COST?, HotOS 2015

## Parallel Graph Processing Pitfalls





USA Road Network 24M nodes, 58M edges High diameter, Low Uniform Degrees

LiveJournal Social Network 5M nodes, 69M edges Low diameter, Highly-skewed Degrees



### **Perfect storm for a DSL**

State-of-the-art DSLs massively underperform

Handwritten optimized code exists (guide for DSL)

Optimizations are not portable:

- i.e. it makes sense to decouple optimizations from algorithm, similar to Halide

### IrGL (intermediate graph representation)

IrGL is a language for graph algorithm kernels

- Slightly higher-level than CUDA

IrGL kernels are compiled to CUDA code

- Incorporated into larger applications

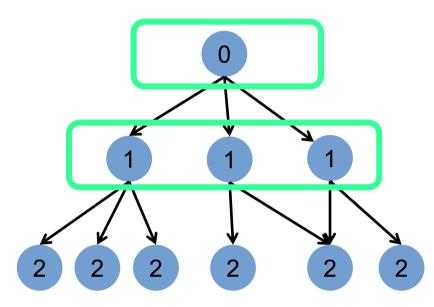
IrGL compiler applies 3 throughput optimizations

- User can select exact combination
- Yields multiple implementations of algorithm

Compiler generates all the interesting variants!

### Bottlenecks in GPU Graph Processing

## Example: Level-by-Level BFS



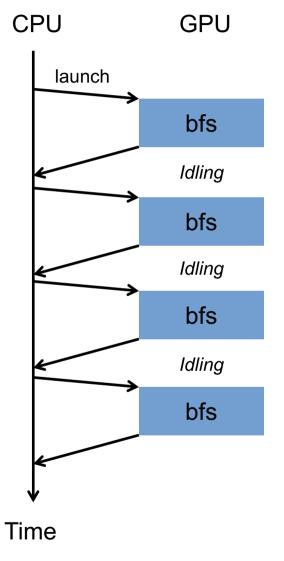
}

## Bottleneck #1: Short Kernels

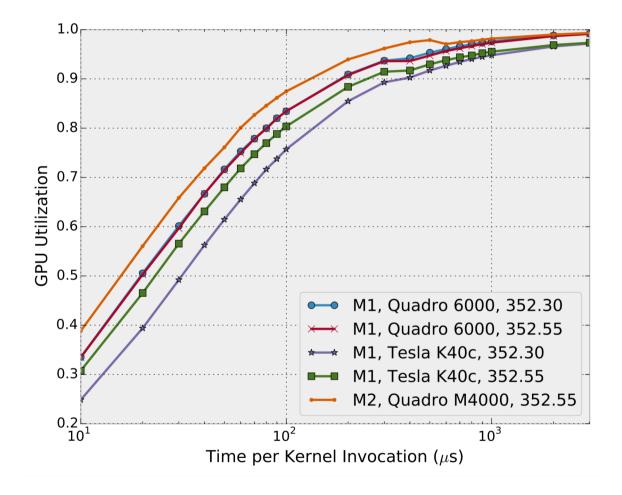
```
src.level = 0
Iterate bfs(graph, LEVEL) [src] {
    LEVEL++
}
```

.USA road network: 6261 bfs calls
.Average bfs call duration: 16 µs
.Total time should be 16\*6261 = 100 ms
.Actual time is 320 ms: 3.2x slower!

## **Iterative Algorithm Timeline**



## **GPU Utilization for Short Kernels**



# Improving Utilization

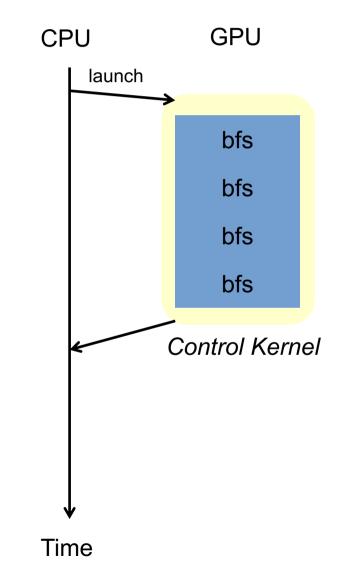
Generate Control Kernel to execute on GPU

Control kernel uses function calls on GPU for each iteration

Separates iterations with devicewide barriers

- Tricky to get right!

Device-wide barriers now supported in CUDA 9

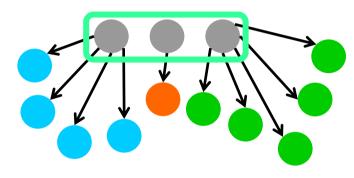


# Bottleneck #2: Load Imbalance from Inner-loop Serialization

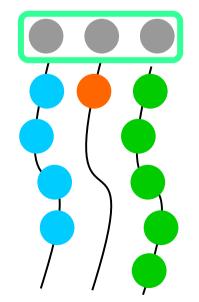
Worklist

Kernel bfs(graph, IFVFI)
ForAll(node in Worklist)
ForAll(edge in graph.edges(node))
if(edge.dst.level == INF)
edge.dst.level = LEVEL
Worklist.push(edge.dst)

```
src.level = 0
Iterate bfs(graph, LEVEL) [src] {
   LEVEL++
}
```



Threads



# **Exploiting Nested Parallelism**

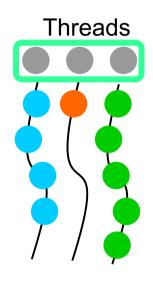
Generate code to execute inner loop in parallel

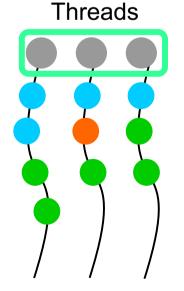
 Inner loop trip counts not known until runtime

Use Inspector/Executor approach at runtime

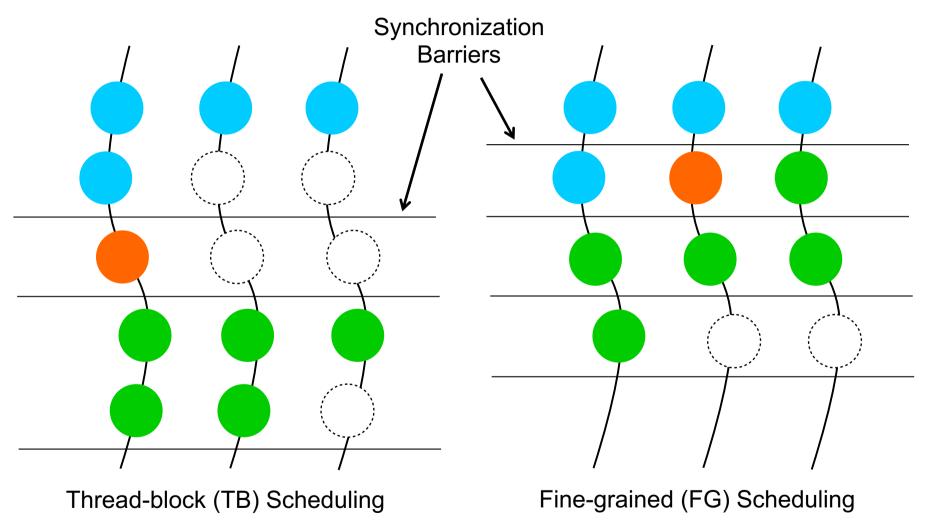
Primary challenges:

- Minimize Executor overhead
- Best-performing Executor varies by algorithm and input



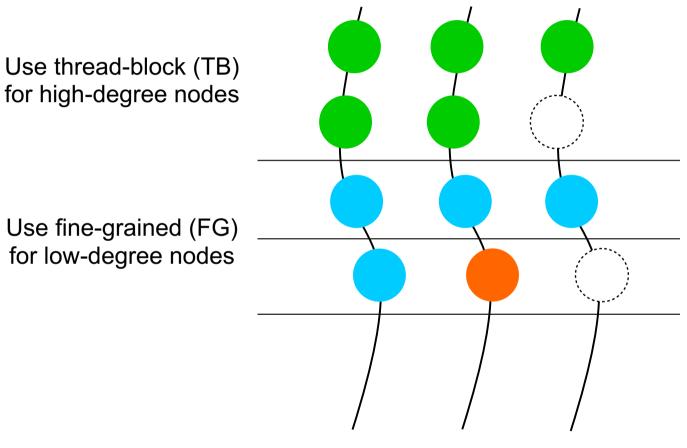


# Scheduling Inner Loop Iterations



Example schedulers from Merrill et al., Scalable GPU Graph Traversal, PPoPP 2012

## **Multi-Scheduler Execution**



Thread-block (TB) + Finegrained (FG) Scheduling

*Example schedulers from* Merrill et al., Scalable GPU Graph Traversal, PPoPP 2012

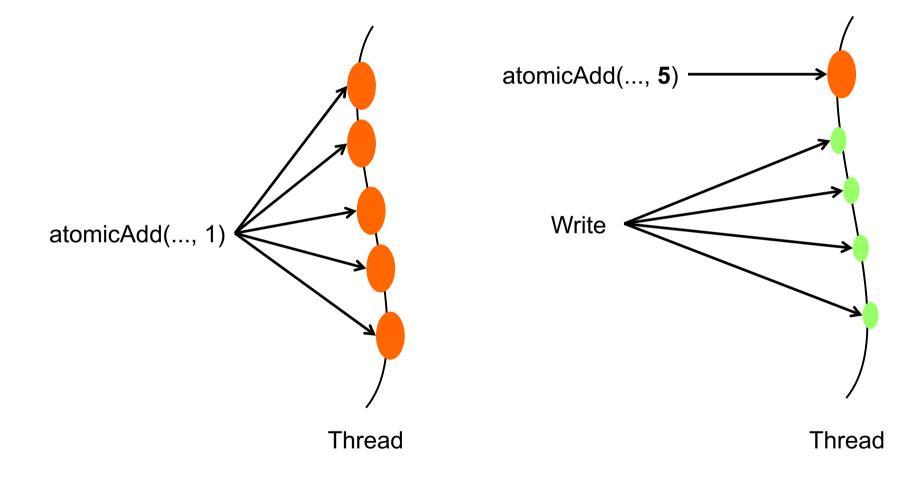
## **Bottleneck #3: Atomics**

```
Kernel bfs(graph, LEVEL)
    ForAll(node in Worklist)
        ForAll(edge in graph.edges(node))
            if(edge.dst.level == INF)
            edge.dst.level = LEVEL
            Worklist.push(edge.dst)

src.level = 0
Iterate bfs(graphing = atomicAdd(Worklist.length, 1)
            Worklist.items[pos] = edge.dst
```

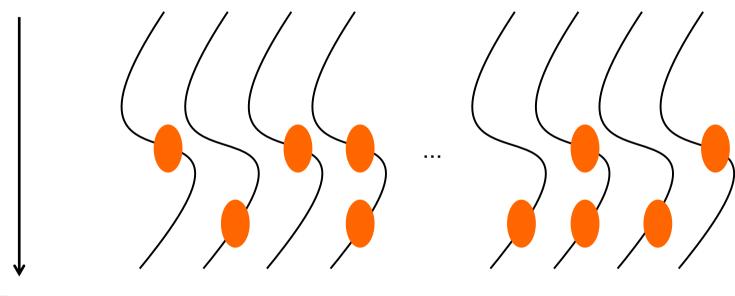
Atomic Throughput on GPU: 1 per clock cycle
 Roughly translated: 2.4 GB/s
 Memory bandwidth: 288GB/s

# Aggregating Atomics: Basic Idea



## **Challenge: Conditional Pushes**

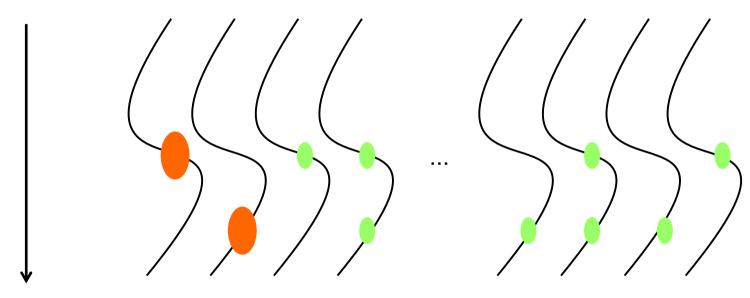
if(edge.dst.level == INF)
 Worklist.push(edge.dst)



Time

## **Challenge: Conditional Pushes**

if(edge.dst.level == INF)
 Worklist.push(edge.dst)



Time

Must aggregate atomics across threads

# Three Optimizations for Bottlenecks

### 1. Iteration Outlining

 Improve GPU utilization for short kernels

### 2.Nested Parallelism

- Improve load balance
- **3.Cooperative Conversion** 
  - Reduce atomics

### **Unoptimized BFS**

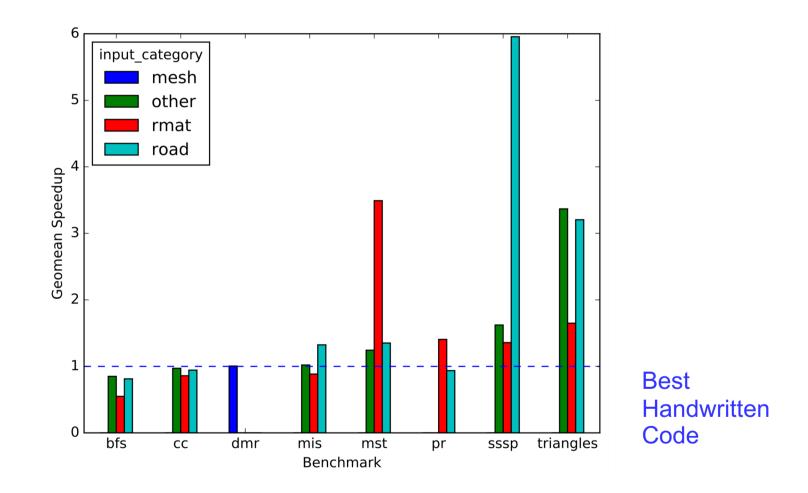
- -~15 lines of CUDA
- 505ms on USA road network
- Optimized BFS
  - -~200 lines of CUDA
  - 120ms on the same graph

# Evaluation

### •Eight irregular algorithms

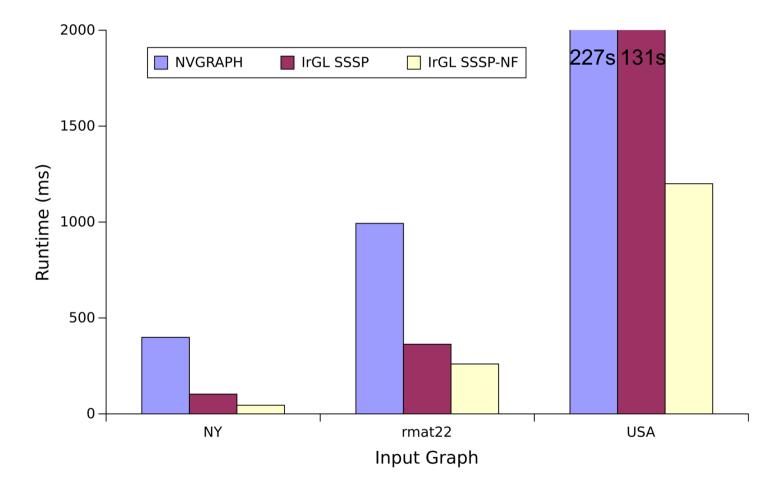
- Breadth-First Search (BFS) [Merrill et al., 2012]
- Connected Components (CC) [Soman et al., 2010]
- Maximal Independent Set (MIS) [Che et al., 2013]
- Minimum Spanning Tree (MST) [da Silva Sousa et al. 2015]
- PageRank (PR) [Elsen and Vaidyanathan, 2014]
- Single-Source Shortest Path (SSSP) [Davidson et al. 2014]
- Triangle Counting (TRI) [Polak et al. 2015]
- Delaunay Mesh Refinement (DMR) [Nasre et al., 2013]

#### **Overall Performance**



Note: Each benchmark had a single set of optimizations applied to it

### Comparison to NVIDIA nvgraph SSSP



#### Making IrGL portable

One Size Doesn't Fit All: Quantifying Performance Portability of Graph Applications on GPUs

Imperial College London, UK

Princeton University, USA UC Santa Cruz, USA tyler.sorensen@ucsc.edu

results, but at the expense of portability.

degrees of specialisation.

University of Rochester, USA sree@cs.rochester.edu Tyler Sorensen

Abstract—Hand-optimising graph algorithm code for different

GPUs is particularly labour-intensive and error-prone, involving

complex and ill-understood interactions between GPU chips,

applications, and inputs. Although the generation of optimised

variants has been automated through graph algorithm DSL

compilers, these do not yet use an optimisation policy. Instead

they defer to techniques like autotuning, which can produce good

In this work, we propose a methodology to automatically

identify portable optimisation policies that can be tailored ("semi-

specialised') as needed over a combination of chips, applications

and inputs. Using a graph algorithm DSL compiler that targets

the OpenCL programming model, we demonstrate optimising

and 6 GPUs spanning multiple vendors. We show that existing

automatic approaches for building a portable optimisation policy

fall short on our dataset, providing trivial or biased results.

Thus, we present a new statistical analysis which can characterise optimisations and quantify performance trade-offs at various

We use this analysis to quantify the performance trade-

offs as portability is sacrificed for specialisation across three

natural dimensions: chip, application, and input. Compared to

not optimising programs at all, a fully portable approach provides a 1.15× improvement in geometric mean performance, rising to

 $1.29 \times$  when specialised to application and inputs (but not hard-

modify-write aggregation transformation applied to the sg-cmb

microbenchmark (discussed in Section VIII) shows a speedup of more than  $22\times$  on an AMD GPU, but yields a *slowdown* 

Although specialisation is useful, identifying transforma- $(.88\times)$  on an Nvidia GPU. tions that lead to portable performance improvements, i.e. those that yield improvements consistently, can deliver important insights into similarities (and differences) across environments. Additionally, portable transformations can be more widely deployed, reducing the maintenance demanded by fragile specialisations. To the best of our knowledge, however, there is no systematic and automatic methodology that can identify these portable transformations from a larger set of compiler transformations. In part, this is not a straightforward problem: prior work [8]-[10] has shown that even identifying graph algorithms to run in a portable fashion across a wide transformations that yield performance improvements in a range of GPU devices for the first time. We use this compiler and its optimisation space as the basis for a large empirical study across 17 graph applications, 3 diverse graph inputs

fixed environment can be confounded by chance effects. Worse, a quest in search of portable transformations may be quixotic – there may be no such set of portable transformations

due to the diversity of architectures today. In that event, then, we would like a rigorous methodology that explicitly delimits the environment in which a particular transformation is effective. For example, an analysis that can confirm that transformation T only yields performance improvements on architecture A is still valuable. Knowledge of such semiportable transformations would also immediately enable semispecialisation. Specialisation does not have to be an all or nothing strategy. Transformations can be specialised across The second of the second critical features of specialisation. For

#### Believe it or not...

#### GPU != Nvidia

#### There are probably more Apple/Intel GPUs in this room than Nvidia GPUs

We perform a massive empirical study (240 hours across 6 different GPUs)

Using a GPU graph application DSL and optimizing compiler, we find:



Compiler optimizations can provide **speedups** of up to **16x** and a geomean across the domain of **1.5x** 



These optimizations can also provide **slowdowns** of up to **22x** 

# Traditional *performance portability* fall short for graph applications on GPUs

• Previous approaches produce trivial or biased results

All optimization combinations cause slowdowns **AND** speedups across the domain.



Magnitude-based approaches are **biased** towards more sensitive GPUs

# **Rank-based** statistical procedures offer a new way of thinking about performance portability

# **Rank-based** statistical procedures offer a new way of thinking about performance portability

Produces non-trivial performance portable optimization combination yielding a **max speedups** of **6x** 



Analysis can create **semispecialized** optimization strategies, which yield greater speedups and **performance critical insights**.

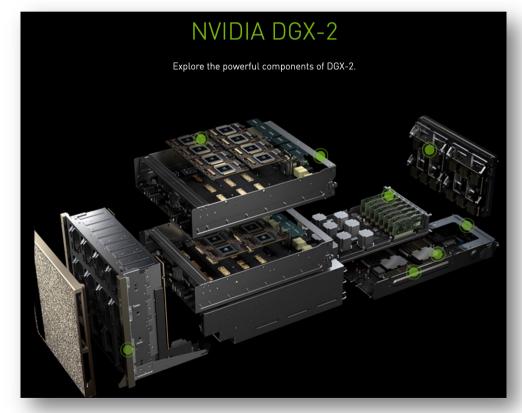
### What is a GPU? (1999 Edition)

The technical definition of a GPU is "a single chip processor with integrated <u>transform, lighting</u>, triangle setup/clipping, and <u>rendering</u> engines that is capable of processing a minimum of 10 million <u>polygons</u> per second."

https://web.archive.org/web/20160408122443/http://www.nvidia.com/object/gpu.html

# What is a GPU? (2019 Edition)

20 years later, Nvidia's homepage advertises GPUs without the ability to output graphics!



https://www.nvidia.com/en-us/data-center/dgx-2/



Still used for highend graphics





Still used for highend graphics

Use in data centers for AI and scientific computing









Still used for highend graphics

Use in data centers for AI and scientific computing

Increasingly used in mobile devices

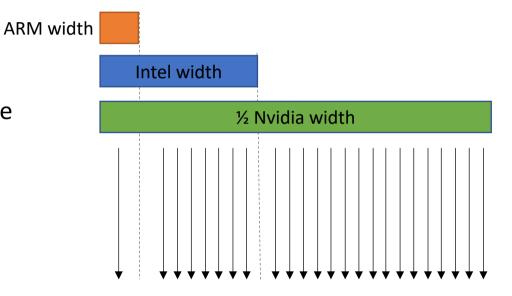
#### Programmable vector lanes?

- Nvidia GPUs have 32 threads per lane
- Intel GPUs have 8 threads per lane
- ARM GPUs have 1 thread per lane

#### High Bandwidth?

#### Highly parallel?

- Nvidia GPUs execute over 10K threads concurrently
- ARM GPUs execute 500 threads concurrently







#### Role of a compiler

#### As GPUs have diversified, it's the compilers job to

- judiciously apply optimizations

   (apply transformations that cause speedups, not slowdowns)
- specialize when possible

# This Work

Characterizing performance portability of Graph applications on GPUs

#### We Developed:

• A portable backend for a GPU graph application DSL and optimizing compiler

#### We Conducted:

• A large empirical study, collecting 240 hours of runtime data across 6 GPU

#### We Characterized:

• Performance portability in this domain using a rank-based statistical method

# A GPU Graph DSL and Compiler

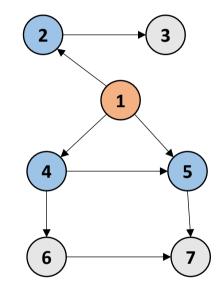
#### IrGL : Pai and Pingali, OOPSLA 2016

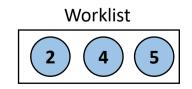
• Original work targets only Nvidia GPUs

#### First class support for nodes, edges, worklists

#### Optimizing compiler

- Load balancing
- On-chip synchronization
- Atomic RMW coalescing



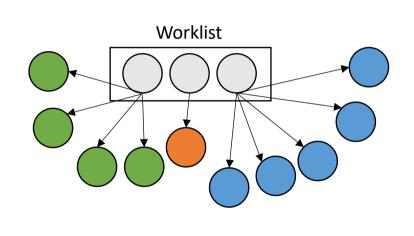


## IrGL Optimizations

Load Balancing

Graphs have *irregular* parallelism leading to load imbalance

IrGL has 3 transformations to perform load balancing at 3 levels of the GPU hierarchy: Local, Subgroup, Workgroup

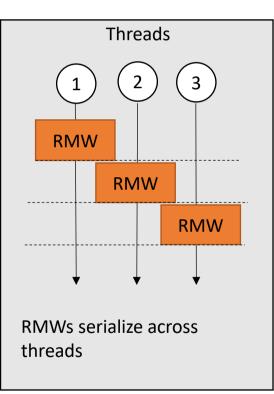


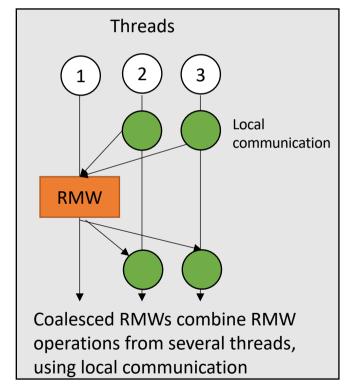
Threads

### IrGL Optimizations

#### Atomic RMW Coalescing

Graph applications require atomic RMWs to update the worklist for the next iteration

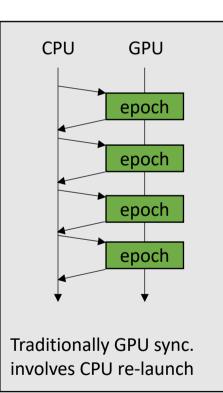


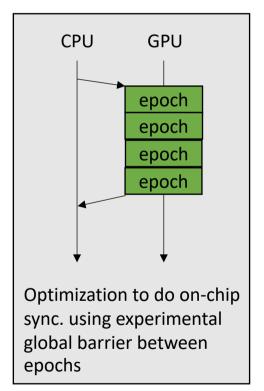


# IrGL Optimizations

#### **On-chip Synchronization**

Many graph apps are iterative, requiring a global sync between iterations (epochs)





# **Our Empirical Study**

	Applications		
	BFS		GPUs
Optimizations	SSSP		Nvidia-Quadro
LB - Local	PR		Nvidia-1080
LB - Subgroup	СС	Inputs	AMD-R9
LB - Workgroup	MIS	Uniform	Intel-Iris
OC - Sync	MST	RMAT	Intel-HD5500
RMW-Cls	TRI	NY-Road	ARM-Mali T628

All combinations of above were run

Total runtime of 240 hours

**Over 10K individual runs** 

widest empirical study across GPUs that we are aware of!

#### **Performance Portability**

Which optimizations should be applied to provide best performance across the entire domain?

Optimizations
LB - Local
LB - Subgroup
LB - Workgroup
OC - Sync
RMW-Cls

Optimization Space (32 options)

Applications		
BFS		GPUs
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TRI	NY-Road	ARM-Mali T628
	Domain	

#### Do No Harm

#### Only apply an optimization if it:

- Does not provide any slowdowns across the entire domain
- Provides at least one speedup

Easily to query from our data set, and we found...

#### Do No Harm

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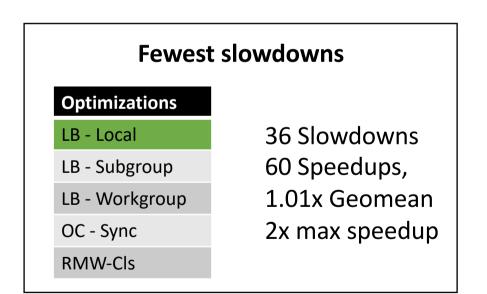
Easily to query from our data set, and we found...

# NOTHING!!!

All optimizations provided at least one instance of a slowdown

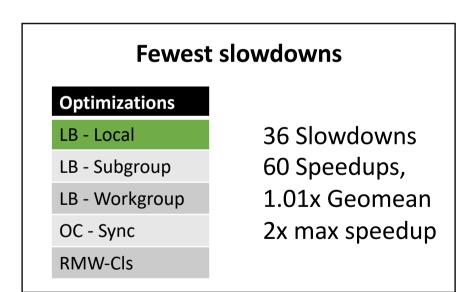
#### Do the Least Harm

Relaxation of Do no Harm: Select the optimization combination that caused the fewest slowdowns.



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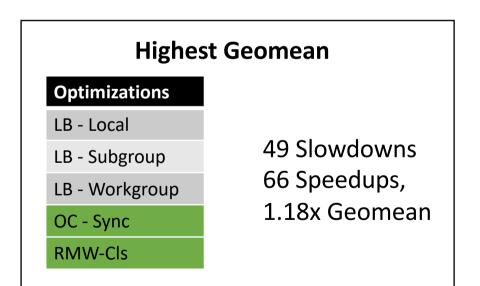


From our exploration:

Compiler optimizations can provide **speedups** of up to **16x** and a geomean across the domain of **1.5x** 

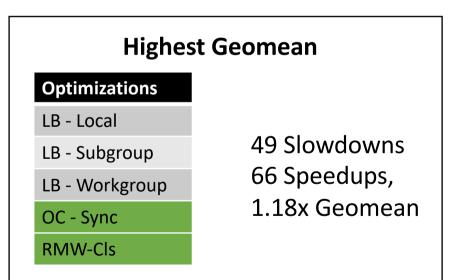
#### Max Geomean

Select the optimization combination that provides the highest geomean across the domain



#### Max Geomean

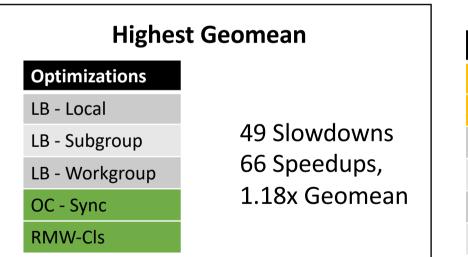
Select the optimization combination that provides the highest geomean across the domain



GPUs	# Speedups	# Slowdowns
Nvidia-Quadro	10	21
Nvidia-1080	00	16
AMD-R9	12	3
Intel-Iris	10	2
Intel-HD5500	14	2
ARM-Mali T628	20	5

#### Max Geomean

Select the optimization combination that provides the highest geomean across the domain

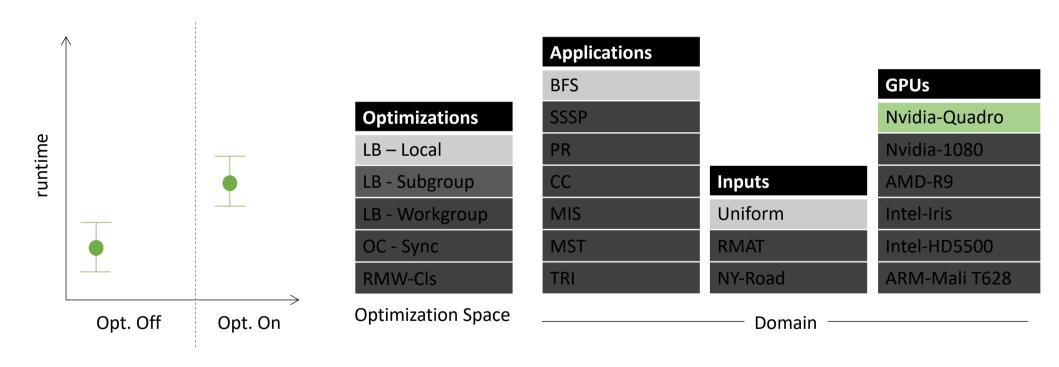


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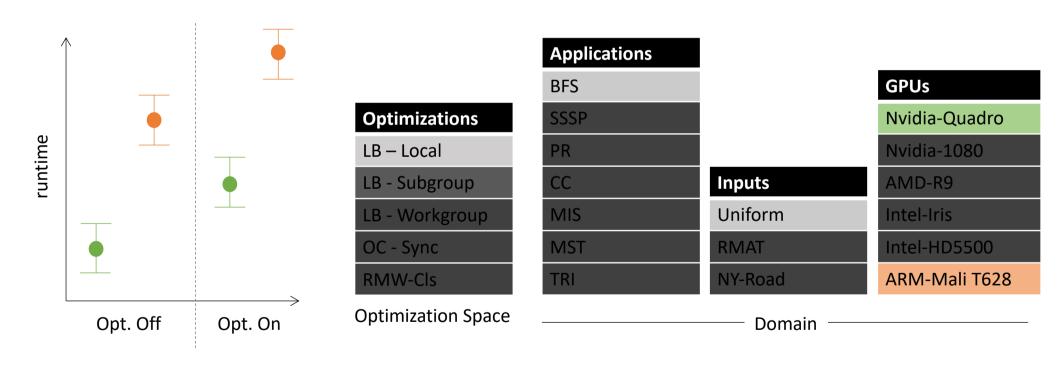
For a single chip, app, input combination, just compare confidence intervals

	Applications		
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Optimization Space		— Domain —	

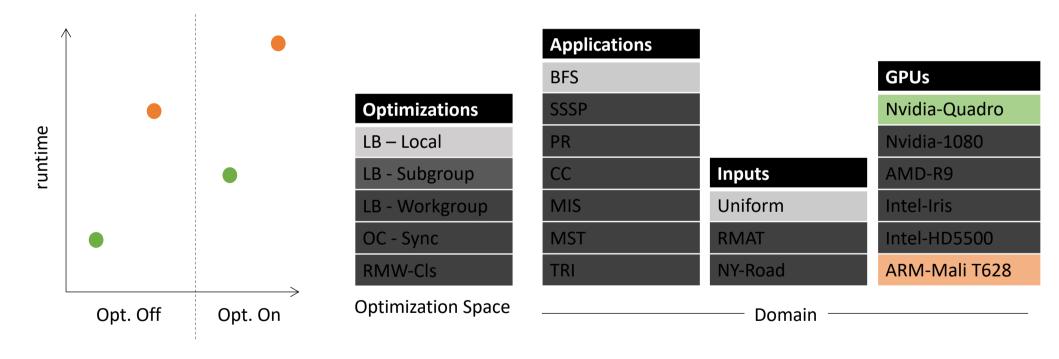
For a single chip, app, input combination, just compare confidence intervals



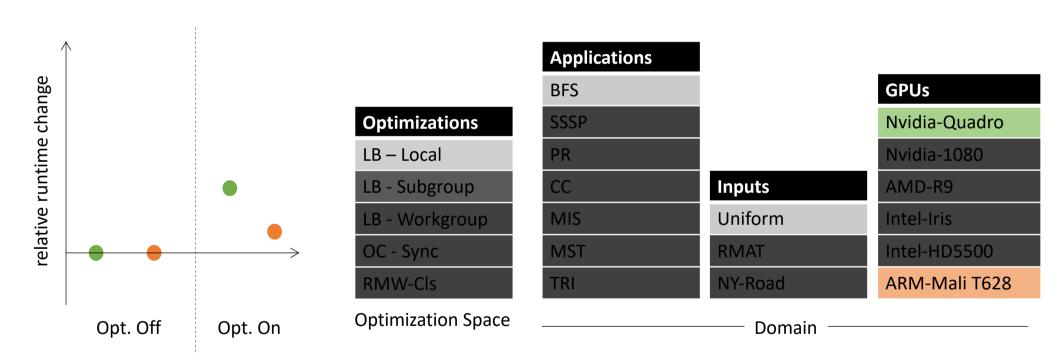
Things become trickier when more chips are added



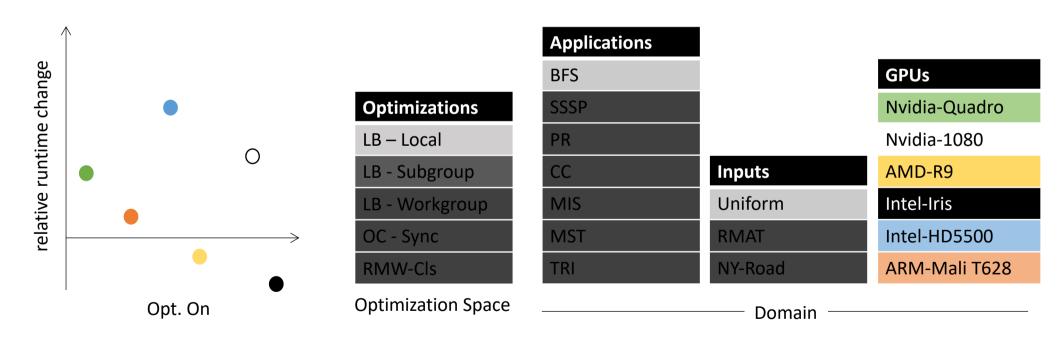
First, only consider points whose confidence intervals don't overlap

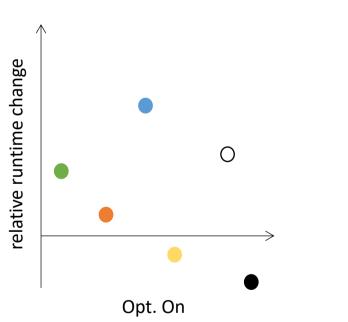


Normalize with respect to Opt. Off



Only consider relative *Opt. On* points, we can show more now visually



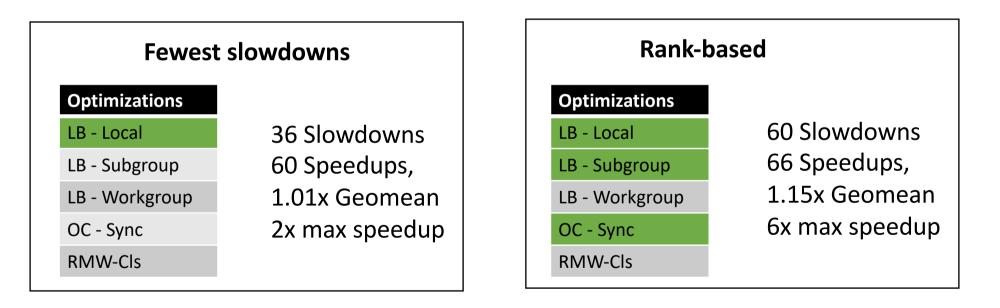


We now use the *Mann-Whitney U test* to determine if points are *stochastically more likely to be above* the horizontal line.

The test is *non-parametric*: it assumes nothing about the distribution.

## **Rank-based Results**

Compared to fewest slowdowns, more slowdowns, also more speedups. Higher Geomean and higher max



### **Rank-based Results**

## Compared to highest geomean: No more bias against Nvidia GPUs

Highest Geomean

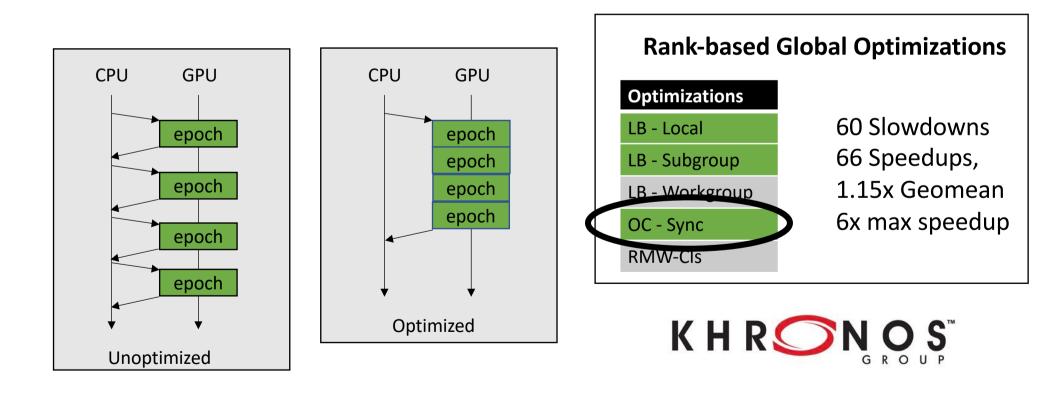
GPUs	# Speedups	# Slowdowns
Nvidia-Quadro	10	21
Nvidia-1080	00	16
AMD-R9	12	3
Intel-Iris	10	2
Intel-HD5500	14	2
ARM-Mali T628	20	5

#### Rank-based

GPUs	# Speedups	# Slowdowns
Nvidia-Quadro	22	13
Nvidia-1080	13	07
AMD-R9	17	4
Intel-Iris	10	10
Intel-HD5500	21	12
ARM-Mali T628	20	04

## Impact on GPU Programming Languages

Working with Khronos group to better specify a progress model that allows on-chip synchronization (OC-Sync)



## **GPU Compiler Summary**

## GPUs and graph applications are important emerging domain.

• We perform a massive empirical study (240 hours across 6 different GPUs)

Traditional *performance portability* fall short in this domain.

**Rank-based** statistical procedures offer a new way of thinking about performance portability

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LB - Local

LB - Subgroup

LB - Workgroup

OC - Sync

**RMW-Cls** 

Applications		
BFS		GPUs
SSSP		Nvidia-Quadro
PR		Nvidia-1080
CC	Inputs	AMD-R9
MIS	Uniform	Intel-Iris
MST	RMAT	Intel-HD5500
TRI	NY-Road	ARM-Mali T628
	Domain	

#### Optimizations

LB - Local

LB - Subgroup

LB - Workgroup

OC - Sync

**RMW-Cls** 

Applications		
BFS		GPUs
SSSP		
PR		
СС	Inputs	
MIS	Uniform	
MST	RMAT	
TRI	NY-Road	ARM-Mali T628
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#### Optimizations

LB - Local

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**RMW-Cls** 

Applications		
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SSSP		
PR		
СС	Inputs	
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MST	RMAT	Intel-HD5500
TRI	NY-Road	
	— Domain —	

#### Optimizations

LB - Local

LB - Subgroup

LB - Workgroup

OC - Sync

**RMW-Cls** 

Applications		
BFS		GPUs
SSSP		
PR		
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TRI	NY-Road	
	Domain	

## Semi-specialization

## Provides 6 different optimization strategies, one per chip:

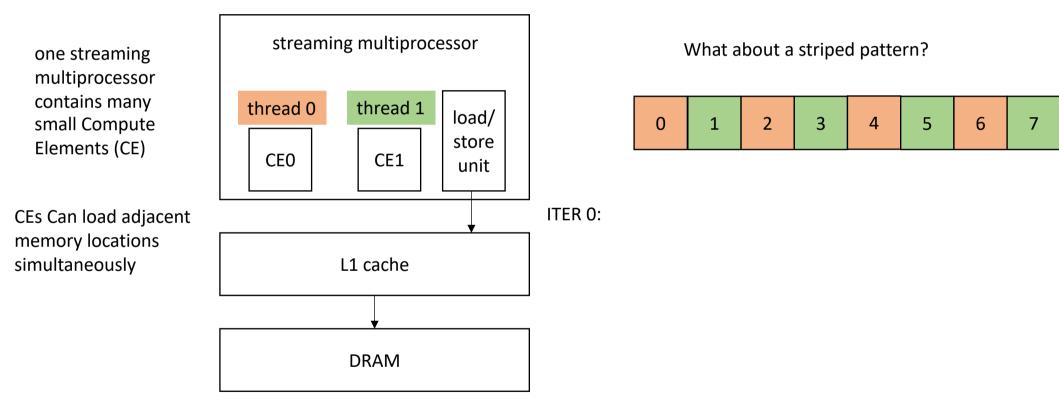
GPUs	LB-Local	LB-Subgroup	LB-Workgroup	OC - Sync	RMW-Cls
Nvidia-Quadro	.86	.68	.22	.47	.07
Nvidia-1080	.86	.78	.32	.22	.19
AMD-R9	.90	.74	.18	.65	.70
Intel-Iris	.58	.63	.09	.73	.67
Intel-HD5500	.54	.56	.12	.63	.41
ARM-Mali T628	.47	.76	.11	.71	.12

## Semi-specialization

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# What about streaming multiprocessors (GPUs)?



## Semi-specialization

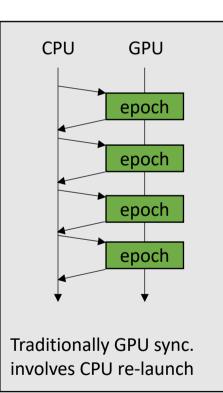
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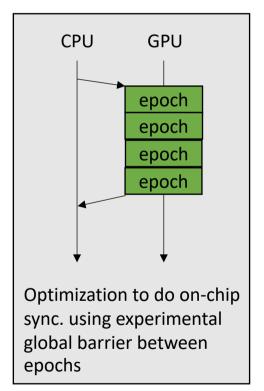
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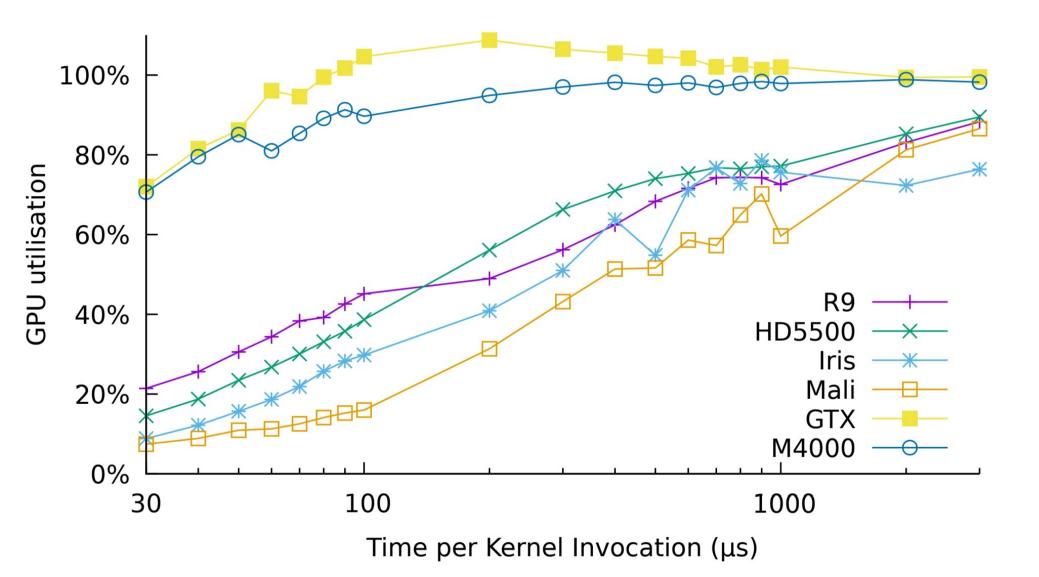
## IrGL Optimizations

### **On-chip Synchronization**

Many graph apps are iterative, requiring a global sync between iterations (epochs)







## Next lecture

Optimization impact in general purpose languages!