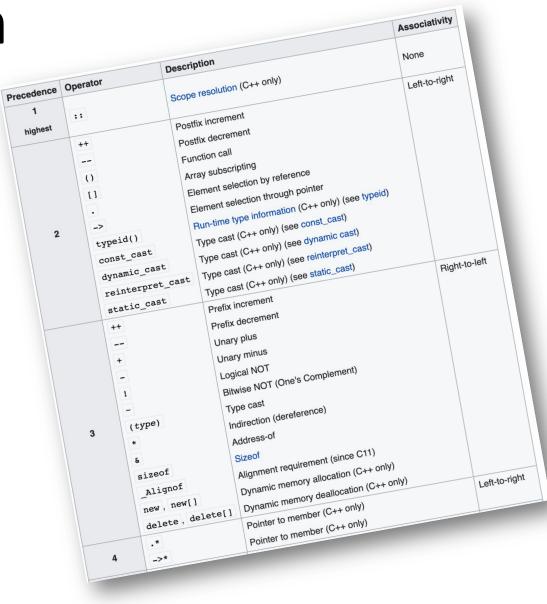
CSE211: Compiler Design Oct. 1, 2021

- **Topic**: Parsing overview 3 (associativity and production actions)
- Questions:
 - What is associativity?
 - What are some operators that are associative and what are some that are not?



Announcements

- Homework 1 will be released on Monday
- if you have ideas for projects, we can start discussing!
- Join the slack for discussions
 - Thanks to Farid for some initial discussion points!
- New people:
 - Introductions

Review

• How do we define a context-free grammar?

BNF Production Rules

- Tokens:
 - NUM = [0-9]+
 - PLUS = '\+'
 - TIMES = '*'
 - LP = '\('
 - RP = \)'

expression : NUM

| expression PLUS expression| expression TIMES expression| LP expression RP

Review

• How do we determine if a string matches a context-free grammar?

Parse trees

 A string is accepted by a BNF form if and only if there exists a parse tree.

input: (1+5)*6

expr : NUM

expr PLUS expr

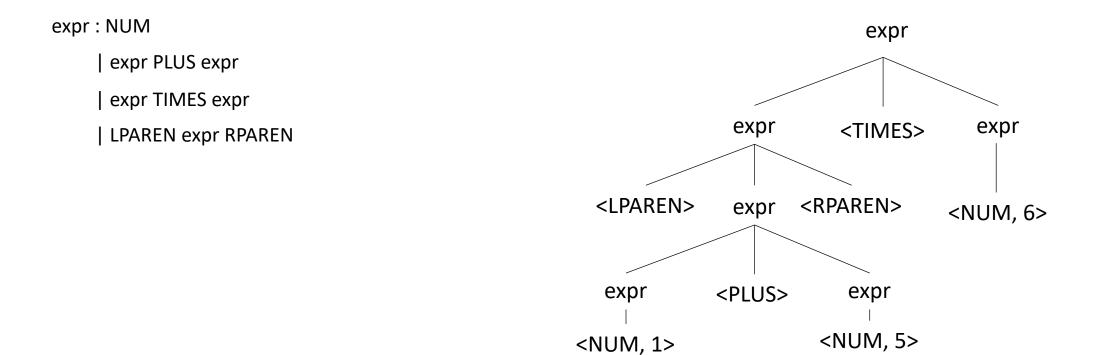
| expr TIMES expr

| LPAREN expr RPAREN

Parse trees

 A string is accepted by a BNF form if and only if there exists a parse tree.

input: (1+5)*6



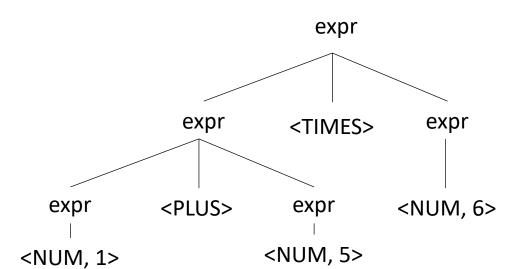
Review

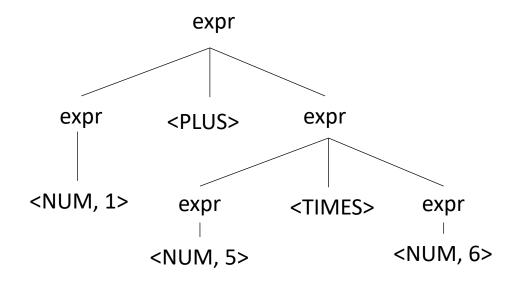
• What do we call it when a CFG can produce 2 different parse trees for the same string? Is this an issue?

Ambiguous grammars

expr : NUM | expr PLUS expr | expr TIMES expr | LPAREN expr RPAREN

• input: 1 + 5 * 6





Review

• How do we encode precedence in a CFG?

Now lets create a parse tree

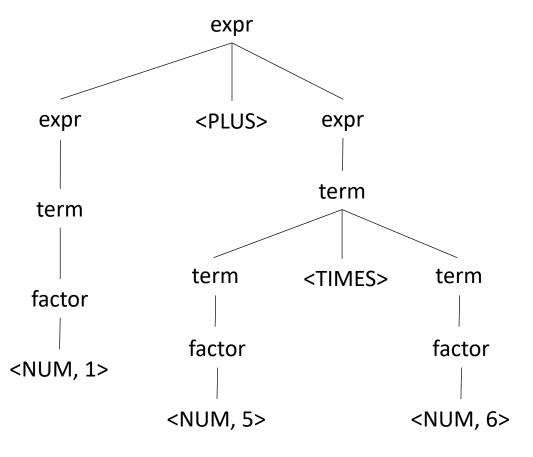
input: 1+5*6

Operator	Name	Productions
+	expr	: expr PLUS expr term
*	term	: term TIMES term factor
()	factor	: LPAREN expr RPAREN NUM

Now lets create a parse tree

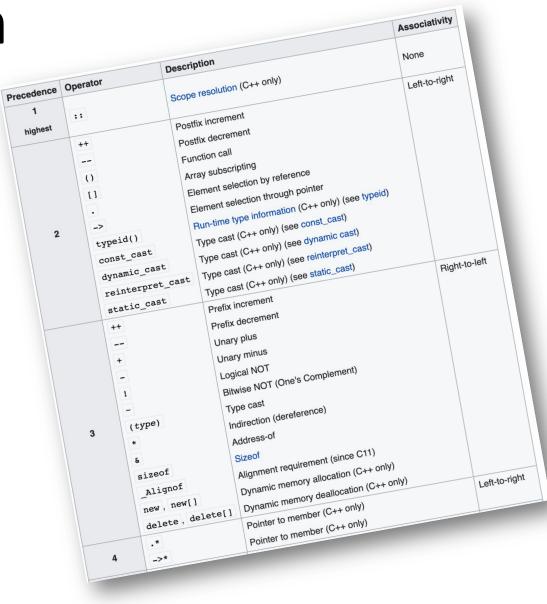
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 - What are some operators that are associative and what are some that are not?



Let's make some more parse trees

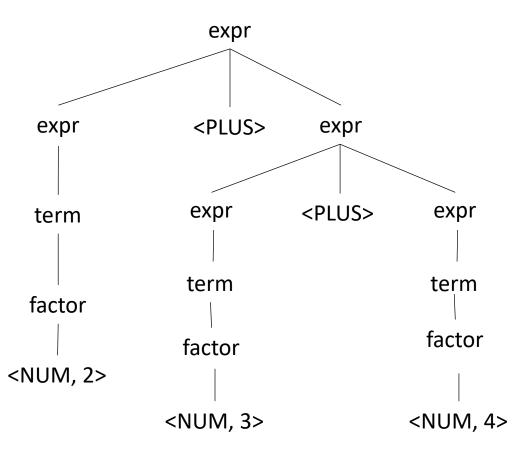
input: 2+3+4

Operator	Name	Productions
+	expr	: expr PLUS expr term
*	term	: term TIMES term factor
()	factor	: LP expr RP NUM

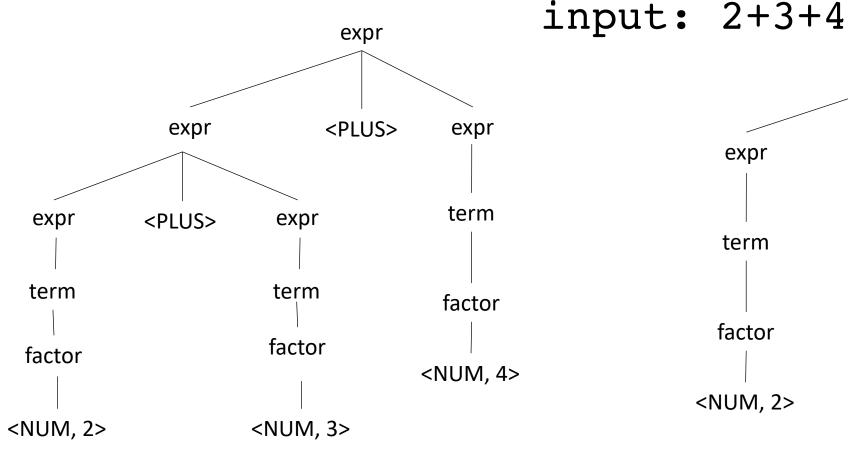
Let's make some more parse trees

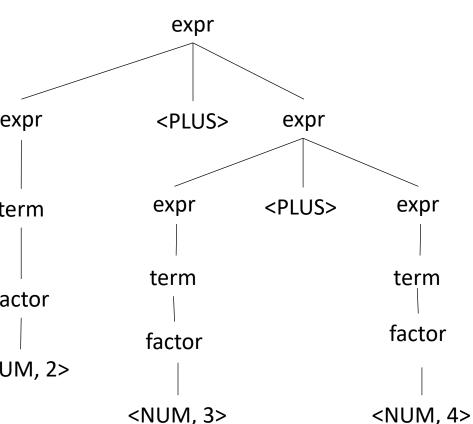


Operator	Name	Productions
+	expr	: expr PLUS expr term
*	term	: term TIMES term factor
()	factor	: LP expr RP NUM



This is ambiguous, is it an issue?

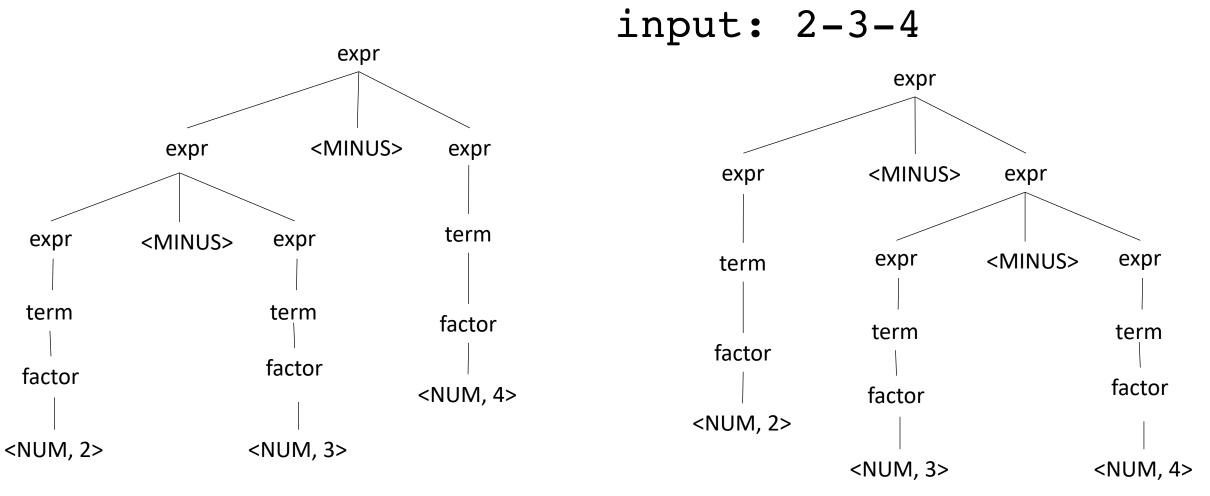




What about for a different operator?

input: 2-3-4

What about for a different operator?



Which one is right?

Associativity

The order in which we evaluate the same operator

Sometimes it doesn't matter:

- Integer arithmetic
- Integer multiplication
- What else?

Good test:

• ((a OP b) OP c) == (a OP (b OP c))

What about floating point arithmetic?

Associativity

The order in which we evaluate the same operator

- left to right (left-associative)
 - 2-3-4 is evaluated as ((2-3) 4)
 - What other operators are left-associative
- right-to-left (right-associative)
 - Any operators you can think of?

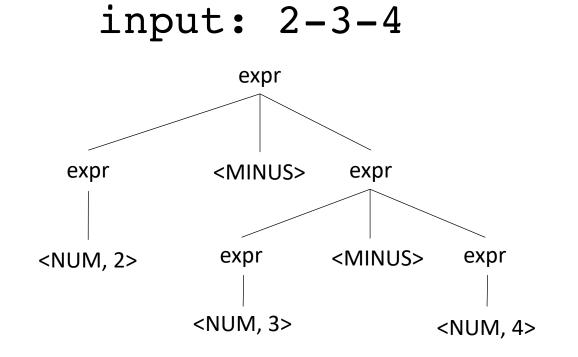
Associativity

The order in which we evaluate the same operator

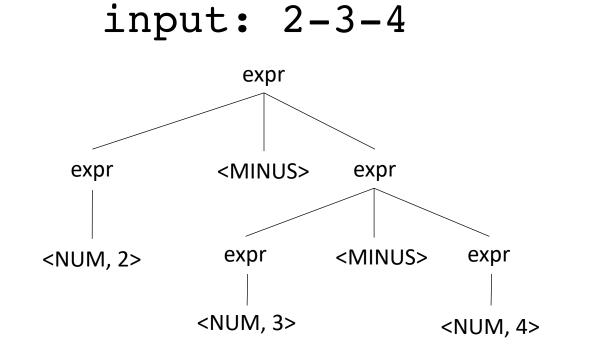
- left to right (left-associative)
 - 2-3-4 is evaluated as ((2-3) 4)
 - What other operators are left-associative
- right-to-left (right-associative)
 - Any operators you can think of?
 - Assignment, power operator

How to encode associativity?

- Like precedence, some tools (e.g. YACC) allow associativity specification through keywords:
 - "+": left, "^": right
- Like precedence, we can also encode it into the production rules

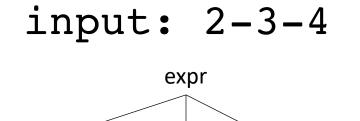


Operator	Name	Productions
-	expr	: expr MINUS expr NUM



Operator	Name	Productions
-	expr	: expr MINUS NUM NUM

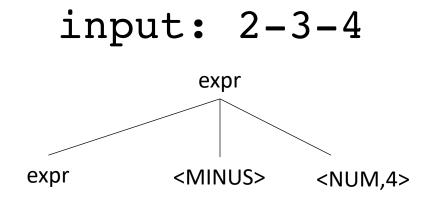
No longer allowed



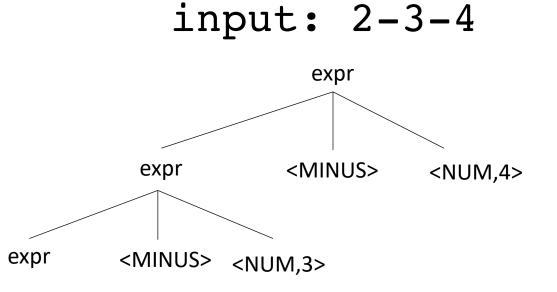
		<
expr	<minus></minus>	<num,?></num,?>

Operator	Name	Productions
-	expr	: expr MINUS NUM NUM

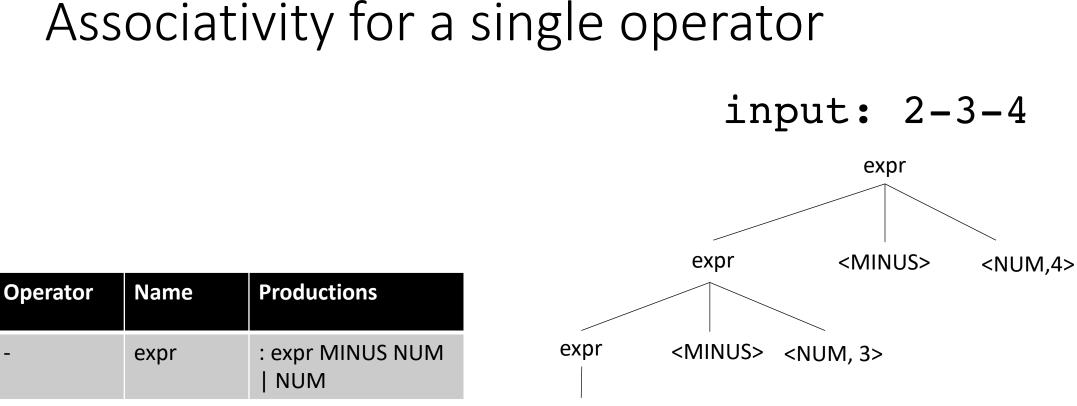
Lets start over



Operator	Name	Productions
-	expr	: expr MINUS NUM NUM

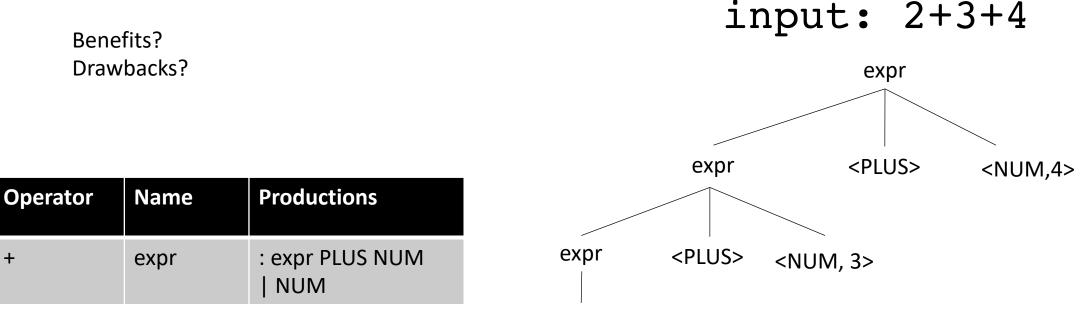


Operator	Name	Productions
-	expr	: expr MINUS NUM NUM



<NUM, 2>

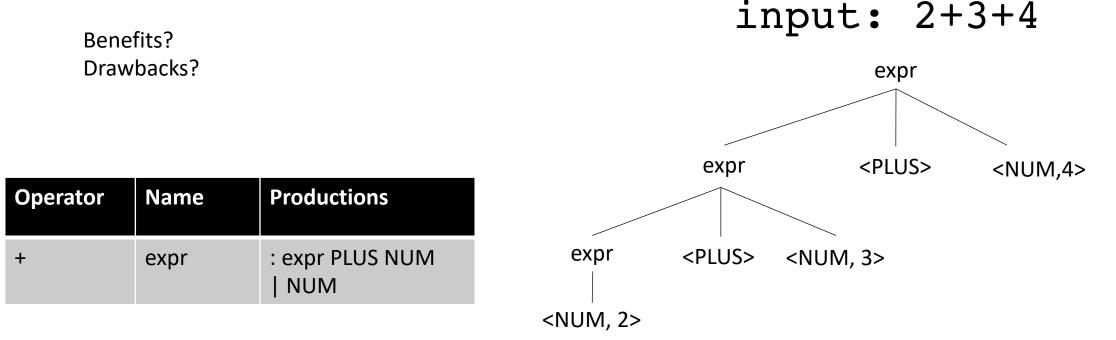
Should you have associativity when its not required?



+

<NUM, 2>

Should you have associativity when its not required?



Good design principle to avoid ambiguous grammars, even when strictly not required too.

Helps with debugging, etc. etc.

Many tools will warn if it detects ambiguity

Let's make a richer grammar

Let's add minus, division and power to our grammar

Operator	Name	Productions
+,-	expr	: expr PLUS term expr MINUS term term
*,/	term	: term TIMES pow term DIV pow pow
٨	pow	: factor CARROT pow factor
()	factor	: LPAR expr RPAR NUM

Tokens: NUM = [0-9]+ PLUS = ' + ' TIMES = ' + ' LP = ' (' RP =)' MINUS = '-' DIV = '/' $CARROT = ' ^'$

Let's make a richer grammar

Let's add minus, division and power to our grammar

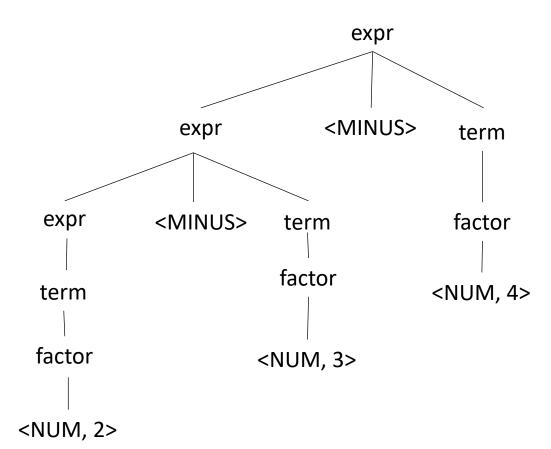
Operator	Name	Productions
+,-	expr	: expr PLUS term expr MINUS term term
*,/	term	: term TIMES pow : term DIV pow pow
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()	factor	: LPAR expr RPAR NUM

Tokens: NUM = [0-9]+ PLUS = ' + ' TIMES = ' + ' LP = ' (' RP =)' MINUS = '-' DIV = '/' $CARROT = ' ^'$

Let's make a richer grammar

input: 2-3-4

Operator	Name	Productions
+,-	expr	: expr PLUS term expr MINUS term term
*,/	term	: term TIMES pow : term DIV pow pow
^	pow	: factor CARROT pow : factor
()	factor	: LPAR expr RPAR NUM



Production rules in a compiler

- Great to check if a string is grammatically correct
- But can the production rules actually help us with compilation??

Production actions

- Each production *option* is associated with a code block
 - It can use values from its children
 - it returns a value to its parent
 - Executed in a post-order traversal (natural order traversal)

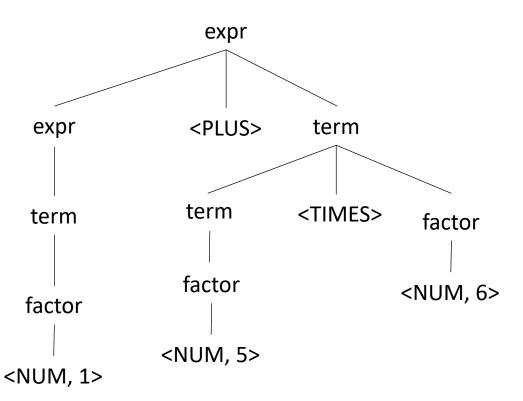
Production actions

Example: executing a mathematical expression during parsing

Children values are passed in as an array C, indexed from left to right

Operator	Name	Productions	Actions
+,-	expr	: expr PLUS term expr MINUS term term	<pre>{ret C[0] + C[2]} {} {ret C[0]}</pre>
*,/	term	: term TIMES factor : term DIV factor factor	<pre>{ret C[0] * C[2]} {} {ret C[0]}</pre>
()	factor	: LPAR expr RPAR NUM	<pre>{} {ret int(C[0])}</pre>

input: 1+5*6



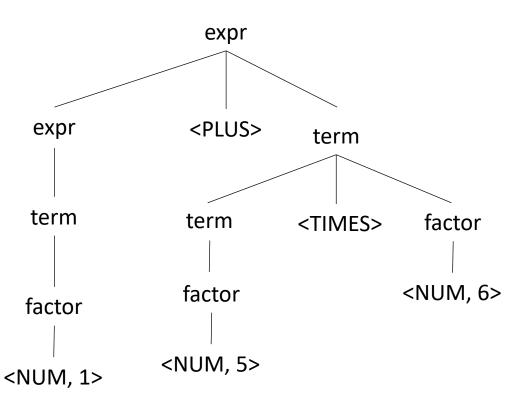
Production actions

Example: executing a mathematical expression during parsing

Children values are passed in as an array C, indexed from left to right

Operator	Name	Productions	Actions
+,-	expr	: expr PLUS term expr MINUS term term	<pre>{ret C[0] + C[2]} {ret C[0] - C[2]} {ret C[0]}</pre>
*,/	term	: term TIMES factor : term DIV factor factor	<pre>{ret C[0] * C[2]} {ret C[0] / C[2]} {ret C[0]}</pre>
()	factor	: LPAR expr RPAR NUM	<pre>{ret C[1]} {ret int(C[0])}</pre>

input: 1+5*6



We have just implemented a simple arithmetic interpreter! Could this be in a compiler?

Next week

- We will look at LEX and YACC
- Homework will be released on Monday
- Enjoy your weekend!