CSE110A: Compilers

May 31, 2023

Topics:

Local value numbering continued

Announcements

• Grades:

- Expect HW 2 grades by the end of the day
- HW 3 grades are coming shortly after

• HW 5 is out

- It is another big assignment, so get started early!
- Due on Sunday June 11
 - Try to turn it in my Friday so that you have time to study.
- For HW 4, our office hours the first week were almost empty! Please take advantage of them

Final

- Monday June 12 at 8 AM ⊗
- 3 pages of notes allowed
- Comprehensive

Quiz

Quiz

It's the parser's job to perform local value numbering

 \bigcirc True

○ False

- Local value numbering operates over 3 address code
- The parser produces 3 address code
- In some cases, the parser might use LVN, but it is independent

```
a2 = b0 + c1;

b4 = a2 - d3;

c5 = b4 + c1;

d6 = a2 - d3;
```

```
H = {
    "b0 + c1" : "a2",
}
```

Quiz

Local value numbering can only work in just one basic block.

○ True

○ False

• Reminder on a basic block

- Programs can be split into **Basic Blocks**:
 - A sequence of 3 address instructions such that:
 - There is a single entry, single exit

• Important property: an instruction in a basic block can assume that all preceding instructions will execute

How might they appear in a high-level language?

How many basic blocks?

```
...
if (expr) {
    ...
}
else {
    ...
}
...
```

Two Basic Blocks

Single Basic Block

```
Label_x:
op1;
op2;
op3;
br label_z;
```

```
Label_x:
op1;
op2;
op3;
Label_y:
op4;
op5;
```

Label_0:

$$x = a + b;$$

 $y = a + b;$

optimized
to

Label_0:
 $x = a + b;$
 $y = x;$

Quiz

Local value numbering can only work in just one basic block.

○ True

○ False

True!

Although you might imagine algorithms that can work on more basic blocks. This is called *superlocal value numbering*

Quiz

After perform local value numbering on the following program, how many operations can you save?

```
a = b + c;
```

$$d = e * f;$$

$$b = b + c$$
;

$$c = c + b$$
;

$$g = f * e;$$

 \bigcirc 1

O 2

○ 3

O 4

```
a = b + c;
d = e * f;
b = b + c;
c = c + b ;
g = f * e;
```

```
H = {
```

```
a = b + c;
d = e * f;
b = b + c;
c = c + b;
q = f - e;
H = {
}
```

What if we changed this?

Quiz

What is a good order of performing the following optimizations (left to right):

- 1) Local value numbering
- 2) Loop unrolling
- 3) Constant propagation

```
for (int i = 0; i < 10; i++) {
   x = y + z;
}</pre>
```

loop unrolling

```
for (int i = 0; i < 10; i++) {
    x = y + z;
    i++;
    x = y + z;
}</pre>
```

how might this influence other optimizations?

```
a = 16;
b = a + c;
d = 16;
e = d + c;
```

How might constant propagation change this program

```
a = 16;
b = a + c;
d = 16;
e = d + c;
```

How might constant propagation change this program

```
a = 16;
b = 16 + c;
d = 16;
e = 16 + c;
```

```
a = 16;
b = a + c;
d = 16;
e = d + c;
```

How might constant propagation change this program

$$a = 16;$$
 $b = 16 + c;$
 $d = 16;$
 $e = 16 + c;$
 $LVN can$

LVN can now replace the bottom one

It's a little more difficult to apply to ClassleR. Do people have any ideas?

Quiz

What is a good order of performing the following optimizations (left to right):

- 1) Local value numbering
- 2) Loop unrolling
- 3) Constant propagation

Loop unrolling -> Constant propagation -> Local value numbering

Review

- Basic blocks
 - A piece of 3 address code that has one entry and one exit
 - Any line of code can assume that all lines before it have been executed
 - Allows "local" reasoning
 - pycfg example
- Local value numbering
 - Local optimization
 - Simple algorithm that can be built on:
 - initial version just used string comparison
 - next we added commutativity
 - lastly we extended the algorithm to not add any new registers

Review

- Algorithm for applying LVN:
 - split 3 address code into basic blocks
 - for each basic block
 - number the variables
 - try to remove expensive arithmetic operations

Today

- Adding constant folding to LVN
- Discussing memory and functions in LVN
- How to add optimized code blocks back into the IR

- Colloquially, they are often used interchangeably
- Technically (e.g. according to the books)
 - Constant propagation is replacing variables with constants
 - Constant folding is compile-time evaluation when constants are known

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

from: https://en.wikipedia.org/wiki/Constant folding#Constant propagation

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

constant propagation

```
int x = 14;
int y = 7 - 14 / 2;
return y * (28 / 14 + 2);
```

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

constant propagation

```
int x = 14;
int y = 7 - 14 / 2;
return y * (28 / 14 + 2);
```

constant folding

```
int x = 14;
int y = 0;
return y * (4);
```

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

```
int x = 14;
int y = 0;
return 0 * (4);
```

constant propagation

constant propagation

```
int x = 14;
int y = 7 - 14 / 2;
return y * (28 / 14 + 2);
```

constant folding

```
int x = 14;
int y = 0;
return y * (4);
```

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

```
int x = 14;
int y = 0;
return 0 * (4);
```

constant propagation

```
int x = 14;
int y = 7 - 14 / 2;
return y * (28 / 14 + 2);
```

constant folding

```
int x = 14;
int y = 0;
return y * (4);
```

constant

propagation

constant folding

```
int x = 14;
int y = 0;
return 0;
```

Typically performed at the same time

```
int x = 14;
int y = 7 - x / 2;
return y * (28 / x + 2);
```

constant propagation and folding second line

```
int x = 14;
int y = 0;
return y * (28 / x + 2);
```

```
int x = 14;
int y = 0;
return 0;
```

constant propagation and folding third line

```
b = 5;
c = 3;

a = b + c;
b = a - d;
c = a + c;
d = a - d;

Known_values = {
```

numbering

```
b0 = 5;
c1 = 3;
a2 = b0 + c1;
b4 = a2 - d3;
c5 = a2 + c1;
d6 = a2 - d3;
```

```
H = {
}

Known_values = {
```

As you are iterating through code, add any constant mappings to Known_values:

```
b0 = 5;
c1 = 3;
a2 = b0 + c1;
b4 = a2 - d3;
c5 = a2 + c1;
d6 = a2 - d3;
```

```
H = {
}

Known_values = {
```

As you are iterating through code, add any constant mappings to Known_values:

```
b0 = 5;

c1 = 3;

a2 = b0 + c1;

b4 = a2 - d3;

c5 = a2 + c1;

d6 = a2 - d3;
```

```
H = {
}

Known_values = {
"b0" : 5
"c1" : 3
}
```

When you find an arithmetic operation, first check if operands are known

```
b0 = 5;
c1 = 3;
a2 = b0 + c1;
b4 = a2 - d3;
c5 = a2 + c1;
d6 = a2 - d3;
```

```
H = {
}

Known_values = {
"b0" : 5
"c1" : 3
```

When you find an arithmetic operation, first check if operands are known

```
b0 = 5;

c1 = 3;

a2 = b0 + c1;

b4 = a2 - d3;

c5 = a2 + c1;

d6 = a2 - d3;

Known_values = {
"b0" : 5
"c1" : 3
```

When you find an arithmetic operation, first check if operands are known

```
H = {
                     5 + 3
                      evaluate and add to known values
c5 = a2 + c1;
d6 = a2 - d3;
                                        Known_values = {
                                        "b0" : 5
                                        "c1" : 3
                                        "a2" : 8
```

Adding constant folding to LVN

When you find an arithmetic operation, first check if operands are known

```
b0 = 5;
c1 = 3;
a2 = 8;
b4 = 8 - d3;
c5 = a2 + c1;
d6 = a2 - d3;
```

```
propagate constant (if IR allows it)
                   H = {
                   Known_values = {
                   "b0" : 5
                   "c1" : 3
                   "a2" : 8
```

Adding constant folding to LVN

When you find an arithmetic operation, first check if operands are known

add to H

H = {
"8 - d3" : b4
}

Known_values = {
"b0": 5

"c1" : 3
"a2" : 8

why do we want to store 8 here rather than a2?

continue on.

```
b0 = 0;
d3 = 1;
f7 = 4;
a2 = b0 + c1;
b4 = a2 * d3;
d6 = e5 * f7;
```

```
H = {
}

Known_values = {
```

what can we do here?

```
b0 = 0;
d3 = 1;
f7 = 4;
a2 = b0 + c1;
b4 = a2 * d3;
d6 = e5 * f7;
```

```
Known_values = {
"b0":0, "d3":1, "f7":4
}
```

 $H = {$

```
b0 = 0;
d3 = 1;
f7 = 4;
a2 = b0 + c1;
b4 = a2 * d3;
d6 = e5 * f7;
```

what can we do here? add a special rule for + that if any side is 0, you can just drop the 0.

```
H = {
}

Known_values = {
"b0":0, "d3":1, "f7":4
}
```

```
b0 = 0;
d3 = 1;
f7 = 4;
a2 = c1;
b4 = a2 * d3;
d6 = e5 * f7;
```

what can we do here? add a special rule for + that if any side is 0, you can just drop the 0.

```
H = {
}

Known_values = {
"b0":0, "d3":1, "f7":4
}
```

What other rules could we have?

Other considerations in LVN

Memory and functions

Consider a 3 address code that allows memory accesses

```
a[i] = x[j] + y[k];
b[i] = x[j] + y[k];

is this transformation allowed?

a[i] = x[j] + y[k];
b[i] = a[i];
```

• Consider a 3 address code that allows memory accesses

```
a[i] = x[j] + y[k];

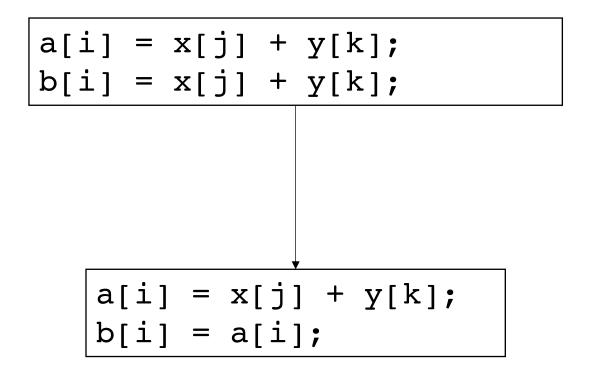
b[i] = x[j] + y[k];
```

is this transformation allowed?
No!

only if the compiler can prove that a does not alias \mathbf{x} and \mathbf{y}

In the worst case, every time a memory location is updated, the compiler must update the value for all pointers.

Consider a 3 address code that allows memory accesses



Example, initially:

What does b[i] equal at the end of each computation?

- How to number:
 - Number each pointer/index pair

```
a[i] = x[j] + y[k];

b = x[j] + y[k];
```

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b,6) = (x[j],?) + (y[k],?);
```

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b,6) = (x[j],4) + (y[k],5);
```

Does this help at all?

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b,6) = (x[j],4) + (y[k],5);

(c,7) = (x[j],4) + (y[k],5);
```

Does this help at all?

If there is no memory writes between an assignment to a variable then we can do a replacement

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b,6) = (x[j],4) + (y[k],5);

(c,7) = (b,6);
```

Does this help at all?

If there is no memory writes between an assignment to a variable then we can do a replacement

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b[i],6) = (x[j],4) + (y[k],5);
```

A compiler analysis might try to determine that addresses can't alias

```
can we trace a, x, y to
a = malloc(...);
x = malloc(...);
y = malloc(...);
// a, x, y are never overwritten
```

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b[i],6) = (x[j],1) + (y[k],2);
```

in this case we do not have to update the number

A compiler analysis might try to determine that addresses can't alias

```
can we trace a, x, y to
a = malloc(...);
x = malloc(...);
y = malloc(...);
// a, x, y are never overwritten
```

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b[i],6) = (x[j],4) + (y[k],5);
```

programmer annotations can also tell the compiler that no other pointer can access the memory pointed to by a

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b[i],6) = (x[j],4) + (y[k],5);
```

in this case we do not have to update the number

restrict a

programmer annotations can also tell the compiler that no other pointer can access the memory pointed to by a

Warning: the compiler does not enforce this!

- How to number:
 - Number each pointer/index pair
 - Any pointer/index pair that might alias must be incremented at each instruction

```
(a[i],3) = (x[j],1) + (y[k],2);

(b[i],6) = (a[i],3);
```

How to number?

```
a = foo(x);
x = b;
c = foo(x);
```

How to number?

the same way

```
a = foo(x);
x = b;
c = foo(x);
```

```
a1 = foo(x0);
x3 = b2;
c4 = foo(x3);
```

What if you had first class functions?

How to number?

the same way

```
a = foo(x);
x = b;
c = foo(x);
```

```
a1 = foo(x0);
x3 = b2;
c4 = foo(x3);
```

Can we replace?

How to number?

the same way

```
a = foo(x);
c = foo(x);
```

```
a1 = foo(x0);
c2 = foo(x0);
```

How about now?

How to number?

the same way

```
a = foo(x);
c = foo(x);
```

```
a1 = foo(x0);
c2 = foo(x0);
```

How about now?

```
int count = 0;
int foo(int x) {
  count += 1;
  return 0;
};
```

What if foo had this implementation?

How to number?

the same way

```
a = foo(x);

c = foo(x);
```

```
a1 = foo(x0);
c2 = foo(x0);
```

How about now?

side effects!

```
int count = 0;
int foo(int x) {
  count += 1;
  return 0;
};
```

What if foo had this implementation?

```
a = foo(x);
c = foo(x);
print(count);
```

```
a1 = foo(x0);
c2 = a1;
print(count);
```

are these two programs the same?

```
int count = 0;
int foo(int x) {
  count += 1;
  return 0;
};
```

• In C/++, functions are assumed to have side effects

- A function that does not have side effects is called "pure"
 - You can annotate a function as pure
 - ___attribute___((pure))
 - warning: compiler does not check this and you can introduce subtle bugs
- Functional languages tend to have a pure-by-default design. Allows more compiler optimizations, but less control to the programmer.

```
a = b + c;
d = e + f;
g = b + c;

label_0:
h = g + a;
k = a + g;
```

split into basic blocks

k = a + q;

```
label_0:
h = g + a;
k = a + g;
```

number

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = b0 + c1;$

```
label_0:
h2 = g0 + a1;
k3 = a1 + g0;
```

move code on slide to make room

```
a2 = b0 + c1;

d5 = e3 + f4;

g6 = b0 + c1;
```

```
label_0:
h2 = g0 + a1;
k3 = a1 + g0;
```

optimize

```
a2 = b0 + c1;

d5 = e3 + f4;

g6 = b0 + c1;
```

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = a2;$

```
label_0:

h2 = g0 + a1;

k3 = a1 + g0;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
```

optimize

a2 = b0 + c1; d5 = e3 + f4;g6 = b0 + c1;

```
label_0:

h2 = g0 + a1;

k3 = a1 + g0;
```

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = a2;$

```
label_0:
h2 = g0 + a1;
k3 = h2;
```

put together?

```
a2 = b0 + c1;
d5 = e3 + f4;
g6 = a2;
label_0:
h2 = g0 + a1;
k3 = h2;
```

What are the issues?

optimize

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = b0 + c1;$

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = a2;$

```
label_0:
h2 = g0 + a1;
k3 = h2;
```

put together?

```
a2 = b0 + c1;
d5 = e3 + f4;
g6 = a2;
label_0:
h2 = g0 + a1;
k3 = h2;
```

undefined!

optimize

stitch
part 1: assign original
variables their latest values

```
a2 = b0 + c1;

d5 = e3 + f4;

g6 = b0 + c1;
```

$$a2 = b0 + c1;$$

 $d5 = e3 + f4;$
 $g6 = a2;$

```
label_0:
h2 = g0 + a1;
k3 = a1 + g0;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
```

```
a2 = b0 + c1;
d5 = e3 + f4;
g6 = a2;
g = g6;
d = d5
a = a2;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
h = h2;
k = k3;
```

make room on slide

```
a2 = b0 + c1;
d5 = e3 + f4;
g6 = a2;
g = g6;
d = d5
a = a2;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
h = h2;
k = k3;
```

what else needs to be done?

stitch part 2: drop numbers from first use of variables

```
a2 = b0 + c1;
d5 = e3 + f4;
g6 = a2;
g = g6;
d = d5
a = a2;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
h = h2;
k = k3;
```

```
label_0:
h2 = g + a;
k3 = h2;
h = h2;
k = k3;
```

Now they can be combined

```
a2 = b + c;
d5 = e + f;
g6 = a2;
g = g6;
d = d5
a = a2;
```

```
label_0:
h2 = g0 + a1;
k3 = h2;
h = h2;
k = k3;
```

```
label_0:
h2 = g + a;
k3 = h2;
h = h2;
k = k3;
```

```
a2 = b + c;
d5 = e + f;
g6 = a2;
g = g6;
d = d5
a = a2;
label 0:
h2 = g + a;
k3 = h2;
h = h2;
k = k3;
```

original

```
a = b + c;
d = e + f;
g = b + c;

label_0:
h = g + a;
k = a + g;
```

new

```
a2 = b + c;
d5 = e + f;
q6 = a2;
g = g6;
d = d5
a = a2;
label 0:
h2 = q + a;
k3 = h2;
h = h2;
k = k3;
```

is it really optimized?

It looks a lot longer...

original

```
a = b + c;
d = e + f;
g = b + c;

label_0:
h = g + a;
k = a + g;
```

new

```
a2 = b + c;
d5 = e + f;
g6 = a2;
g = g6;
d = d5
a = a2;
label 0:
h2 = g + a;
k3 = h2;
h = h2;
k = k3;
```

is it really optimized?

Common pattern for code to get larger, but it will contain patterns that are easier optimize away

later passes will minimize copies

Loop optimizations

For loops

- How do they look in different languages
 - C/C++
 - Python
 - Numpy
- How do Python and Numpy look under the hood?
- The more constrained the for loops are, the more assumptions the compiler can make, but less flexibility for the programmer

For loops

• The compiler can optimize For loops if they fit a certain pattern

- When developing a compiler optimization, we start with strict constraints and then slowly relax them and make the optimization more general.
 - Sometimes it is not worth relaxing the constraints (code gets too complex)
 - If you know the constraints, then often you can write code such that the compiler can recognize the pattern and optimize!

For loops terminology

- Loop body:
 - A series of statements that are executed each loop iteration

- Loop condition:
 - the condition that decides whether the loop body is executed

- Iteration variable:
 - A variable that is updated exactly once during the loop
 - The loop condition depends on the iteration variable

Loop unrolling

• Executing multiple instances of the loop body without checking the loop condition.

```
FOR LPAR assignment_statement expr SEMI assignment_statement RPAR statement
```

unrolled by a factor of 2

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

```
for (int i = 0; i < 128; i++) {
   // body
   i++
   // body
}</pre>
```

Under what conditions can we unroll?

```
FOR LPAR assignment_statement expr SEMI assignment_statement RPAR statement
```

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

Under what conditions can we unroll?

```
FOR LPAR assignment_statement expr SEMI assignment_statement RPAR statement
```

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

Validate that we actually have an iteration variable

- 1. lhs of assignment statement
- 2. no assignment to variable in body
- 3. lhs of loop condition
- 4. lhs of assignment_statement

Do these guarantee we will find an iteration variable? What happens if we don't find one?

Under what conditions can we unroll?

```
FOR LPAR assignment_statement expr SEMI assignment_statement RPAR statement
```

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

Validate that we actually have an iteration variable

- 1. Ihs of assignment statement
- 2. no assignment to variable in body
- 3. lhs of loop condition
- 4. lhs of assignment_statement

How does C-simple help us here?

Do these guarantee we will find an iteration variable? What happens if we don't find one?

Under what conditions can we unroll?

```
FOR LPAR assignment_statement expr SEMI assignment_statement RPAR statement
```

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

Validate properties of iteration variable 1. ?

Under what conditions can we unroll?

```
FOR LPAR assignment statement expr SEMI assignment statement RPAR statement
```

```
for (int i = 0; i < 128; i++) {
   // body
}</pre>
```

Validate properties of iteration variable

- 1. identify an iteration range (start and end)
- 2. increment by 1

See everyone on Friday

Topics: Continue Loop unrolling and other loop optimizations!