

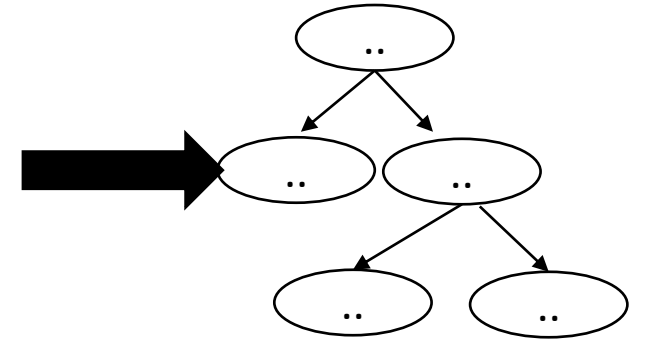
CSE110A: Compilers

April 22, 2022

Topics:

- *Symbol Tables in parsing*
- *Parsing actions*
- *Parser generators*

```
int main() {  
    printf("");  
    return 0;  
}
```



Announcements

- HW 2 is out!
 - due on May 2 at midnight
 - You had everything for part 1 and 2 after wednesday
 - You will have everything you need for part 3 after today
 - Plenty of chances for help. Get started early
- Midterm will be given on May 2
 - Take home midterm.
 - Assigned on Monday and due on Friday
 - No late midterms are accepted
- No class on Monday (use the time to work on homework)

Announcements

- Expect HW 1 grades around May 2
 - You have 2 weeks to do the homework and we get 2 weeks to grade it

Announcements

- HW 2 clarifications:
 - No skeleton for part 1 - it is done completely in your report
 - Please read the piazza for questions about the grammar and other hints

– An assignment statement, which is ID followed by = followed by an expression.

An assignment statement is followed by a semi colon. The language is a subset of C. Anything that C-simple accepts should also be accepted by C (with the same meaning).

Announcements

- Some more homework examples:
 - Variable declarations vs. assignment statements
 - for statements
 - block statements

Quiz

Is the following grammar backtrack free?

$A \rightarrow B a$

$B \rightarrow d a b$

$| C b$

$C \rightarrow c B$

$| A c$

Quiz

First sets

$A \rightarrow B a$ $\{\}$

$B \rightarrow d a b$ $\{\}$

$| C b$ $\{\}$

$C \rightarrow c B$ $\{\}$

$| A c$ $\{\}$

Quiz

First sets

$A \rightarrow B a$ $\{d,c\}$

$B \rightarrow d a b$ $\{d\}$

$| C b$ $\{d,c\}$

$C \rightarrow c B$ $\{c\}$

$| A c$ $\{d,c\}$

no! in both B and C we do not have disjoint first sets

Quiz

Is the following grammar backtrack free?

$A \rightarrow B a$

$B \rightarrow d a b$

$| C b$

$C \rightarrow c B$

$| D$

$D \rightarrow d B$

Quiz

First sets

$A \rightarrow B a$ $\{\}$

$B \rightarrow d a b$ $\{\}$

$| C b$ $\{\}$

$C \rightarrow c B$ $\{\}$

$| D$ $\{\}$

$D \rightarrow d B$ $\{\}$

Quiz

First sets

$A \rightarrow B a$ $\{c,d\}$

$B \rightarrow d a b$ $\{d\}$

$| C b$ $\{c,d\}$

$C \rightarrow c B$ $\{c\}$

$| D$ $\{d\}$

$D \rightarrow d B$ $\{d\}$

No, because for production B the first sets are not disjoint

Quiz

in a recursive descent parser, you make a function for each or what?

production option

CFG

non-terminal

terminal

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit  ::= '(' Expr ') '
5:      | ID
6: Op    ::= '+'
7:      | '*'
```

How do we parse an Expr?

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit  ::= '(' Expr ') '
5:      | ID
6: Op    ::= '+'
7:      | '*'
```

How do we parse an Expr?

We parse a Unit followed by an Expr2

We can just write exactly that!

```
def parse_Expr(self):
    self.parse_Unit();
    self.parse_Expr2();
    return
```

Let's look at the grammar

1: Expr ::= Unit Expr2

2: Expr2 ::= Op Unit Expr2

3: | ""

4: Unit ::= '(' Expr ')'

5: | ID

6: Op ::= '+'

7: | '*'

How do we parse an Expr2?

Let's look at the grammar

1: Expr ::= Unit Expr2

2: Expr2 ::= Op Unit Expr2

3: | ""

4: Unit ::= '(' Expr ')'

5: | ID

6: Op ::= '+'

7: | '*'

How do we parse an Expr2?

First+ sets:

1: {'(', ID}

2: {'+', '*'}

3: {None, ')'}
')'

4: {'('}

5: {ID}

6: {'+'}

7: {'*'}

Let's look at the grammar

1: Expr ::= Unit Expr2

2: Expr2 ::= Op Unit Expr2

3: | ""

4: Unit ::= '(' Expr ')'

5: | ID

6: Op ::= '+'

7: | '*'

How do we parse an Expr2?

First+ sets:

1: {'(', ID}

2: {'+', '*'}

3: {None, ')'}
4: {'('}

5: {ID}

6: {'+'}

7: {'*'}

```
def parse_Expr2(self):
    token_id = get_token_id(self.to_match)

    # Expr2 ::= Op Unit Expr2
    if token_id in ["PLUS", "MULT"]:
        self.parse_Op()
        self.parse_Unit()
        self.parse_Expr2()
        return

    # Expr2 ::= ""
    if token_id in [None, "RPAR"]:
        return

    raise ParserException(-1, self.to_match, ["PLUS", "MULT", "RPAR"])
    # line number (for you to do)
    # observed token
    # expected token
```

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit  ::= '(' Expr ')'
5:      | ID
6: Op    ::= '+'
7:      | '*'
```

How do we parse a Unit?

First+ sets:

```
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:       | ""
4: Unit  ::= '(' Expr ')'
```

```
5:       | ID
```

```
6: Op    ::= '+'
```

```
7:       | '*'
```

First+ sets:

```
1: {'(', ID}
```

```
2: {'+', '*'}  
3: {None, ')'}  
4: {'('}
```

```
5: {ID}
```

```
6: {'+'}
```

```
7: {'*'}
```

How do we parse a Unit?

```
def parse_Unit(self):  
  
    token_id = get_token_id(self.to_match)  
  
    # Unit ::= '(' Expr ')'  
    if token_id == "LPAR":  
        self.eat("LPAR")  
        self.parse_Expr()  
        self.eat("RPAR")  
        return  
  
    # Unit ::= ID  
    if token_id == "ID":  
        self.eat("ID")  
        return  
  
    raise ParserException(-1, self.to_match, ["LPAR", "ID"])  
# line number (for you to do)  
# observed token  
# expected token
```

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit  ::= '(' Expr ')'
```

How do we parse a Unit?

```
5:      | ID
6: Op    ::= '+'
7:      | '*'
```

```
def parse_Unit(self):
```

```
    token_id = get_token_id(self.to_match)
```

```
    # Unit ::= '(' Expr ')'
```

```
    if token_id == "LPAR":
```

```
        self.eat("LPAR")
```

```
        self.parse_Expr()
```

```
        self.eat("RPAR")
```

```
        return
```

```
    # Unit ::= ID
```

```
    if token_id == "ID":
```

```
        self.eat("ID")
```

```
        return
```

```
    raise ParserException(-1,
                           self.to_match,
                           ["LPAR", "ID"])
```

*ensure that to_match has token ID of "LPAREN"
and get the next token*

*# line number (for you to do)
observed token
expected token*

First+ sets:

```
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```

Let's look at the grammar

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:       | ""
4: Unit  ::= '(' Expr ') '
5:       | ID
6: Op    ::= '+'
7:       | '*'
```

How do we parse an Op?

First+ sets:

```
1: {'(', ID}
2: {'+', '*'}
3: {None, ') ' }
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```


Quiz

parsing An LL(1) grammar has a runtime proportional to:

-
- The number of non-terminals

 - The length of the input string

 - The number of tokens in the input string

 - How many times a backtrack might occur

Quiz

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Quiz

parsing An LL(1) grammar has a runtime proportional to:

- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
- How many times a backtrack might occur

Likely plays a small role, but typically the number of non-terminals is much smaller than the input string

Quiz

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- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
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Quiz

parsing An LL(1) grammar has a runtime proportional to:

- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
- How many times a backtrack might occur

Good answer, but potentially the input string is one giant ID. Then the parser simply needs to match one token.

Quiz

parsing An LL(1) grammar has a runtime proportional to:

-
- The number of non-terminals

 - The length of the input string

 - The number of tokens in the input string

 - How many times a backtrack might occur

Quiz

parsing An LL(1) grammar has a runtime proportional to:

- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
- How many times a backtrack might occur

The parser needs to match every single token once. This is the correct answer

Quiz

parsing An LL(1) grammar has a runtime proportional to:

- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
- How many times a backtrack might occur

Quiz

parsing An LL(1) grammar has a runtime proportional to:

- The number of non-terminals
- The length of the input string
- The number of tokens in the input string
- How many times a backtrack might occur

Backtracking is not required for LL(1) grammar

Review

Do we need backtracking?

The First+ set is the combination of First and Follow sets

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit ::= '(' Expr ') '
5:      | ID
6: Op ::= '+'
7:      | '*'
```

```
First+ sets:
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```

For each non-terminal: if every production has a disjoint First+ set then we do not need any backtracking!

Do we need backtracking?

The First+ set is the combination of First and Follow sets

```
1: Expr ::= Unit Expr2
2: Expr2 ::= Op Unit Expr2
3:      | ""
4: Unit ::= '(' Expr ')'
5:      | ID
6: Op ::= '+'
7:      | '*'
```

First+ sets:

```
1: {'(', ID}
2: {'+', '*'}
3: {None, ')'}
4: {'('}
5: {ID}
6: {'+'}
7: {'*'}
```

For each non-terminal: if every production has a disjoint First+ set then we do not need any backtracking!

Sometimes the grammar needs to be refactored

```
1: Factor ::= ID
2:         | ID '[' Args ']'
3:         | ID '('  Args ')'
```

...

Sometimes the grammar needs to be refactored

1: Factor ::= ID	First
2: ID '[' Args ']'	1: {ID}
3: ID '(' Args ')'	2: {ID}
...	3: {ID}
	...

Sometimes the grammar needs to be refactored

```
1: Factor ::= ID
2:         | ID '[' Args ']'
3:         | ID '('  Args ')'
...
```

First

```
1: {ID}
2: {ID}
3: {ID}
...
```

We cannot select the next rule based on a single look ahead token!

Sometimes the grammar needs to be refactored

1: Factor ::= ID	First
2: ID '[' Args ']'	1: {ID}
3: ID '(' Args ')'	2: {ID}
...	3: {ID}
	...

We can refactor

1: Factor ::= ID Option_args	First
2: Option_args ::= '[' Args ']'	1: {ID}
3: '(' Args ')'	2: {'['}
4: ""	3: {'('}
	4: {""}

Sometimes the grammar needs to be refactored

1: Factor ::= ID	First
2: ID '[' Args ']'	1: {ID}
3: ID '(' Args ')'	2: {ID}
...	3: {ID}
	...

We can refactor

1: Factor ::= ID Option_args	First
2: Option_args ::= '[' Args ']'	1: {ID}
3: '(' Args ')'	2: {'['}
4: ""	3: {'('}
	4: {""} // We will need to compute the follow set

Sometimes the grammar needs to be refactored

```
1: Factor ::= ID
2:         | ID '[' Args ']'
3:         | ID '(' Args ')'
...
```

```
First
1: {ID}
2: {ID}
3: {ID}
...
```

It is not always possible to rewrite grammars into a predictive form, but many programming languages can be.

We can refactor

```
1: Factor ::= ID Option_args
2: Option_args ::= '[' Args ']'
3:             | '(' Args ')'
4:             | ""
```

First

```
1: {ID}
2: {'['}
3: {'('}
4: {""}
```

// We will need to compute the follow set

New material

Scope

- What is scope?
- Can it be determined at compile time? Can it be determined at runtime?
- C vs. Python
- Anyone have any interesting scoping rules they know of?

Scope

- Lexical scope example

```
int x = 0;
int y = 0;
{
    int y = 0;
    x+=1;
    y+=1;
}
x+=1;
y+=1;
```

What are the final values in x and y?

Scope

- We can catch certain variable scope errors at parse time
 - e.g. if a variable was declared in the current scope or not

Scope

- Lexical scope example

```
int x = 0;
int y = 0;
{
    int y = 0;
    x+=1;
    y+=1;
}
x+=1;
y+=1;
```

This program should parse and execute

```
int x = 0;
{
    int y = 0;
    x+=1;
    y+=1;
}
x+=1;
y+=1;
```

What about this one?

Scope

- Lexical scope example

```
int x = 0;
int y = 0;
{
    int y = 0;
    x+=1;
    y+=1;
}
x+=1;
y+=1;
```

This program should parse and execute

```
int x = 0;
{
    int y = 0;
    x+=1;
    y+=1;
}
x+=1;
y+=1;
undeclared!
```

What about this one?

How to track scope?

How to track scope?

- Symbol table object
- two methods:
 - **lookup(id)** : lookup an id in the symbol table.
Returns None if the id is not in the symbol table.
 - **insert(id,info)** : insert a new id (or overwrite an existing id) into the symbol table along with a set of information about the id.

What information might we store about an id?

a very simple programming language

ID = [a-z]⁺

INCREMENT = "\+\⁺"

TYPE = "int"

LBRAC = "{"

RBRAC = "}"

SEMI = ";"

```
int x;  
x++;  
int y;  
y++;
```

statements are either a declaration or an increment

a very simple programming language

ID = [a-z]+

INCREMENT = "\+\+"

TYPE = "int"

LBRAC = "{"

RBRAC = "}"

SEMI = ";"

```
int x;  
{  
    int y;  
    x++;  
    y++;  
}  
y++;
```

statements are either a declaration or an increment

a very simple programming language

ID = [a-z]+

INCREMENT = "\+\+"

TYPE = "int"

LBRAC = "{"

RBRAC = "}"

SEMI = ";"

```
int x;  
{  
    int y;  
    x++;  
    y++;  
}  
y++;
```

error!

statements are either a declaration or an increment

How to track scope?

- `SymbolTable ST;`

Say we are matched the statement:
`int x;`

```
declare_statement ::= TYPE ID SEMI  
{ }
```

lookup(id) : lookup an id in the symbol table. Returns None if the id is not in the symbol table.

insert(id,info) : insert a new id (or overwrite an existing id) into the symbol table along with a set of information about the id.

How to track scope?

- `SymbolTable ST;`

Say we are matched the statement:
`int x;`

```
declare_statement ::= TYPE ID SEMI
```

```
{  
  self.eat(TYPE)  
  variable_name = self.to_match[1] # lexeme value  
  self.eat(ID)  
  ST.insert(variable_name, None)  
  self.eat(SEMI)  
}
```

How to track scope?

- `SymbolTable ST;`

Say we are matched string:
`x++;`

```
inc_statement ::= ID INCREMENT SEMI  
{ }
```

lookup(id) : lookup an id in the symbol table. Returns None if the id is not in the symbol table.

insert(id,info) : insert a new id (or overwrite an existing id) into the symbol table along with a set of information about the id.

How to track scope?

- `SymbolTable ST;`

Say we are matched string:
`x++;`

```
inc_statement ::= ID INCREMENT SEMI
{
    variable_name = self.to_match[1] # lexeme value
    if ST.lookup(variable_name) is None:
        raise SymbolTableException(variable_name)
    self.eat(ID)
    self.eat(INCREMENT)
    self.eat(SEMI)
}
```


How to track scope?

- SymbolTable ST;

statement : LBRAC statement_list RBRAC

```
int x;  
{  
    int y;  
    x++;  
    y++;  
}  
y++;
```

How to track scope?

- SymbolTable ST;

statement : LBRAC statement_list RBRAC

start a new scope S

remove the scope S

```
int x;  
{  
    int y;  
    x++;  
    y++;  
}  
y++;
```

How to track scope?

- Symbol table
- **four** methods:
 - **lookup(id)** : lookup an id in the symbol table.
Returns None if the id is not in the symbol table.
 - **insert(id,info)** : insert a new id into the symbol table along with a set of information about the id.
 - **push_scope()** : push a new scope to the symbol table
 - **pop_scope()** : pop a scope from the symbol table

How to track scope?

- `SymbolTable ST;`

statement : **LBRAC** statement_list **RBRAC**

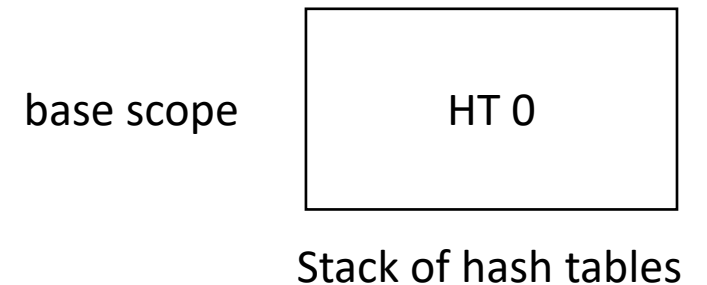
You will be adding the functions to push and pop scopes in your homework

How to implement a symbol table?

- Thoughts? What data structures are good at mapping strings?
- Symbol table
- **four** methods:
 - **lookup(id)** : lookup an id in the symbol table.
Returns None if the id is not in the symbol table.
 - **insert(id, info)** : insert a new id into the symbol table along with a set of information about the id.
 - **push_scope()** : push a new scope to the symbol table
 - **pop_scope()** : pop a scope from the symbol table

How to implement a symbol table?

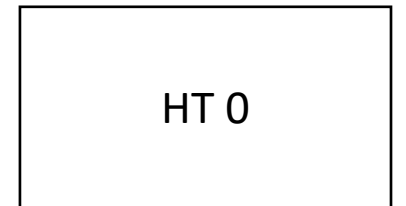
- Many ways to implement:
- A good way is a stack of hash tables:



How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

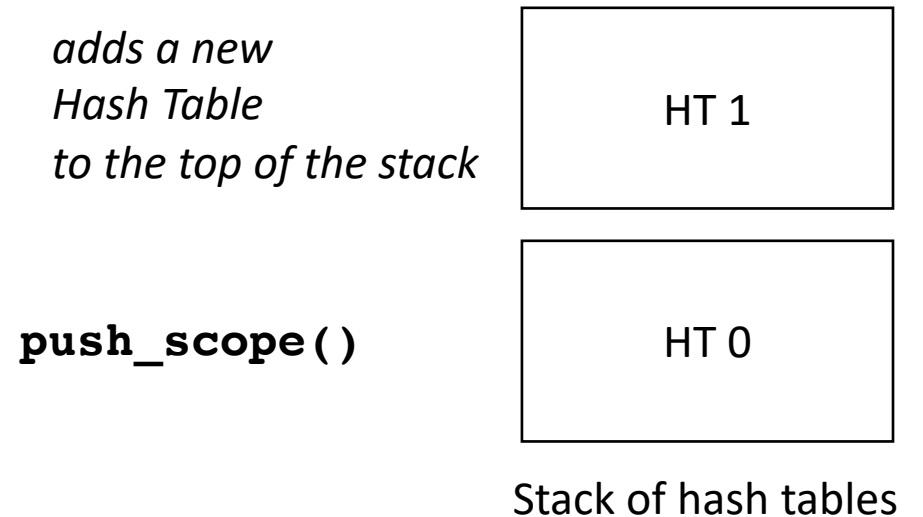
push_scope()



Stack of hash tables

How to implement a symbol table?

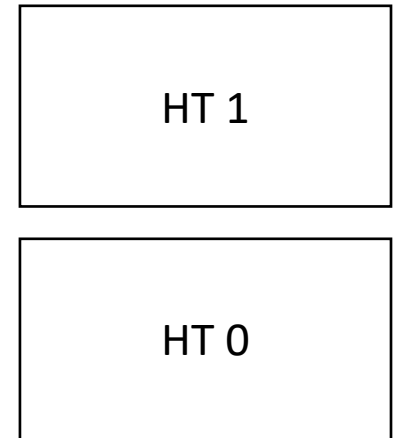
- Many ways to implement:
- A good way is a stack of hash tables:



How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

`insert(id, data)`



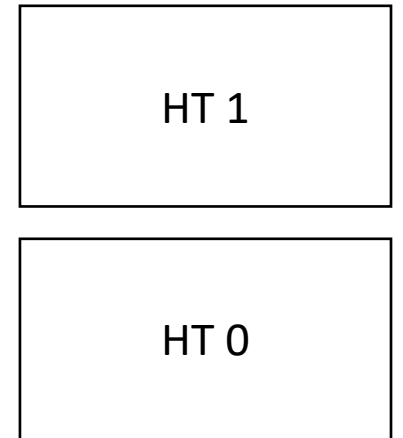
Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

`insert(id, data)`

`insert(id -> data)` at
top hash table

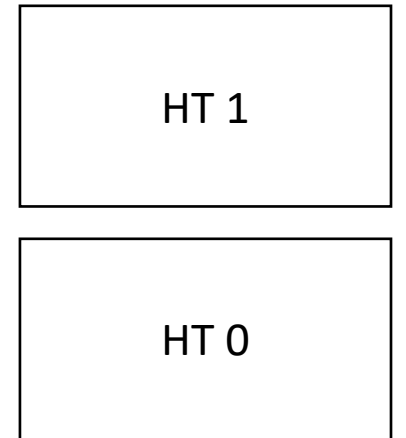


Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

lookup(id)



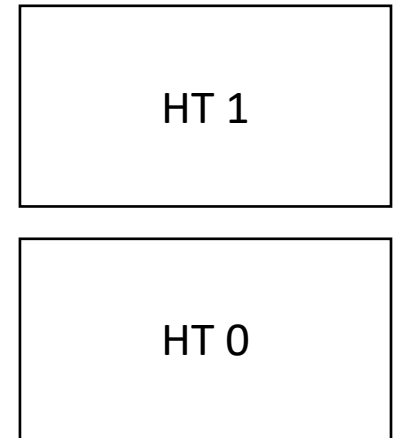
Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

lookup(id)

check here
first



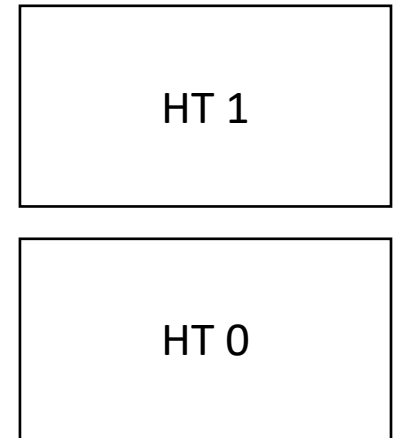
Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

lookup(id)

then check
here

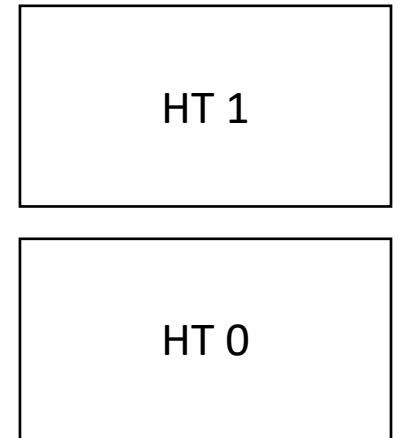


Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
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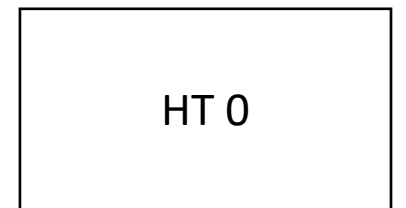
pop_scope ()



Stack of hash tables

How to implement a symbol table?

- Many ways to implement:
- A good way is a stack of hash tables:

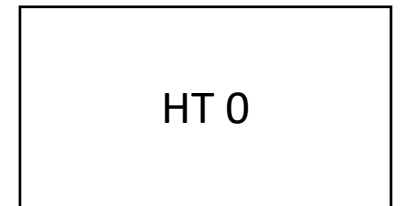


Stack of hash tables

How to implement a symbol table?

- Example

```
int x = 0;
{
    int y = 0;
    y++;
    x++;
}
x++;
y++;
```



Stack of hash tables

Parser actions

Parser actions

- Like token actions: perform an action each time a production option is matched. Useful for: tracking state

Parser actions

- Like token actions: perform an action each time a production option is matched.
- Typically performed after the entire production action is matched
- Useful for:
 - tracking state

Example

- `SymbolTable ST;`

Say we are matched the statement:
`int x;`

```
declare_statement ::= TYPE ID SEMI
```

```
{  
    self.eat(TYPE)  
    variable_name = self.to_match[1] # lexeme value  
    self.eat(ID)  
    ST.insert(variable_name, None)  
    self.eat(SEMI)  
}
```

If we wrote our own recursive descent parser we can implement our own actions inlined

Example

Say we are matched the statement:
`int x;`

- `SymbolTable ST;`

Parser actions would be written like this

```
                                $1  $2  $3
declare_statement ::= TYPE ID SEMI
{
    ST.insert($2, None);
}
```

*result of each symbol.
For a terminal it will be
the value*

always some way to refer to symbol value, e.g. an array

What values get returned from non-terminals?

```
1: Expr ::= Expr '+' Unit      {print $1}  
2:      | Expr '-' Unit  
3:      | Unit  
4: Unit ::= '(' Expr ')'  
5:      | NUM
```

What does this print?

What values get returned from non-terminals?

```
1: Expr ::= Expr '+' Unit    {print $1; return "expr"}
2:      | Expr '-' Unit      {return "expr"}
3:      | Unit                {...}
4: Unit ::= '(' Expr ')'
5:      | NUM
```

*Each production rule
needs to return something*

What values get returned from non-terminals?

building a calculator

```
1: Expr ::= Expr '+' Unit {}
2:      | Expr '-' Unit  {}
3:      | Unit            {}
4: Unit  ::= '(' Expr ')' {}
5:      | NUM            {}
```


What values get returned from non-terminals?

building a calculator

```
1: Expr ::= Expr '+' Unit    {return $1 + $3}
2:      | Expr '-' Unit     {return $1 - $3}
3:      | Unit                {return $1}
4: Unit ::= '(' Expr ')'     {return $2}
5:      | NUM                 {return $1}
```

Shortcomings of parser actions

Difficult to perform actions in the middle of a production

- `SymbolTable ST;`

statement : **LBRAC** statement_list **RBRAC**

```
int x;  
{  
    int y;  
    x++;  
    y++;  
}  
y++;
```

start a new scope S

remove the scope S

Parser generators

- You provide the CFG, along with some hints, you get a parser back
- They typically use bottom-up parsers
 - Algorithm is more complicated
 - Able to handle more types of grammars naturally
 - Able to naturally encode precedence and associativity
- Examples of tools:
 - Yacc, Antrl, PLY

calculator example

These slides follow the calculator example from the PLY documentation

calculator example

```
import ply.lex as lex

tokens = ["NUM", "MULT", "PLUS", "MINUS", "DIV", "LPAR", "RPAR"]

t_NUM = '[0-9]+'
t_MULT = '\*'
t_PLUS = '+'
t_MINUS = '-'
t_DIV = '/'
t_LPAR = '('
t_RPAR = ')'

t_ignore = ' '

# Error handling rule
def t_error(t):
    print("Illegal character '%s'" % t.value[0])
    exit(1)

lexer = lex.lex()
```

Set up the lexer

calculator example

- *Import the library*

```
import ply.yacc as yacc
```

- Simple rule

```
def p_expr_num(p):  
    "expr : NUM"  
    p[0] = int(p[1])
```

functions are given prefixed by p_

production rules are the doc string

return values are stored in p[0]

children values are in p[1], p[2], etc.

calculator example

- *Try it out*

calculator example

- *Next rule*

```
def p_expr_plus(p):  
    "expr : expr PLUS expr"  
    p[0] = p[1] + p[3]
```

- Try it again

calculator example

- Set associativity (and precedence)

```
precedence = (  
    ('left', 'PLUS'),  
)
```

calculator example

- *Next rules*

```
def p_expr_minus(p):  
    "expr : expr MINUS expr"  
    p[0] = p[1] - p[3]
```

```
def p_expr_mult(p):  
    "expr : expr MULT expr"  
    p[0] = p[1] * p[3]
```

```
def p_expr_div(p):  
    "expr : expr DIV expr"  
    p[0] = p[1] / p[3]
```

```
precedence = [  
    ('left', 'PLUS', 'MINUS'),  
    ('left', 'MULT', 'DIV'),  
]
```

calculator example

- *Last rule for expressions*

```
def p_expr_par(p):  
    "expr : LPAR expr RPAR"  
    p[0] = p[2]
```

calculator example

- *An extra we can easily implement*

```
def p_expr_div(p):  
    "expr : expr DIV expr"  
    if p[3] == 0:  
        print("divide by 0 error:")  
        print("cannot divide: " + str(p[1]) + " by 0")  
        exit(1)  
    p[0] = p[1] / p[3]
```

calculator example

- *Combining rules:*

```
def p_expr_plus(p):  
    "expr : expr PLUS expr"  
    p[0] = p[1] + p[3]
```

```
def p_expr_minus(p):  
    "expr : expr MINUS expr"  
    p[0] = p[1] - p[3]
```

```
def p_expr_mult(p):  
    "expr : expr MULT expr"  
    p[0] = p[1] * p[3]
```

```
def p_expr_bin(p):  
    """"  
    expr : expr PLUS expr  
          | expr MINUS expr  
          | expr MULT expr  
    """"  
    if p[2] == '+':  
        p[0] = p[1] + p[3]  
    elif p[2] == '-':  
        p[0] = p[1] - p[3]  
    elif p[2] == '*':  
        p[0] = p[1] * p[3]  
    else:  
        assert(False)
```

calculator example

- Other useful options
 - Error recovery
 - Error reporting (it is better in our top down parsers)
- Question: how would we do a calculator implementation in our C-simple grammar? It is not left recursive so it is not as natural...

See you on Wednesday!

- Work on HW 2
- Starting the next module: intermediate representations